

# THE CONTRIBUTION OF STRUCTURAL BREAK MODELS TO FORECASTING MACROECONOMIC SERIES

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**Abstract:** This paper compares the forecasting performance of different models which have been proposed for forecasting in the presence of structural breaks. These models differ in their treatment of the break process, the model which applies in each regime and the out-of-sample probability of a break occurring. In an extensive empirical evaluation involving 60 macroeconomic quarterly and monthly time series, we demonstrate the presence of structural breaks and their importance for forecasting in the vast majority of cases. We find no single forecasting model consistently works best in the presence of structural breaks. In many cases, the formal modeling of the break process is important in achieving good forecast performance. However, there are also many cases where simple, rolling window based forecasts perform well.

**Keywords:** Forecasting, change-points, Markov switching, Bayesian inference.

**JEL Classification:** C11, C22, C53.

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# 1 Introduction

Structural breaks are commonly found to be present in many macroeconomic and financial time series (e.g. Stock and Watson (1996) and Ang and Bekaert (2002)) and to be one of the major reasons of poor forecasting performance (e.g. Clements and Hendry (1998)). This has led to several papers working with univariate forecasting methods which are robust to breaks (e.g. Pesaran and Timmermann (2007), Eklund, Kapetanios, and Price (2009) or Clark and McCracken (2009)) or formally model the break process (e.g. McCulloch and Tsay (1993), Pesaran, Pettenuzzo, and Timmermann (2006), Koop and Potter (2007), Giordani and Kohn (2008), and Maheu and Gordon (2008)). The latter class of models is typically estimated by Bayesian inference because they involve latent variables and use a specific prior specification tailored for forecasting.

It is an open empirical question as to which types of methods or models work best when dealing with the sort of structural change present in many macroeconomic series. The purpose of this paper is to shed light on this question. We compare empirically the forecasting performance of existing models that explicitly allow for structural breaks both in the sample period and in the forecast period. We use the models defined in Pesaran, Pettenuzzo, and Timmermann (2006), hereafter PPT, Koop and Potter (2007), hereafter KP, and Giordani and Kohn (2008), hereafter GK, and these form the main focus of our forecast evaluation. Conventional time-varying parameter (TVP) models also allow explicitly for structural breaks in-sample and out-of-sample and are also included in our forecast evaluation. In addition, we include some basic forecasting procedures based on recursive and rolling windows, and an unobserved component model with stochastic volatility.

Only a limited number of large scale forecasting exercises for macroeconomic time series exist in the literature. Meese and Geweke (1984) apply five autoregressive forecasting techniques to 150 quarterly and monthly series and study also the impact of preliminary data transformations. Stock and Watson (1996) consider eight univariate and eight bivariate specifications, including TVP models, to forecast 76 monthly univariate series. Marcellino, Stock, and Watson (2006) focus on the more specific empirical question whether autoregressive model iterated forecasts outperform direct forecasts by considering 170 monthly series.

This is the first paper that studies the forecasting performance of state-of-the-art structural break models. Our study is in the same spirit as the above large scale forecasting

exercises in the sense that we investigate the performance of various forecasting approaches at different forecast horizons in a set of macroeconomic time series using relatively simple autoregressive forecasting models. To be precise, for thirty-nine quarterly and twenty-one monthly macroeconomic series between 1959 and 2011, we consider eight break and seven<sup>1</sup> no-break type models to produce forecasts at several horizons. We consider less series than in the studies cited above because performing our exercise for hundreds of series would be too costly in computation time. We do sensitivity analyses to investigate the forecast performance since the beginning of the great recession. In addition we check if the results depend on the choice of some prior parameters and we find little impact.

We evaluate forecast performance using two metrics. In addition to a conventional measure based on point forecasts, i.e. root mean squared forecast error (RMSE), we also use average predictive likelihoods (APL) which are based on the entire predictive density that can be easily obtained with the Bayesian estimation procedure. It turns out that the two loss functions yield substantially different conclusions. In fact, while the break type models seem to dominate no-break models in terms of RMSE, the reverse is often true in terms of APL. However, if we restrict our evaluations to the subset of break models, we find that KP and PPT models perform better on average than GK and TVP models.

Structural break models can differ in important aspects, such as the hierarchical prior specification on the conditional mean and variance and the prior on the regime duration. Furthermore, some approaches impose the restriction that a precise number of breaks occurs in-sample, whereas in others the number of in-sample breaks is treated as unknown. It is eventually an empirical matter which of these approaches works well in practice and it is possible that each approach forecasts well in some cases but not in others. KP and PPT each illustrate the performance of their approaches with a single time series and with modeling details calibrated to that particular series, while GK do the same with two series. We find that structural breaks are an important feature of most of the time series we consider. Formally modeling such breaks is shown to be an important issue for forecasting. However, we find that there is no one single method which can be recommended universally. That is, for some series PPT forecasts best, for others KP or GK do, for others simpler methods such as rolling window based forecasts perform best. We argue that this is empirically sensible and stress the

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<sup>1</sup>Actually, nine for the monthly series.

importance of tailoring forecasting models to the empirical application at hand as opposed to recommending a single approach as being universally best for all macroeconomic time series.

We use autoregressive models or extensions thereof without explanatory variables. Although additional regressors could enhance predictability, doing so for the series used in this paper would enlarge considerably the scope of our study. It would require us to take many decisions linked to the choice of regressors and the need to forecast their future values when forming more than one-step ahead forecasts. Related to this, we also leave aside the investigation of multivariate models because the break models we consider here would require nontrivial adaptations (those models have been proposed only for univariate time series) and because a large scale study would involve too many possible models. This is the reason why for example D’Agostino, Gambetti, and Giannone (2009) consider only three main macroeconomic series and a standard trivariate TVP model in their forecasting evaluation.

In Section 2, we compare in a non-technical manner the specifications of the PPT, KP, and GK models that we use in our empirical evaluation. Technical details about estimation and forecasting are provided in an online technical appendix.<sup>2</sup> In Section 3, we present the estimation results of applying PPT, KP, and GK to the series we analyze using the full sample, focussing on the presence and timing of breaks in the series. In Section 4 we present our main results. Section 5 contains the results of sensitivity analyses and the last section our conclusions and future research directions.

## 2 Models with and without Structural Breaks

In this section, we present the break models used in the forecast evaluation exercise that is the main objective of the paper. After providing a framework for structural break models, we discuss how the parameters of different regimes are linked, how the break process is modeled, and how the number of breaks is determined in the PPT and KP models. We present the GK models that we use in subsection 2.5. In subsection 2.6, we present the ”no-break” models used in the forecast comparisons.

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<sup>2</sup>Downloadable at [http://personal.strath.ac.uk/gary.koop/bkk\\_r\\_ta\\_webversion.pdf](http://personal.strath.ac.uk/gary.koop/bkk_r_ta_webversion.pdf)

## 2.1 A Framework for Structural Break Modelling

A linear regression model framework for discussing structural break models is:

$$y_t = Z_t \beta_{s_t} + \sigma_{s_t} \varepsilon_t, \quad (1)$$

where  $y_t$  ( $t = 1, \dots, T$ ) is the dependent variable,  $Z_t$  (with  $m$  elements in total) contains lagged dependent variables or lagged exogenous variables available for forecasting  $y_t$ , and  $\varepsilon_t$  is i.i.d.  $N(0, 1)$ . Equation (1) allows for  $\beta_{s_t}$  and  $\sigma_{s_t}$  to vary over time with  $s_t \in \{1, \dots, K\}$  a random variable indicating which regime applies at time  $t$ . The vector  $\beta_{s_t}$  determines the conditional mean of  $y_t$  and, thus, we will refer to them as conditional mean coefficients with  $\sigma_{s_t}$  being the volatilities.

Different structural break models vary in the way they model the break process. To be concise, we focus our exposition on  $\beta_{s_t}$ , without repeating the arguments for  $\sigma_{s_t}$ . But we stress that breaks in volatilities can be modeled in exactly the same manner as breaks in the conditional mean coefficients and in our empirical work we allow for breaks in volatility. Furthermore, in principle we could allow for breaks in volatility to occur independently of breaks in the conditional mean. In this case,  $s_t$  is a bivariate discrete random variable with the first element controlling breaks in conditional mean and the second element controlling breaks in volatility.

## 2.2 Linking the Parameters in Different Regimes

It is possible to allow for  $\beta_j$  for  $j = 1, \dots, K$  to be completely independent of one another, i.e. after a break occurs, pre-break information provides absolutely no information about what likely values for the new conditional mean coefficients are. But, in practice, it is typically desirable to avoid such independence when forecasting subject to structural breaks. Suppose a break occurs during the forecast period, and the conditional mean coefficient switches from  $\beta_j$  to  $\beta_{j+1}$ . Forecasting must be done using  $\beta_{j+1}$ . If we assume complete independence of conditional mean coefficients across regimes, then immediately after the break we have no data-based information to estimate  $\beta_{j+1}$ . In a Bayesian forecasting exercise, this means the prior for  $\beta_{j+1}$  will be used to produce forecasts. Given a common desire to use relatively noninformative priors, this could lead to extreme and unreasonable forecasts when a break occurs. This has motivated various models which link  $\beta_j$  and  $\beta_{j+1}$  in some manner.

In this paper, we consider two main approaches. The first approach (used in PPT) is to adopt a link of the form  $\beta_j = \beta_0 + u_j$  for  $j = 1, \dots, K$ , where  $u_j$  is i.i.d.  $N_m(0, B_0)$  or, equivalently, in Bayesian language, a hierarchical prior of the form  $\beta_j \sim N_m(\beta_0, B_0)$ , where the parameters  $\beta_0$  and  $B_0$  are assumed unknown and can be estimated from the data. Thus, the conditional mean coefficients in each regime are drawn independently from a common distribution. This practice is commonly used in panel data models with random effects or in random coefficient models and results from that literature can easily be adapted to show that  $\beta_0$  and  $B_0$  reflect average values across all regimes. If a break occurs in a forecast period, this means that the new value of the conditional mean coefficients will be drawn from a distribution which reflects the values of the coefficients from all past regimes. This is an empirically sensible approach in environments where breaks occur, but in a recurrent way. It allows, for instance, for the 1950s, 1970s, 1990s and 2000's to be different regimes, but the regime in the 2000s is just as likely to be similar to the 1950s as to more recent regimes.

The second approach, used both by PPT and KP, adopts a hierarchical prior motivated by the state space literature on TVP models. They specify random walk evolution of coefficients, say  $\beta_j = \beta_{j-1} + u_j$ , where  $u_j$  is specified as above, or equivalently,  $\beta_j | \beta_{j-1} \sim N_m(\beta_{j-1}, B_0)$ . This hierarchical prior embodies a dependence between the coefficients of successive regimes: when a break occurs, the conditional mean coefficients are drawn from a distribution centered at  $\beta_{j-1}$ . Thus, it is the most recent regime which has the most influence on conditional mean coefficients in a new regime. This is a common modelling assumption in macroeconomic models such as TVP-VARs and, indeed, the KP model is equivalent to a TVP regression model if  $s_t = t$  and, thus,  $K = T$ .

The difference between the dependent and the independent hierarchical priors described above vanishes if the prior covariance ( $B_0$ ) is large. In the hierarchical setup,  $B_0$  is a random parameter, hence "large" means large on average. Intuitively  $B_0$  will tend to be large if the number of breaks is small, in which case the explained difference between the two priors will not affect much the posterior and predictive results.

In brief, we use the independent prior with the PPT model and the dependent prior with the KP model, both being lightly informative. For the PPT model, the prior, including the

prior hierarchy or the error variance parameters  $\sigma_j$  in (1), is defined by

$$\begin{aligned} \beta_j | \beta_0, B_0 &\sim N_m(\beta_0, B_0), \beta_0 \sim N_m(\underline{\mu}_\beta, \underline{V}_\beta), B_0^{-1} \sim \text{Wishart}(\underline{\xi}, \underline{B}), \\ \sigma_j^{-2} | v_0, d_0 &\sim \text{Gamma}(v_0, d_0), v_0 \sim \text{Gamma}(\underline{\lambda}, \underline{\rho}), d_0 \sim \text{Gamma}(\underline{c}, \underline{d}). \end{aligned}$$

For the forecasting evaluation in Section 4, we set  $\underline{\mu}_\beta = 0$ ,  $\underline{V}_\beta = I_m$ ,  $\underline{B} = 10I_m$ ,  $\underline{\xi} = m + 1$  (where  $m$  is the dimension of  $Z_t$ ),  $\underline{\lambda} = 1$ ,  $\underline{\rho} = 0.1$ ,  $\underline{c} = 1$ , and  $\underline{d} = 0.1$ .

For KP, the prior is

$$\begin{aligned} \beta_j &\sim N_m(\beta_{j-1}, B_0), \beta_0 \sim N_m(0, \underline{V}_\beta), B_0^{-1} \sim \text{Wishart}(\underline{\xi}, \underline{B}), \\ \omega_j &\sim N(\omega_{j-1}, \delta), \omega_0 \sim N(0, \underline{V}_\omega), \delta^{-1} \sim \text{Gamma}(\underline{\kappa}_1, \underline{\kappa}_2), \end{aligned}$$

where  $\omega_j = \log \sigma_j$ . For the forecasting evaluation in Section 4, we set  $\underline{V}_\beta = I_m$ ,  $\underline{V}_\omega = 1$ ,  $\underline{B} = 10I_m$ ,  $\underline{\xi} = m + 1$ , and  $\underline{\kappa}_1 = \underline{\kappa}_2 = 0.5$ .

Further discussion of the prior is given in Section 5.2. The online technical appendix (TA) provides details on relevant posterior and predictive simulation algorithms.

### 2.3 Modeling the Break Process

The break process is modeled through  $S_T = (s_1, \dots, s_T)'$  where  $s_t \in \{1, 2, \dots, K\}$  are the regime identifying (or state) variables defined previously. It is possible to use a noninformative prior which does not restrict the timing of the breaks. This is an approach developed in Koop and Potter (2009). However, unless the number of breaks is small, computation is difficult (or infeasible) due to the large number of possible configurations of  $K$  breakpoints (i.e.  $T^K$ ). Furthermore, when forecasting under structural breaks, it is necessary to forecast the probability that a break occurs during the forecast period and this cannot be done using a noninformative prior for  $S_T$ . This has led to an interest in informative hierarchical priors for the break process. The most popular of these is developed in Chib (1998) and adopted by PPT. This begins by assuming a restricted Markov process for  $S_T$ :

$$\begin{aligned} \Pr(s_t = i | s_{t-1} = i) &= p_i \\ \Pr(s_t = i + 1 | s_{t-1} = i) &= 1 - p_i. \end{aligned} \tag{2}$$

Thus, if regime  $i$  holds at time  $t - 1$ , then at time  $t$  the process can either remain in regime  $i$  (with probability  $p_i$ ) or a break occurs and the process moves to regime  $i + 1$  (with probability  $1 - p_i$ ). Equation (2) can be interpreted as a hierarchical prior. It can be shown that (2)

implies a Geometric prior distribution for the duration of regime  $i$ , denoted by  $d_i$  and defined as the number of periods  $t$  for which  $s_t = i$ .

KP argue that this may be restrictive in some situations. For instance, the geometric distribution is decreasing and, thus, this hierarchical prior imposes  $p(d_i) > p(d_i + 1)$ . They suggest the use of the more flexible Poisson distribution for the durations, i.e.  $d_i - 1 \sim \text{Poisson}(\lambda_i)$ . However, in the present paper, in order to avoid the computational complexity inherent to the use of the Poisson prior we implement the KP approach using the Geometric prior implied by (2). The KP model of this paper is thus to be understood from here on to differ from the model of Koop and Potter (2007) in this aspect.

The same prior for  $p_i$  is used in all PPT and KP models. It does not depend on  $i$  and in practice we use a uniform distribution on the unit interval.

## 2.4 Choosing the Number of Breaks

Thus far, we have said nothing about choosing  $K - 1$ , the number of breaks. But this raises an important issue. Note that both the Geometric and Poisson duration distributions have unbounded support. Thus, it is possible that any regime endures beyond the end of the sample. For instance, if the sample runs from  $t = 1, \dots, T$  and the model has three breaks, it is possible that  $s_T = 1$  or  $2$  and, thus, that the third regime has not begun before  $T$ . PPT and KP adopt two different ways of dealing with this issue, which we describe in turn (technical details are provided in the TA).

PPT, following Chib (1998), impose additional prior information beyond (2). Intuitively, we can impose that exactly  $K$  regimes occur in sample by adding prior information of the form:

$$\Pr[s_T = K | s_{T-1} = K] = \Pr[s_T = K | s_{T-1} = K - 1] = 1. \quad (3)$$

Thus, if the process reaches the final regime before the end of the sample it stays there. But if it has not reached the final regime by period  $T - 1$ , it must switch to the final regime. If  $K$  exceeds 2, additional restrictions are required. To express these restrictions in words, consider the case  $K = 3$ . If, in period  $T - 1$ , we are not already in the third regime, then it must be the case that a regime switch occurs in period  $T$  and this must be imposed on the model. Similarly, if, in period  $T - 2$ , we are still in the first regime, then we must impose that regime switches occur in both periods  $T - 1$  and  $T$ , in order to ensure that  $K = 3$ . Note that,



as discussed in Koop and Potter (2009), this can lead to a pile-up of prior probability near the end of the sample, leading to a prior which is quite informative (and, thus, potentially influential) precisely at the time forecasting is being done.

KP simply recommend working with models which allow for breakpoints to occur out-of-sample. Statistically, working with such models poses no difficulties for a Bayesian using a proper prior. Consider the case where regime  $j$  occurs entirely out-of-sample. It appears that there is no data to directly estimate  $\beta_j$ . However, Bayesian inference is still possible. If the prior for  $\beta_j$  were independent of the conditional mean coefficients in the other regimes, then its posterior would simply equal its prior. Such an approach would allow for valid statistical inference but could yield poor forecasting results unless strong prior information existed about  $\beta_j$ . However, using hierarchical priors allows for data information from in-sample regimes to spill over into out-of-sample regimes and, thus, the posterior for  $\beta_j$  will contain data information. More importantly, allowing for regimes to occur out-of-sample allows us to estimate the number of regimes in-sample. For instance, if we allow for two breakpoints, but one of these occurs after time  $T$ , then (in-sample) this is equivalent to estimating a model with one breakpoint. This means that we can simply select a value for the maximum number of breakpoints to allow for as opposed to doing a search over all possible numbers. By contrast, with the PPT approach, marginal likelihoods are calculated for  $K = 1, ..K^{\max}$  and the value with the highest marginal likelihood is selected.

## 2.5 Mixture Innovation and TVP Models

GK follow a dynamic mixture approach, that is a state-space model where the state error is driven by a mixture distribution, in order to model the break process. We use the following form of the model:

$$y_t = Z_t\beta_t + \sigma_t\varepsilon_t, \quad (4)$$

$$\beta_t = \beta_{t-1} + k_{1,t}u_t, \quad (5)$$

$$\log \sigma_t = \log \sigma_{t-1} + k_{2,t}v_t, \quad (6)$$

where  $\varepsilon_t \sim N(0, 1)$ ,  $u_t \sim N(0, B_0)$ ,  $v_t \sim N(0, \delta_0)$ ,  $k_{1,t}$  and  $k_{2,t}$  are each an independent sequence of Bernoulli variables, and furthermore the two sequences are mutually dependent. Thus, for  $i = 1$  and  $i = 2$ ,  $k_{i,t} = 1$  with probability  $\pi$  and  $k_{i,t} = 0$  with probability  $1 - \pi$ .

\*\*\* DO WE HAVE A SINGLE  $\pi$  OR TWO OF THEM ( $\pi_1$  AND  $\pi_2$ )? \*\*\*

Using this specification, the state errors  $\tilde{u}_t = k_{1,t}u_t$  and  $\tilde{v}_t = k_{2,t}v_t$  are mixtures of a normal component (with probability  $\pi$ ) and a point mass at zero (with probability  $1 - \pi$ ). Upon occurrence of a break ( $k_{1,t} = k_{2,t} = 1$ ) the parameters evolve exactly as in KP. When  $k_{1,t} = k_{2,t} = 0$ , we stay in the same regime, since  $\beta_t = \beta_{t-1}$  and  $\log \sigma_t = \log \sigma_{t-1}$ . A change in either  $\beta_t$  or  $\sigma_t$  can also happen ( $k_{1,t} = 0$  with  $k_{2,t} = 1$  or vice-versa). In that respect, this makes this model more flexible than KP and PPT. Notice however that in PPT and KP the state variable  $s_t$  is driven by a dependent process (a Markov chain), whereas in the mixture innovation model the state variables are driven by independent processes.

Another feature that differentiates the mixture innovation model from the ones presented so far is the way the state variables are estimated: instead of relying on the algorithm of Chib (1998), they can be estimated using state-space methods. GK rely on the efficient methods of Gerlach, Carter, and Kohn (2000) for estimating  $k_{1,t}$  and  $k_{2,t}$  without having to condition on the remaining model parameters and states.

We use two versions of this model. The first one, which is a generalization of McCulloch and Tsay (1993), is based on assuming that the prior on the regime duration is geometric with mean  $\pi/(1 - \pi)$  and standard deviation  $\sqrt{(1 - \pi)}/\pi$ . The second version is closer to the original specification of KP since it assumes that the prior on the regime duration is based on the Poisson distribution with parameter  $\lambda_i$ , i.e. the prior  $p(d_i - 1)$  is  $\text{Poisson}(\lambda_i)$ , for  $i = 1, \dots, K$ . Correspondingly, we use two sets of priors for the parameter  $\pi$ .

The first one, which corresponds to the geometric regime duration, is of the form  $\pi \sim \text{Beta}(0.1, 10)$ . In the spirit of the original model of McCulloch and Tsay (1993), this prior encourages few breaks. We label this model GKxB (B for Bernoulli prior, x=1 or 4 denoting the lag order of the autoregressive part corresponding to  $Z_t\beta_t$ ).

The second prior is more complicated, since the probability of a break is time-varying. Denoting this probability at time  $t$  as  $p(k_t|k_{t' \neq t})$ , where  $k_t = (k_{1,t} k_{2,t})$ , then

\*\*\* NOT CLEAR WHAT THESE PROBABILITIES ARE SINCE  $k_t$  IS BIVARIATE \*\*\*

$$\begin{aligned} p(k_t = 1|k_{t' \neq t}) &= p(d_{1t})p(d_{2t}), \\ p(k_t = 0|k_{t' \neq t}) &= p(d_{3t}), \end{aligned}$$

where  $d_{1t}$  and  $d_{2t}$  are the number of periods (duration) between two adjacent breaks, and  $d_{3t}$  is the number of periods between the last break before period  $t$  and the first break after

period  $t$  (see GK for details). Finally, adopting the Poisson prior approach of Koop and Potter (2007), the prior for these durations is a Poisson probability mass function with the following hierarchical structure:

$$d_{it} - 1 \sim \text{Poisson}(\lambda_i), \lambda_i \sim \text{Gamma}(12, \beta_\lambda), \beta_\lambda^{-1} \sim \text{Gamma}(12, 12).$$

We label this model GKxP (P for Poisson, x=1 or 4 indicating the lag order).

The priors we use for for the other parameters in both versions are

$$\begin{aligned} \beta_0 &\sim N_m(0, 4I_m), \quad \log \sigma_0 \sim N(0, 1) \quad \delta_0^{-1} \sim \text{Gamma}(1, 0.1), \\ B_0^{-1} &\sim \text{Wishart}(m+1, (0.001^2(m+1)R)^{-1}), \end{aligned}$$

where  $R$  is a diagonal matrix with elements  $R\{1, 1\} = 5$  for the intercept, and  $R\{i, i\} = 1/i$  for lag length  $i = 1, \dots, p$ .

Finally, the time-varying parameter models are obtained by setting  $k_{1,t} = k_{2,t} = 1$  for all  $t$  in (5) and (6). They are labeled TVP1 (1 lag) and TVP4 (4 lags).

## 2.6 No-break Models

In addition to the break models described above, we consider a few other models. These models can be viewed as no-break models since they do not include a process generating the breaks.

Firstly, we estimate AR( $q$ ) models on rolling windows to generate forecasting results (with  $q$  set to 1 and to 4). Bayesian inference is used for these models using the same prior density as in the PPT implementations if we allow for a single regime.<sup>3</sup> For the quarterly data, we use two window sizes, with 20 and 40 observations corresponding to 5 and 10 years. For monthly data, we use 3, 5 and 10 years, corresponding to 36, 60 and 120 monthly observations. We use more than one window size to evaluate the sensitivity of the corresponding forecasts to the window size which is often an arbitrary choice in practice.<sup>4</sup> The largest size of ten years seems reasonable since we have about twenty years available before the forecast period,

Secondly, we also compute forecasts based on the AR(1) and AR(4) models estimated recursively, i.e. with an expanding window of data.

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<sup>3</sup>Bayesian inference allows us to compute APL in addition to RMSE results. RMSEs calculated using OLS, do not differ much from the Bayesian results.

<sup>4</sup>Choosing the window size optimally is discussed in Pesaran and Timmermann (2007). Their analytical results do not apply to AR models. The cross-validation procedure they propose is left for future research.

Finally we use an unobserved component model with stochastic volatility (UC-SV). We follow the formulation of Stock and Watson (2007), who specify a model with only a time-varying trend (no AR dynamics), which takes the form

$$\begin{aligned} y_t &= \mu_t + \sigma_{\epsilon,t}\varepsilon_t, & \mu_t &= \mu_{t-1} + \sigma_{\eta,t}\eta_t, \\ \log \sigma_{\epsilon,t} &= \log \sigma_{\epsilon,t-1} + v_t, & \log \sigma_{\eta,t} &= \log \sigma_{\eta,t-1} + w_t, \end{aligned} \tag{7}$$

where in this case,  $(\varepsilon_t, \eta_t) \sim N(0, I_2)$ ,  $u_t \sim N(0, \gamma_1)$  and  $v_t \sim N(0, \gamma_2)$ . For U.S. inflation, Stock and Watson (2007) set  $\gamma_1 = \gamma_2 = 0.2$ . We estimate these parameters and the priors we use to forecast with this model are

$$\begin{aligned} \mu_0 &\sim N_m(0, 4), & \log \sigma_{\epsilon,0} &\sim N(0, 1), & \log \sigma_{\eta,t} &\sim N(0, 1) \\ B_0^{-1} &\sim \text{Gamma}(1, 0.1), & \gamma^{-1} &\sim \text{Gamma}(1, 0.1). \end{aligned}$$

Forecasting in the above model is similar in spirit with the TVP and KP models. We first need to simulate the future values of the time-varying parameters, and then plug in these simulated values in the first equation of (7).

Table 1 lists the models used in the forecasting evaluations, with a short definition.

### 3 Breaks in US Macroeconomic Series

We apply the PPT and KP models to thirty-nine quarterly and twenty-one monthly series for the USA (listed in Table 2) which are among the most important macroeconomic variables. Twenty-one quarterly series are obtained by aggregation of the corresponding monthly series, The remaining eighteen quarterly series are not available at the monthly frequency. The sample period is 1959, first month (or quarter), till 2011, ninth month (or third quarter). As indicated in the table, we have transformed most series to growth rates or first differences, and in this we are proceeding as in the literature, see e.g. Stock and Watson (1996) and Bernanke, Boivin, and Elias (2005). We use AR(1) and AR(4) models in each regime, hence,  $Z_t$  in (1) contains an intercept and the lags of  $y_t$ .

In Tables 3-5, we report the break dates found in the PPT-AR(1) and AR(4) models (called PPT1 and PPT4 hereafter), and similarly KP-AR(1) and AR(4) models (KP1 and KP4), using the complete sample. The reported break dates are medians of posterior distributions.

We find no break in nine quarterly series (numbered 6, 14, 18, 22, 24, 26, 31, 35, 38) out of thirty-nine both with PPT and KP (irrespective of the lag order), in six other series

with PPT (2, 3, 5, 10, 11, 30), and in two other series (32, 39) with KP; see Tables 3 and 4. Three monthly series (26, 31, 35) out of twenty-one have no break both by PPT and KP, and one more (24) by KP. Three series (22, 24, 38) have breaks when used at the monthly frequency, but no break at the quarterly frequency. More generally, more breaks are obtained with monthly than quarterly series (compare Tables 4 and 5).

No quarterly series has more than three breaks, and few – seven by PPT, three by KP – have three breaks. On the contrary, ten monthly series have at least four breaks by one of the four models (PPT1, PPT4, KP1, KP4). PPT models generate more breaks than KP especially for the monthly series. This is due (only partly) to the occurrence of breaks at close dates in eleven monthly series, a phenomenon observed only in two quarterly series.

To illustrate the parameter estimates of PPT and KP models, Table 6 provides the posterior means of the parameters of the AR(1) equations of each regime for a few series. The table also reports the estimates when no break is allowed on the full sample, and estimates on subsamples, which will be commented in subsection (4.3). These results illustrate that the most sensitive parameter is the variance of the error term. The constant term changes also as a consequence of some level changes in the data of some series. The autoregressive coefficient ( $\phi$ ) is more stable, with some exceptions, illustrated by series 23. For this series (the growth rate of industrial production), using the PPT results, the first regime (ending in 1960Q3) has the highest variability ( $\sigma^2$ ), the lowest persistence and average level (estimated as  $c$  divided by  $1 - \phi$ ). The third regime, starting in 1983Q1, corresponds to the lowest variability, the highest persistence, and an average growth rate between those of the other two regimes. The third regime corresponds to the great moderation period, except that a break is not detected by PPT in 2008. \*\*\* WHAT DOES KP TELL US ABOUT SERIES 23? \*\*\*

We do not report break dates for the GK models, since these models generate much more breaks than PPT and KP. This is mainly a consequence of using an independent Bernoulli prior for the sequence of state variables  $s_t$ , instead of a Markov chain structure.

In summary, there is evidence that macroeconomic series are subject to breaks since about three quarters of our series have at least one break when modeled by structural break models.

## 4 Results of Forecasting Evaluations

For each series listed in Table 2, we carry out a recursive forecasting exercise for the final (approximately) sixty percent of the observations: we first estimate the models with an initial sample consisting of (approximately) forty percent of the data, and we forecast at the horizons  $h$  equal 1 and 4 for quarterly data, and 1 and 12 for monthly data. Then we add one data point, estimate and forecast again, until the end of the data. Thus for quarterly data, we have 83 in-sample observations at the start (1959Q1-1979Q4), and 127 in the forecast period, and for monthly data these numbers are 251 (1959M1-1979M12) and 381.<sup>5</sup> For  $h > 1$ , our forecasts are iterated (see, e.g., Marcellino, Stock, and Watson (2006) for a motivation for use of iterated over direct forecasts).

Our forecast metrics are RMSE and the average of log predictive likelihoods (APL). RMSE is based the predictive median as point forecast. The predictive likelihood is the predictive density evaluated at the observed outcome. This is estimated by a nonparametric kernel smoother using draws from the predictive simulator.

We discuss the results based on the RMSE criterion in subsection 4.1, and in subsection 4.2 the results based on the APL criterion. We are interested in three questions:

**Question 1:** How does the forecasting performance differ between break models and no-break models?

**Question 2:** How does the forecasting performance differ between break models?

**Question 3:** How does the forecasting performance differ between lag orders?

For each question, we shall also comment how the forecasting performance differ between quarterly and monthly series, whenever this is relevant.

### 4.1 RMSE Results

We provide in Table 7 the list of the best model for each quarterly series, together with the relative performance of the best break model with respect to the best no-break model. The same type of information is provided in Table 8 for the monthly series.

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<sup>5</sup>Our forecast evaluation exercise requires us to estimate each model for 60 series; for 39 quarterly series, the recursive forecast evaluation requires that we estimate each model 126 times, and for 21 monthly series, 380 times, for a total of 12,894 estimations per model. For some break models, this takes a lot of time.

For the quarterly series: at horizon one, the break models are the best in 85 percent of all series (8 series for PPT, 3 for KP, 12 for GK, and 10 for TVP). At horizon four, the break models forecast better in 77 percent (3 series for PPT, 5 for KP, and 16 for GK, and 6 for TVP). Hence, as the horizon increases, it appears that the performance of break models decreases slightly, while the KP and GK models increase their share at the expense of PPT and TVP.

For the monthly series: the break models perform best in 67 percent of the series at both horizons, but the share of KP and GK models also increases with the horizon, at the expense of PPT and TVP.

Note that these scores do not take account of the magnitude of the differences of the RMSE between the different models (for this see below).

With the results in Tables 7 and 8, we can answer the three questions about the forecasting performance of the different models.

**Question 1:** We compare the best break model RMSE value to the best no-break model value, see columns ”% diff.” in the tables. For example, a value of -3 (+3) means that the best break (no-break) model has its RMSE three percent smaller (larger) than the RMSE of the best no-break (break) model. Although for a high proportion of the series the differences are negative, they are nevertheless generally small, by what we mean they are less than five percent.<sup>6</sup> Exceptions occur only for quarterly series: at horizon one, series 8 (in favor a no-break model); at horizon 4, series 15, 19, 20, 24, 36, and 39 (all in favor of break models).

Significance tests for the nullity of the mean of the differences<sup>7</sup> are insignificant at the ten percent level for the two forecast horizons at each frequency (see reported *t*-statistics in the last rows of the tables). In brief, there is some weak evidence in our results that break models perform a little better than no-break models.

**Question 2:** The relative differences (in percent) between the RMSE of the different models

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<sup>6</sup>The choice of five percent as the frontier between small and large is of course arbitrary, and not necessarily sensible from an economic perspective. For example, for financial returns, five percent is a lot even at the quarterly frequency. Using an economic criterion to fix a threshold would require to define different criteria for different series and would render the comparison between the series difficult and also arbitrary to some extent.

<sup>7</sup>The test is based on the assumption that the 39 observed values of column 4 of Table 7 (as an example) are random draws of a common distribution with mean  $\mu$ . The tested hypothesis is ” $\mu = 0$ ” (versus  $\mu \neq 0$ ). The test statistic (-0.79), equal to the sample mean (-1.34) divided by the sample standard deviation (1.69) of the 39 values, is asymptotically standard normal under the null hypothesis.

for forecasts at horizons 1 and 4 (quarterly series) or 12 (monthly) are shown in Tables 5-12 of the TA. For example, the value  $-1.93$  of quarterly series 1 for a comparison of PPT12 and KP1 at horizon 1 (see Table 5 of TA) means that PPT12 is performing better than KP1 by almost two percent.

For most series, the differences are small, but there are a few cases where they are large. For example, at horizon 1, for quarterly series 15, 30, 35 and 38, in the comparisons involving GK1B and GK4B, the ratios indicate that GK1B and GK4B is forecasting far away from the realizations; for series 21, there is also a number of large differences (around 50 percent), and the culprits are TVP1, TVP4, and KP4. For monthly series, more series have large differences, e.g. at horizon 1, series 20, 21, 25, 32, 35, 36 in comparisons involving GK1B and GK4B; series 21 in comparisons involving TVP1 and TVP4; series 36, 38, 39 in comparisons involving KP1.

Means and *t*-tests of significance of the means of the differences for each model comparison (like for Question 1) are given at the bottom of each column of the tables. In computing these statistics, we have eliminated the large differences (as shown in the tables)

Judging by the means (at the bottom of the tables), for quarterly series, at horizons 1 (Table 5 of TA) and 4 (Table 7 of TA), KP1 performs better on average than the other models (PPT12, GK1B, GK1P, TVP1); PPT12 performs better than GK1P, GK1B, TVP1; GK1P dominates GK1B. TVP1 dominates GK1B and is dominated by GK1P at horizon 1, while at horizon 4, TVP1 surpasses GK1P and is surpassed by GK1B. For models using 4 lags, on average, at horizon 1 (Table 6 of TA), PPT41 dominates the other models (KP4, GK4B, GK4P, TVP4); KP4 dominates TVP4, GK4B and GK4P; TVP4 performs better than both GK models and GK4P surpasses GK4B. At horizon 4 (Table 8 of TA), both GK models dominate TVP4, GK4P performs better than GK4B, PPT41 and KP4 perform quasi-equally, and both dominate the other models. However, the *t*-statistics are all insignificant at 10 percent in Tables 5-8 of the TA; this remains true if we do not trim the extreme values.

For monthly series, at horizon 1 (Table 9 of TA), PPT12 performs better on average than KP1, GK1B, GK1P, TVP1; TVP1 dominates KP1, GK1P, GK1B; GK1P dominates KP1 and GK1B, and GK1B surpasses KP1. At horizon 12 (Table 11 of TA), the results differ slightly: KP1 and GK1B dominate GK1P. For AR(4) models, at horizon 1 (Table 10 of TA), KP4 dominate the other models (PPT41, GK4B, GK4P, TVP4); PPT41 surpasses GK4B, GK4P,



TVP4; TVP4 dominates both GK models, and GK4P surpasses GK4B. At horizon 12 (Table 12), TVP4 dominates the other models (PPT41, KP4, GK4B, GK4P); PPT41 surpasses KP4, GK4P and GK4B; KP4 dominates both GK models, and GK4P surpasses GK4B. Again, no  $t$ -statistic (with or without trimming) is significant at 10 percent in Tables 9-12 of the TA.

In summary, on average (across series), the results do not indicate that a subset of models performs better than the other, on the basis of the  $t$ -tests. However, judging by the average differences only, the KP, PPT and TVP models perform better than the GK models. This result holds after elimination of the large individual differences and thus are not due to the trimming we have applied. Combined with the fact that the models that provoke the large differences in some series is in almost all cases the GKxB model, we conclude that the KP, PPT and TVP models should be considered as the most useful class of break models, when evaluating forecasts by the RMSE criterion.

**Question 3:** The relative differences (in percent) between the RMSE of the different models for forecasts at all horizons are reported in Table 13-16 in the TA.

For break models, no clear indication emerges in favor of one of the lag orders: the computed mean differences vary in sign and all  $t$ -statistics are insignificant at 10 percent. For no-break rolling window models, the computed mean differences are negative at all horizons (with two exceptions for RO110Y/RO410Y, in Tables 15 and 16 of the TA), suggesting that models with one lag tend to perform better. However, this evidence is weak, since the  $t$ -statistics reveal that the mean differences are not significant at the 10 percent level, both for quarterly and monthly series, and for all horizons.

## 4.2 APL Results

We list the best model for each quarterly and monthly series, respectively in Tables 9 and 10, together with the relative performance of the best break model with respect to the best no-break model.

For the quarterly series, at both horizons the no-break models perform better than the break models in roughly 80 percent of the series. The RO models have the highest share: 54 percent (21 series) at horizon 1 and 36 percent (14 series) at horizon 4. They are followed by the REC models (21 and 26 percent). Among the RO models, RO120 (1 lag, 20 observations per window) appears most often (12 series at horizon 1, and 10 at horizon 4). Given the

dominance of RO120, models with 1 lag dominate models with 4 lags, but less so at horizon one than four.

For the monthly series, the domination of no-break models is very strong (95 percent at horizon 1, 100 at horizon 12, with a strong dominance of rolling window (RO) models at both horizons. At horizon 1, the RO models with 4 lags dominate those with one lag (12 against 2), while the reverse happens at horizon 12 (1 against 14). There is no clear pattern for the effect of the window size.

These scores do not take account of the magnitude of the differences of the APL between the different models (for this see question 1 below) but suggest that RO models are dominating the other models by far.

With the results in Tables 9 and 10, we can answer the three questions about the forecasting performance of the different models.

**Question 1:** We compare the best break model APL value to the best no-break model value, see columns "% diff." in the tables. For example, a value of +4 (-4) means that the best break (no-break) model has its APL four percent larger than the APL of the best no-break (break) model.

For a high proportion of the series the differences are negative, as our discussion just above has illustrated. They are larger than for the RMSE results: the average difference for quarterly data at horizon 1 is -3.5, and at horizon 4, it is -6.5. For monthly data, the mean differences are larger (-5.9 and -16.3) and also increase with the horizon. Nevertheless, the *t*-statistics are insignificant at 10 percent. In brief, there is weak evidence in our results that the no-break models (especially RO) perform better than break models. Exceptions occur for the quarterly series numbered 6, 18, 27 and 33 at both horizons, and for a few other series at one horizon (series 1, 14, 16, 19, 20, 29). For monthly series, there is one exception only at horizon 1 (series 34).

**Question 2:** The relative differences (in percent) between the APL of the break models for forecasts at horizon one are shown in Tables 21-28 of the TA. For example, the value 28 for the quarterly series 1 (see Table 21 of TA) for the comparison GK1P/GK1B means that the APL of GK1P exceeds the APL of GK1B by 28 percent. The differences vary a lot, and there are a few cases where they are very large. The large differences occur mainly for series 21, 24-26, 30, 35 (plus 32 and 39 with monthly data) and in comparisons involving the TVP

and GK models. Thus we have trimmed the statistics (as shown in the Tables) to avoid the influence of extreme values of the differences.

Judging by the means (at the bottom of the tables), for quarterly series, at horizon 1, KP1 performs better on average than the other models (PPT12, GK1B, GK1P, TVP1); PPT12 performs better than GK1P, GK1B, TVP1; GK1P dominates GK1B, and TVP1 dominates both GK models. For models using 4 lags, on average, KP4 dominates the other models (PPT41, GK4B, GK4P, TVP4); PPT14 dominates TVP4, G4KB and GK4P; TVP4 performs better than both GK models and GK4P surpasses GK4B. At horizon 4, the results are of the same kind. However, the  $t$ -statistics are insignificant at 10 percent in Tables 21-24 of the TA, except in the comparison PPT41/KP4 at horizon 4 (see Table 24 of the TA).

For monthly series, at horizon 1, PPT12 performs better on average than KP1, GK1B, GK1P, TVP1; KP1 dominates on average GK1P, GK1B, TVP1; GK1P dominates GK1B, and TVP1 surpasses both GK models. For AR(4) models, the rankings are similar, except that GK4B dominates GK4P. At horizon 12, for AR(1) models, the results differ from those for horizon 1 only by the fact that KP1 dominates PPT12. For AR(4) models, KP4 dominates the other models, PPT41 dominates TVP4 and both GK4 models, GK4B surpasses GK4P and TVP4, and TVP4 performs better than GK4P. Again, no  $t$ -statistic (after trimming) is significant at 10 percent in Tables 25-28 of the TA, but if trimming is not applied, all statistics remain insignificant.

In brief, on average (across series), the results do not indicate that a subset of models performs better than the other, on the basis of the  $t$ -tests. However, judging by the average differences only, the KP and PPT models perform better than the GK and TVP models. This result holds after elimination of the large individual differences and thus are not due to the trimming we have applied. Combined with the fact that the models that provoke the large differences in some series are in almost all cases the GK and TVP models, we conclude that the KP and PPT models should be considered as the most useful class of break models, when evaluating forecasts by the APL criterion.

**Question 3:** The relative differences (in percent) between the APL of the different models for forecasts at horizons 1 and 4 are reported in Tables 29-32 of the TA.

For break models, the computed mean differences do not reveal a systematic dominance (on average) of one lag order, and the  $t$ -statistics are all insignificant at the 10 percent level.

The mean differences are in most cases larger at the higher horizons (4 for quarterly series, 12 for monthly).

For no-break models models, at the larger horizons, all the mean differences are positive, thus in favor of models with 1 lag, but only one is significant (see RO120/RO420 in Tables 30 of the TA). At horizon 1, no systematic pattern emerges and  $t$ -statistics are all insignificant at 10 percent.

### 4.3 Discussion of Previous Results

For the APL criterion, we find that the no-break models, especially rolling AR models, perform better on average than the break models. For the RMSE criterion, we find some weak evidence in favor of break models. Why this difference?

The APL criterion takes into account the whole shape of the predictive density. This is not Gaussian despite the assumption of normality (conditional on the parameters), because it is integrated with respect to a posterior distribution that is not symmetric. However our predictive densities are very moderately skewed, especially for forecasts at short horizons. Therefore, we can summarize the shape of our predictive by their standard deviation. The RMSE results indicate that in terms of the location of the point forecasts in the support of the predictive densities, the two kinds of models (break/no-break) are roughly equivalent on average (of course, individual exceptions occur). Thus the differences in the APL results must be (at least partly) due to differences in the standard deviations of the predictive densities. In the results, we find some evidence that supports our explanation. \*\*\* PROVIDE EXAMPLE(S OF THIS FOR SOME SERIES AND EXPLAIN, OR EXPLAIN LIKE IN PREVIOUS VERSION (this requires to put more if not all series in Table 6) \*\*\*

## 5 Sensitivity Analyses

We perform two sensitivity checks. The first is with respect to the forecast period: we focus on the data starting in 2007, which corresponds more or less to the beginning of the global financial crisis, until the end of the sample (i.e. 19 observations for quarterly series, and 57 monthly observations). The second check concerns the influence of the prior used in the break models.

## 5.1 Forecast performance since 2007

These results were obtained with the same prior as in the previous section. For the RMSE criterion, break models perform better than no-break models in 74 percent of quarterly series at horizon 1 and 59 at horizon 4. These values are a little lower than for the corresponding results (85 and 77) reported in the previous section. The corresponding proportions are 62 (horizon 1) and 86 (horizon 12) for monthly series (versus 67 in the previous section at both horizons). The corresponding mean differences are negative but small, and the  $t$ -statistics (reported in Table 11) are insignificant, as in the previous section.

For the APL criterion, we find that no-break models perform better than break models in 63 percent of series at both horizons for quarterly series (instead of 80 in the previous section), and in 95 percent for monthly series at both horizons, much like in the previous section. The mean differences are insignificant, though for monthly series the mean differences are close to minus 10 percent and one of them is close to being significant at 10 percent.

In summary, the results for the post-2006 forecast sample are broadly similar to those for the post-1979 forecast sample.

## 5.2 Impact of the prior for break models

In Bayesian inference, it is good practice to assess the sensitivity of the results with respect to the informative content of the prior. Thus we have computed all the results with different sets of prior hyperparameters. One set implies a more informative prior (PRIOR M), and the other a less informative prior (PRIOR L) than our intermediate prior (PRIOR I) used for getting all the results reported in the previous (sub)sections. The parameter values of PRIOR I are given at the end of subsection 2.2. Due to space limitations, we report briefly the results for AR(1) PPT and KP models (PPT12 and KP1).

All our priors (M, I, L) imply that the unconditional prior expectations are equal to zero for the regression coefficients of the AR(1) or AR(4) equations in each regime since  $E(\beta_j) = E[E(\beta_j|\beta_0)] = E(\beta_0)$  and the latter is set to zero. They imply non-existing second moments for the regression coefficients because  $Var(\beta_j) = Var[E(\beta_j|\beta_0)] + E[Var(\beta_j|\beta_0)] = Var(\beta_0) + E(B_0)$  and  $E(B_0)$  is not finite due to setting the degrees of freedom of the Wishart prior to  $m + 1$ , with  $m = 2$  for AR(1) and 5 for AR(4). However  $Var(\beta_0)$  is set to  $\underline{V}_\beta = cI_m$  with  $c = 1$  in PRIOR I and by changing the value of  $c$ , we can change the tightness of the

prior on the regression coefficients.

In PRIOR L, we set  $c = 100$ , implying standard deviations equal to 10 for  $\beta_0$ , that is ten times larger than the corresponding value in PRIOR I (which has  $c = 1$ ). We are also less informative on error variances of AR equations by setting  $\underline{\rho} = 0.01$  and  $\underline{d} = 0.01$  (instead of 0.1 for both in PRIOR I) in the PPT model. In the KP model, we set  $\underline{V}_\omega = 100$  (instead of 1) and  $\underline{\kappa}_1 = \underline{\kappa}_2 = 0.01$  (instead of 0.5).

In PRIOR M, we set  $c = 0.01I_m$ , implying a more precise prior (with standard deviations of 0.1) than in PRIOR I. For the other parameters of the prior, the values are the same as in PRIOR I.

Computed by simulation, the highest prior density interval of ninety percent level for each regression coefficient is equal to  $(-17, +17)$  for PRIOR L,  $(-3.9, +3.9)$  for PRIOR I, and  $(-2.6, +2.6)$  for PRIOR M. Notice that if  $c$  is set to a smaller value than 0.01, the last interval does not shrink due to the  $E(B_0)$  term that is not finite. Compared to the precisions typically implied by the type of data and sample size we use, all these priors are little informative, but PRIOR L is substantially less tight than the other two, while PRIOR M is slightly more concentrated than PRIOR I. In Table 12, we summarize the difference between the results with the three priors, for both criteria and for AR(1) specifications.

For each series, horizon, and forecasting model (PPT12 and KP1), we compute the percentage difference in each criterion value (RMSE and APL) of PRIOR M and PRIOR L relative to PRIOR I. Then we take the average of these values over all series and we test the significance of the mean. For example, the *positive* mean of 0.51 for the RMSE criterion for PPT12 at horizon one indicates that on average the performance is better with PRIOR I than with PRIOR L, by half of a percent. The corresponding t-statistic (0.32) indicates that this is not significant even at the ten percent level. For the APL criterion, a *negative* mean such as  $-3.58$  for KP1 at horizon one indicates a better performance with PRIOR I than PRIOR L.

For the RMSE criterion, the differences of performance are small on average, and statistically insignificant: the largest mean difference is at horizon 4 for PPT12 (2.21 percent in favor of PRIOR I relative to M). Except in one case, all mean differences are in favor of prior I.

For the APL criterion, all mean differences are in favor of prior I. The mean differences are

small for PPT12 at both horizons in both comparisons, the largest (-1.98) being significant at 10%. For KP1, the mean differences are larger (over 3.5%), the largest one (-13.2%) being significant at 5%.

## 6 Conclusions

In this paper, we have compared various forecasting procedures which allow for structural breaks in a set of sixty US macroeconomic time series, quarterly and monthly. Our set of forecasting procedures is divided into two groups: ones which formally model the break process (KP, PPT, GK, and TVP) and those which do not (rolling and recursive window based forecasts, and UC-SV).

Our empirical results do not tell one single consistent story, but rather a variety of stories. Most importantly, we have added to the literature establishing the widespread existence of structural breaks in major macroeconomic time series. Our results also show the importance of using a forecasting method which allows for parameter change of some sort. However, perhaps unsurprisingly, we have not established that there is one single forecasting method that always is to be preferred. Each of our methods performs well in some cases, but not as well in others.

In terms of RMSE, we find weak evidence in favor of a better performance of break models, with some advantage to KP and PPT. We find no evidence that these break models are harmful for individual series, so that we recommend to consider them as potentially useful forecasting models. They might also add value if forecast combination were considered, an issue that we leave for further research.

In terms of predictive likelihoods, it is often the case that rolling (fixed window) forecasts are better than approaches which formally model the break process. In Section 5.3, we have offered an explanation for this. However, it is worthwhile to expand on this finding. In an effort to produce automatic forecasting procedures, suitable for repeated use with many data sets, this paper has used very simple implementations of PPT, KP, and GK break models. In particular, for each series, we have used the same models (i.e. AR models), with the same prior (a relatively noninformative one) and the break process has been modeled in a very simple way. It is possible that these break models are not well-designed for use in such a black box fashion. For instance, we have imposed that breaks in AR coefficients and error

variance occur at the same time. But in some of the series, it looks to be the case that having separate break processes for the error variance and regression coefficients would be useful (i.e. ensuring more parsimony by allowing breaks in the conditional variance but not in the conditional mean). Also, it is likely that calibrating priors on a case-by-case basis (or using more sophisticated hierarchical priors) could improve forecast performance. And, the hierarchical structures of the break models will tend to be of most use in more complicated forecasting models (e.g. involving many predictors or with VARs) where rolling or recursive forecasting methods can perform poorly (see, e.g., Korobilis and Koop (2010)) rather than simple univariate AR setups.

In sum, in this paper we have established the importance of structural breaks for forecasting in many macroeconomic time series. However, we also recommend the careful development of appropriate structural break models on a case-by-case basis as opposed to use of an automatic procedure.

A potentially useful extension of our research will be to base the forecasts on models using other regressor variables than lags, and on multivariate models, noticing that Pettenuzzo and Timmermann (2011) have extended the PPT framework to such models.

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Table 1: Models used in the forecasting evaluations

Name	Description
<u>Break models (all series)</u>	
PPT12	PPT with geometric prior, AR(1), 2 breaks allowed in forecast period
PPT41	PPT with geometric prior, AR(4), 1 break allowed in forecast period
KP1	KP with geometric prior, AR(1)
KP4	KP with geometric prior, AR(4)
GK1B	Mixture innovation model, geometric prior, AR(1)
GK4B	Mixture innovation model, geometric prior, AR(4)
GK1P	Mixture innovation model, Poisson prior, AR(1)
GK4P	Mixture innovation model, Poisson prior, AR(4)
TVP1	Time-Varying Parameter AR(1) model
TVP4	Time-Varying Parameter AR(4) model
<u>No-break models (quarterly series)</u>	
RO120	AR(1) estimated with rolling window of 5 years (20 observations)
RO140	AR(1) estimated with rolling window of 10 years (40 observations)
RO420	AR(4) estimated with rolling window of 5 years
RO440	AR(4) estimated with rolling window of 10 years
REC1	AR(1) estimated on expanding window
REC4	AR(4) estimated on expanding window
UC-SV	Unobserved component model with stochastic volatility
<u>No-break models (monthly series)</u>	
RO13Y	AR(1) estimated with rolling window of 3 years (36 observations)
RO15Y	AR(1) estimated with rolling window of 5 years (60 observations)
RO110Y	AR(1) estimated with rolling window of 10 years (120 observations)
RO43Y	AR(4) estimated with rolling window of 3 years
RO45Y	AR(4) estimated with rolling window of 5 years
RO410Y	AR(4) estimated with rolling window of 10 years
REC1	AR(1) estimated on expanding window
REC4	AR(4) estimated on expanding window
UC-SV	Unobserved component model with stochastic volatility

Table 2: Variables used in forecast evaluation

	Acronym	T	F	Definition
1	GDP96	5	Q	Real Gross Domestic Product
2	PINCOME	5	Q	Personal Income
3	PCECC96	5	Q	Real Personal Consumption Expenditures
4	PCECTPI	5	Q	Personal Consumption Expenditures Chain-type Price Index
5	GPDI96	5	Q	Real Gross Private Domestic Investment
6	OPHPBS	5	Q	Business Sector: Output Per Hour of All Persons
7	IMPGSC96	5	Q	Real Imports of Goods & Services
8	EXPGSC96	5	Q	Real Exports of Goods & Services
9	CBIC96	1	Q	Real Change in Private Inventories
10	GCEC96	5	Q	Real Government Consumption Exp. & Gross Inv.
11	WASCUR	5	Q	Compensation of Employees: Wages & Salary Accruals
12	DIVIDEND	5	Q	Net Corporate Dividends
13	PSAVE	5	Q	Personal Saving
14	DPIC96	5	Q	Real Disposable Personal Income
15	GDPDEF	5	Q	Gross Domestic Product: Implicit Price Deflator
16	ULCNFB	5	Q	Nonfarm Business Sector: Unit Labor Cost
17	PRFI	5	Q	Private Residential Fixed Investment
18	GSAVE	5	Q	Gross saving
19	CPIAUCSL	5	Q,M	Consumer Price Index: All Items
20	FEDFUNDS	1	Q,M	Effective Federal Funds Rate
21	BOGNONBR	2	Q,M	Non-Borrowed Reserves of Depository Institutions
22	M2	5	Q,M	M2 Money Stock
23	INDPRO	5	Q,M	Industrial Production Index
24	UTL11	1	Q,M	Capacity Utilization: Manufacturing
25	UNRATE	1	Q,M	Civilian Unemployment Rate
26	HOUST	4	Q,M	Housing Starts: New Privately Owned Housing Units Started
27	PPIFCG	5	Q,M	Producer Price Index: All Commodities
28	AHEMAN	5	Q,M	Average Hourly Earnings: Manufacturing
29	M1	5	Q,M	M1 Money Stock
30	PMCP	1	Q,M	NAPM Commodity Prices Index
31	SP500	5	Q,M	S&P 500 Index
32	GS10	1	Q,M	10-Year Treasury Constant Maturity Rate
33	EXUSUK	5	Q,M	U.S. / U.K Foreign Exchange Rate
34	PAYEMS	5	Q,M	Total Nonfarm Payrolls: All Employees
35	NAPMNOI	1	Q,M	ISM Manufacturing: New Orders Index
36	TB3MS	1	Q,M	3-Month Treasury Bill: Secondary Market Rate
37	BUSLOANS	5	Q,M	Commercial and Industrial Loans at All Commercial Banks
38	TOTALSL	5	Q,M	Total Consumer Credit Outstanding
39	AAA	1	Q,M	Moody's Seasoned Aaa Corporate Bond Yield

T (transformation applied to original series): 1 = none, 2 = first difference, 4 = log, 5 = first difference of logged variable. F (frequency): Q = quarterly, M = monthly. Sample period (after data transformation): 1959M1-2011M9 (633 observations) or 1959Q1-2011Q3 (211 observations)  
Data source: St. Louis FRED database.

Table 3: Break dates based on full sample (quarterly data)

	$q$	PPT-AR( $q$ )			KP-AR( $q$ )		
1	GDPC96	1	1983Q1			1983Q4	
		$\frac{4}{4}$	1982Q2			-	
2	PINCOME	1	-			-	
		$\frac{4}{4}$	-			2008Q3	
3	PCECC96	1	-			1993Q3	
		$\frac{4}{4}$	-			-	
4	PCECTPI	1	2006Q2			2008Q3	2010Q3
		$\frac{4}{4}$	2007Q3			2008Q4	2010Q3
5	GPDIC96	1	-			1984Q3	2008Q3
		$\frac{4}{4}$	-			1983Q4	
6	OPHPBS	1	-			-	
		$\frac{4}{4}$	-			-	
7	IMPGSC96	1	1986Q1			1986Q3	2008Q3
		$\frac{4}{4}$	1984Q4	2007Q2		1986Q1	2008Q3
8	EXPGSC96	1	1978Q3			1979Q1	
		$\frac{4}{4}$	-			1979Q1	
9	CBIC96	1	1979Q4			1977Q3	2009Q1
		$\frac{4}{4}$	1977Q3			1980Q3	
10	GCEC96	1	-			1973Q4	
		$\frac{4}{4}$	-			-	
11	WASCUR	1	-			2000Q1	
		$\frac{4}{4}$	-			-	
12	DIVIDEND	1	2004Q2	2005Q1		1973Q2	2004Q4
		$\frac{4}{4}$	1990Q4	2003Q3	2004Q2	2004Q4	
13	PSAVE	1	1998Q1			1998Q4	
		$\frac{4}{4}$	1996Q3			1998Q4	
14	DPIC96	1	-			-	
		$\frac{4}{4}$	-			-	
15	GDPDEF	1	1965Q4	1982Q2		1985Q2	
		$\frac{4}{4}$	1980Q1			1981Q2	
16	ULCNFB	1	1983Q2	1999Q1		1983Q4	1999Q4
		$\frac{4}{4}$	-			-	
17	PRFI	1	1983Q1	2006Q1		1983Q3	2006Q2
		$\frac{4}{4}$	1982Q2	2006Q1		1983Q2	2007Q1
18	GSAVE	1	-			-	
		$\frac{4}{4}$	-			-	

Break dates are defined as the first observation of the new regime, using the median of the posterior of the states.

Table 4: Break dates based on full sample (quarterly data)

	$q$	PPT-AR( $q$ )			KP-AR( $q$ )			
19	CPIAUCSL	1	1965Q4	1999Q3	2002Q3	1965Q3	1991Q1	2008Q4
		$\frac{4}{4}$	<i>2007Q3</i>			<i>2008Q4</i>		
20	FEDFUNDS	1	1967Q4	1984Q3		1968Q1	1985Q2	2008Q4
		$\frac{4}{4}$	<i>1966Q4</i>	<i>1978Q3</i>	<i>1983Q3</i>	<i>1985Q2</i>		
21	BOGNONBR	1	1970Q2	1983Q4	2007Q2	2007Q4		
		$\frac{4}{4}$	<i>1971Q2</i>	<i>1983Q1</i>	<i>2006Q3</i>	<i>2008Q1</i>		
22	M2	1	-			-		
		$\frac{4}{4}$	-			-		
23	INDPRO	1	1960Q2	1983Q1		1982Q1		
		$\frac{4}{4}$	<i>1960Q2</i>	<i>1981Q1</i>		-		
24	UTL11	1	-			-		
		$\frac{4}{4}$	-			-		
25	UNRATE	1	1983Q3	2007Q4		2008Q4		
		$\frac{4}{4}$	-			-		
26	HOUST	1	-			-		
		$\frac{4}{4}$	-			-		
27	PPIFCG	1	2006Q2			1972Q3	2007Q3	
		$\frac{4}{4}$	<i>2007Q1</i>			<i>2008Q3</i>	<i>2010Q3</i>	
28	AHEMAN	1	1967Q2	1981Q4		1982Q4		
		$\frac{4}{4}$	<i>1974Q1</i>	<i>1980Q3</i>		<i>1981Q4</i>		
29	M1	1	1978Q4			2008Q3		
		$\frac{4}{4}$	<i>1978Q1</i>			<i>2008Q3</i>		
30	PMCP	1	-			2006Q4		
		$\frac{4}{4}$	-			-		
31	SP500	1	-			-		
		$\frac{4}{4}$	-			-		
32	GS10	1	1979Q2	1984Q2		-		
		$\frac{4}{4}$	<i>1978Q3</i>	<i>1983Q2</i>		-		
33	EXUSUK	1	1967Q2			1967Q4		
		$\frac{4}{4}$	<i>1966Q3</i>	<i>1967Q2</i>	<i>1970Q2</i>	-		
34	PAYEMS	1	1983Q2			1984Q1	2008Q2	
		$\frac{4}{4}$	<i>1982Q1</i>			-		
35	NAPMNOI	1	-			-		
		$\frac{4}{4}$	-			-		
36	TB3MS	1	1979Q2	1982Q3		1979Q3	1983Q1	
		$\frac{4}{4}$	<i>1965Q1</i>	<i>1978Q2</i>	<i>1983Q4</i>	-		
37	BUSLOANS	1	-			2008Q4		
		$\frac{4}{4}$	<i>2007Q4</i>			<i>2009Q1</i>		
38	TOTALSL	1	-			-		
		$\frac{4}{4}$	-			-		
39	AAA	1	1965Q2	1979Q2	1984Q2	-		
		$\frac{4}{4}$	<i>1978Q3</i>	<i>1983Q2</i>		-		

See note of Table 3.

Table 5: Break dates based on full sample (monthly data)

	$q$	PPT-AR( $q$ )				KP-AR( $q$ )				
19	CPIAUCSL	1	1965M10	1973M4	1973M8	1982M5	1965M9	2005M6		
	1	1990M9	1996M8	1999M2	2005M5	2004M12				
	4	1965M4	1973M1	1973M6	1990M7	2004M12				
	4	1998M11								
20	FEDFUNDS	1	1962M5	1966M10	1974M6	1975M2	1985M1	2008M10		
	1	1979M8	1982M7	1989M3						
	4	1962M2	1996M7	1979M5	1982M5					
	4	1987M10								
21	BOGNONBR	1	1970M1	1983M8	2001M7	2007M10	2007M12	2008M9	2009M5	
	4	1959M5	1969M10	1983M8	2001M4	2007M12				
	4	2001M8	2007M7							
	4	2000M1								
22	M2	1	2000M1							
	4	1969M8	1982M8	1982M11	1999M10	1970M2	2000M5	2011M7	2011M6	
	4	2001M1								
	4	1960M1	1984M1	2008M6	2009M4					
23	INDPRO	1	1960M1	1984M1	2008M6	2009M4				
	4	1959M11	1983M9	2008M1						
24	UTL11	1	1960M3	1984M1						
	4	1959M11	1982M10							
25	UNRATE	1	-				1986M3	2008M5		
	4	-								
26	HOUST	1	-							
	4	-								
27	PPIFCG	1	1972M10	1975M1	1981M6	2000M11	1972M10	1975M2	2000M4	
	4	1972M7	1974M8	1982M8	2005M3	1972M7	2005M8			
28	AHEMAN	1	1968M7	1981M12			1982M5			
	4	1959M4	1960M3	1982M2						
29	M1	1	1965M1	1979M2	1988M5	2001M7	1965M4	1979M8	2001M8	2008M7
	1	2001M10	2008M5							
	4	1979M7	1981M10	2001M3						
	4	2004M12	2004M9							
30	PMCP	1	2004M12				2005M3			
	4	2004M9								
31	SP500	1	-							
	4	-								
	4	-								
	4	-								
32	GS10	1	1965M9	1979M5	1979M8	1982M8	1966M4	1979M8		
	1	1982M11	1988M4							
	4	1965M6	1979M4	1982M4	1982M7					
	4	1967M9	1967M12	1971M6						
33	EXUSUK	1	1967M9	1967M12	1971M6					
	4	1967M5	1967M8	1971M3						
34	PAYEMS	1	1960M4	1983M6	1983M10					
	4	1960M1	1983M7							
35	NAPMNOI	1	-							
	4	-								
36	TB3MS	1	1960M6	1966M4	1979M7	1982M8	1969M3	1979M4		
	4	1960M2	1966M1	1979M4	1982M4	1966M9	1973M8			
	4	1982M6	1985M4							
	4	2008M8	2008M10							
37	BUSLOANS	1	2008M8	2008M10						
	4	2008M5	2008M9							
38	TOTALSL	1	2002M2	2008M3						
	4	2010M9								
39	AAA	1	1959M12	1963M1	1965M10	1979M7	2002M4	2008M8		
	1	1982M6	1982M10	1988M4						
	4	1965M9	1979M4	1982M12	2002M3					

See note of Table 3.

Table 6: Posterior means of AR(1) models

S	R	PPT-AR(1)			KP-AR(1)			AR(1) full sample			AR(1) last 40 data			AR(1) last 20 data		
		<i>c</i>	$\phi$	$\sigma^2$	<i>c</i>	$\phi$	$\sigma^2$	<i>c</i>	$\phi$	$\sigma^2$	<i>c</i>	$\phi$	$\sigma^2$	<i>c</i>	$\phi$	$\sigma^2$
12	1	0.25	0.51	0.20	0.62	0.28	1.10	0.36	0.28	0.58	0.40	0.19	2.40	0.02	0.65	1.23
	2	0.22	0.38	24.32	0.38	0.45	0.29	-	-	-	<i>0.33</i>	<i>0.47</i>	<i>0.21</i>	<i>0.60</i>	<i>0.30</i>	<i>0.18</i>
	3	0.21	0.57	1.06	0.20	0.10	0.45	-	-	-	-	-	-	-	-	-
23	1	0.03	0.40	1.38	0.14	0.87	0.10	0.08	0.47	0.14	0.01	0.75	0.08	-0.02	0.80	0.13
	2	0.10	0.52	0.17	0.24	0.35	0.04	-	-	-	<i>0.10</i>	<i>0.51</i>	<i>0.21</i>	<i>0.32</i>	<i>0.06</i>	<i>0.11</i>
	3	0.04	0.70	0.05	0.20	0.10	0.45	-	-	-	-	-	-	-	-	-
25	1	0.03	0.99	0.01	0.65	0.26	0.51	0.03	0.98	0.007	0.03	0.99	0.01	0.13	0.96	0.02
	2	0.07	0.94	0.003	0.46	0.42	0.22	-	-	-	<i>0.15</i>	<i>0.91</i>	<i>0.01</i>	<i>0.17</i>	<i>0.88</i>	<i>0.003</i>
	3	0.30	0.89	0.02	0.20	0.10	0.45	-	-	-	-	-	-	-	-	-
32	1	0.02	0.99	0.01	0.13	0.87	0.10	0.02	0.98	0.01	0.15	0.84	0.01	0.17	0.79	0.01
	2	0.19	0.94	0.06	-0.09	0.01	0.64	-	-	-	<i>-0.26</i>	<i>1.15</i>	<i>0.01</i>	<i>-0.71</i>	<i>1.37</i>	<i>0.01</i>
	3	0.05	0.95	0.01	0.20	0.10	0.45	-	-	-	-	-	-	-	-	-
39	1	0.14	0.88	0.001	0.13	0.87	0.10	0.03	0.98	0.009	0.28	0.79	0.004	0.41	0.68	0.004
	2	0.11	0.95	0.004	-0.09	0.01	0.64	-	-	-	<i>-0.36</i>	<i>1.19</i>	<i>0.01</i>	<i>-1.03</i>	<i>1.49</i>	<i>0.01</i>
	3	0.22	0.94	0.04	0.20	0.10	0.45	-	-	-	-	-	-	-	-	-
	4	0.07	0.95	0.006	0.20	0.10	0.45	-	-	-	-	-	-	-	-	-

S = series number (see Table 2); R = regime number. Each AR(1) is written  $y_t = c + \phi y_{t-1} + \sigma \epsilon_t$ . Two estimations are reported in the block "AR(1) last 40 data": on the first row, the results are for the last 40 points of the full sample, on the second row (in italics), they are for the last 40 points ending in 1979Q4 (i.e. at 60 percent of the full sample). Similar for "AR(1) last 20 data".



Table 7: RMSE relative performance of best forecasting models on last sixty percent of sample (quarterly data)

		$h = 1$		$h = 4$	
		best	% diff.	best	% diff.
1	GDPC96	PPT12	-1.06	GK4B	-0.573
2	PINCOME	GK1B	-2.06	UC-SV	3.58
3	PCECC96	PPT41	-1.54	PPT41	-1.08
4	PCECTPI	TVP4	-2.51	TVP1	-2.47
5	GPDIC96	KP1	-0.975	GK4P	-1.39
6	OPHPBS	PPT41	-0.545	KP1	-0.351
7	IMPGSC96	KP1	-0.94	REC1	0.188
8	EXPGSC96	ROW140	5.04	GK1P	-0.851
9	CBIC96	REC1	0.406	GK1P	-1.61
10	GCEC96	GK4B	-0.53	GK4B	-0.725
11	WASCUR	GK4B	-2.63	GK1B	-0.62
12	DIVIDEND	GK1P	-1.91	REC1	0.768
13	PSAVE	GK4P	-2.8	UC-SV	0.323
14	DPIC96	GK4P	-0.102	GK4B	-0.259
15	GDPDEF	TVP4	-2.13	KP1	-8.09
16	ULCNFB	GK4P	-4.48	GK4P	-3
17	PRFI	KP1	-1.64	PPT12	-2.95
18	GSAVE	GK4P	-0.865	GK1P	-0.12
19	CPIAUCSL	UC-SV	1.38	TVP1	-6.87
20	FEDFUNDS	PPT12	-0.745	KP1	-5.79
21	BOGNONBR	PPT12	-3.29	UC-SV	2.24
22	M2SL	UC-SV	0.624	GK4P	-0.313
23	INDPRO	PPT41	-1.49	GK4B	-2.5
24	UTL11	TVP4	-3.77	TVP4	-6.58
25	UNRATE	PPT41	-0.969	REC4	0.242
26	HOUST	TVP1	-1.75	TVP1	-1.21
27	PPIFCG	GK1B	-2.17	GK1B	-3.77
28	AHEMAN	GK4P	-3.81	GK4B	-7.75
29	M1SL	REC1	0.437	ROW140	1.65
30	PMCP	TVP4	-1.45	REC4	0.236
31	SP500	REC1	0.21	KP1	-0.0196
32	GS10	TVP1	-3.11	GK4B	-4.24
33	EXUSUK	GK4B	-0.584	GK1P	-0.218
34	PAYEMS	PPT41	-1.74	GK1P	-0.674
35	NAPMNOI	TVP4	-1.32	PPT41	-0.289
36	TB3MS	TVP4	-3.22	KP1	-5
37	BUSLOANS	TVP1	-0.136	TVP1	-0.347
38	TOTALSL	GK1P	-1.33	TVP1	-1.88
39	AAA	TVP1	-2.66	GK4B	-11.4
		Mean	-1.34	Mean	-1.89
		t-Ratio	-0.79	t-Ratio	-0.61

See Table 1 for model definitions. The "%diff" are computed as [(smallest RMSE across the break models/smallest RMSE across the no-break models)-1]x100. Results computed from Tables 1 and 2 of the TA.

Table 8: RMSE relative performance of best forecasting models on last sixty percent of sample (monthly data)

		$h = 1$		$h = 12$	
		best	% diff.	best	% diff.
19	CPIAUCSL	TVP1	-1.21	GK4P	-2.18
20	FEDFUNDS	TVP4	-1.69	PPT12	-4.87
21	BOGNONBR	PPT12	-1.62	GK4B	-6.26
22	M2SL	ROW410Y	0.16	ROW43Y	1.28
23	INDPRO	GK4P	-2.55	GK4B	-1.34
24	UTL11	PPT41	-0.701	KP4	-0.504
25	UNRATE	PPT41	-0.0418	KP4	-0.0811
26	HOUST	REC4	0.0216	REC4	0.0153
27	PPIFCG	GK1B	-0.504	GK4B	-0.928
28	AHEMAN	TVP4	-2.45	GK1P	-1.15
29	M1SL	GK4P	-1.25	KP1	-0.346
30	PMCP	ROW410Y	0.506	REC4	0.656
31	SP500	REC1	0.389	UC-SV	0.0478
32	GS10	TVP4	-1.54	UC-SV	0.949
33	EXUSUK	REC1	0.236	GK1P	-0.281
34	PAYEMS	PPT41	-1.58	GK1B	-2.22
35	NAPMNOI	PPT12	-0.075	KP4	-0.29
36	TB3MS	KP4	-1.79	KP4	-3.96
37	BUSLOANS	UC-SV	1.28	GK4B	-3.42
38	TOTALSL	REC4	0.138	REC4	1.12
39	AAA	KP4	-0.199	UC-SV	4.81
		Mean	-0.69	Mean	-0.90
		t-Ratio	-0.66	t-Ratio	-0.38

See Table 1 for model definitions. The "%diff" are computed as [(smallest RMSE across the break models/smallest RMSE across the no-break models)-1]x100. Results computed from Tables 3 and 4 of the TA.

Table 9: APL relative performance of best forecasting models on last sixty percent of sample (quarterly data)

		$h = 1$		$h = 4$	
		best	% diff.	best	% diff.
1	GDPC96	GK1P	1.33	UC-SV	-3.92
2	PINCOME	REC4	-0.712	UC-SV	-7.05
3	PCECC96	ROW440	-2.82	UC-SV	-0.987
4	PCECTPI	ROW120	-5.29	ROW120	-19.6
5	GPDIC96	UC-SV	-0.294	UC-SV	-0.88
6	OPHPBS	TVP1	1.41	TVP1	3.05
7	IMPGSC96	ROW120	-8.65	ROW120	-7.84
8	EXPGSC96	ROW120	-1.46	ROW120	-1.98
9	CBIC96	REC1	-3.03	REC1	-5.44
10	GCEC96	UC-SV	-5.16	UC-SV	-3.71
11	WASCUR	ROW140	-1.14	UC-SV	-3.89
12	DIVIDEND	ROW420	-7.58	REC1	-6.36
13	PSAVE	REC1	-6.03	REC1	-11.8
14	DPIC96	GK1P	0.055	UC-SV	-2.69
15	GDPDEF	KP1	2.18	ROW120	-12.8
16	ULCNFB	ROW120	-1.68	KP1	2.27
17	PRFI	ROW120	-2.56	UC-SV	-6.07
18	GSAVE	TVP4	3.32	GK4B	3.28
19	CPIAUCSL	KP1	0.348	ROW120	-15.1
20	FEDFUNDS	ROW420	-2.01	KP1	1.78
21	BOGNONBR	REC1	-20.8	REC4	-27.2
22	M2SL	ROW120	-4.39	ROW120	-9.78
23	INDPRO	ROW120	-10.2	ROW120	-8.96
24	UTL11	ROW440	-16	ROW140	-16.5
25	UNRATE	ROW440	-6.97	ROW140	-15.9
26	HOUST	ROW120	-12.2	REC1	-5.49
27	PPIFCG	GK4B	3.51	GK4B	10.3
28	AHEMAN	ROW440	-8.09	ROW440	-8.77
29	M1SL	REC1	-3.69	GK4B	3.48
30	PMCP	ROW440	-1.62	REC1	-7.87
31	SP500	REC1	-1.13	REC1	-4.21
32	GS10	ROW120	-2.16	ROW120	-21.1
33	EXUSUK	TVP1	12.2	TVP1	12.1
34	PAYEMS	ROW120	-6.83	ROW120	-3.78
35	NAPMNOI	REC4	-1.06	REC4	-4.74
36	TB3MS	ROW420	-3.4	ROW140	-8.13
37	BUSLOANS	REC1	-3.61	REC1	-5.17
38	TOTALSL	ROW120	-6.81	REC1	-3.5
39	AAA	ROW120	-5.03	ROW120	-28
		Mean	-3.54	Mean	-6.49
		t-Ratio	-0.63	t-Ratio	-0.75

See Table 1 for model definitions. The "%diff" are computed as [(largest APL across the break models/largest APL across the no-break models)-1]x100. Results computed from Tables 13 and 14 of the TA.

Table 10: APL relative performance of best forecasting models on last sixty percent of sample (monthly data)

		$h = 1$		$h = 12$	
		best	% diff.	best	% diff
19	CPIAUCSL	ROW13Y	-5.32	ROW13Y	-24.2
20	FEDFUNDS	ROW43Y	-14.6	ROW110Y	-16.9
21	BOGNONBR	REC1	-21.4	REC1	-62.2
22	M2SL	REC4	-8.86	ROW13Y	-24.7
23	INDPRO	ROW45Y	-3.64	ROW15Y	-8.96
24	UTL11	ROW410Y	-5.05	ROW110Y	-14.2
25	UNRATE	ROW410Y	-7.62	ROW110Y	-13.5
26	HOUST	ROW45Y	-6.59	ROW43Y	-21.3
27	PPIFCG	ROW15Y	-0.198	ROW15Y	-9.68
28	AHEMAN	ROW410Y	-4.99	ROW13Y	-8.6
29	M1SL	REC4	-13.6	REC4	-16
30	PMCP	ROW410Y	-5.46	REC1	-7.19
31	SP500	REC1	-1.44	REC1	-6.13
32	GS10	ROW45Y	-2.02	ROW15Y	-20.6
33	EXUSUK	REC4	-2.16	REC1	-9.39
34	PAYEMS	PPT41	0.856	ROW13Y	-8.35
35	NAPMNOI	ROW410Y	-4.04	REC4	-5.75
36	TB3MS	ROW43Y	-10.1	ROW110Y	-23.5
37	BUSLOANS	REC4	-3.31	ROW13Y	-6.82
38	TOTALSL	ROW43Y	-1.39	ROW13Y	-7.11
39	AAA	ROW45Y	-3.5	ROW13Y	-26.2
		Mean	-5.93	Mean	-16.25
		t-Ratio	-1.10	t-Ratio	-1.29

See Table 1 for model definitions. The "%diff" are computed as [(largest APL across the break models/largest APL across the no-break models)-1]x100. Results computed from Tables 15 and 16 of the TA.

Table 11: Performance comparison on forecast period starting in 2007

% diff.	RMSE				APL			
	Quarterly		Monthly		Quarterly		Monthly	
	$h = 1$	$h = 4$	$h = 1$	$h = 12$	$h = 1$	$h = 4$	$h = 1$	$h = 12$
Mean	-2.81	-3.48	-0.59	-3.86	0.09	0.24	-7.76	-11.06
t-stat	-0.61	-0.37	-0.34	0.43	0.01	0.01	-1.56	-1.21

Mean is the mean of percentage differences for all series.

Table 12: Performance comparison of three priors for AR(1) models on last sixty percent of sample (quarterly series)

horizon		PRIOR M/PRIOR I		PRIOR L/PRIOR I	
		PPT12	KP1	PPT12	KP1
RMSE					
1	Mean	-0.22	1.26	0.51	1.45
	t-stat	-0.06	0.58	0.32	0.62
4	Mean	2.21	1.21	0.81	1.20
	t-stat	0.11	0.24	0.55	0.35
APL					
1	Mean	-0.98	-3.53	-1.34	-3.58
	t-stat	-0.30	-0.56	-1.05	-0.64
4	Mean	-0.04	-13.16	-1.98	-4.69
	t-stat	-0.01	-1.97	-1.77	-0.95

Mean is the mean of percentage differences for all series.

**APPENDIX TO  
THE CONTRIBUTION OF STRUCTURAL BREAK MODELS TO  
FORECASTING MACROECONOMIC SERIES**

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This document contains four appendices to the paper of ?. The first three appendices contain details about the implementation of the estimation and forecasting of the structural break models named PPT and KP in the paper. These models are explained in Section 2 of the paper and information about the forecasting implementation of these models is presented in Section 4 of the paper. The fourth appendix contains tables that show detailed results that are summarized and discussed in Section 5 of the paper.

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## Appendix A: Technical Details for PPT Approach

In this appendix, we describe posterior and predictive simulation as well as prior elicitation for our implementation of the PPT approach. ? provide more details for posterior simulation and computing the marginal likelihood, which is used for choosing the number of breaks.

The model is defined by  $y_t = Z_t\beta_{s_t} + \sigma_{s_t}\varepsilon_t$  and by the break process which involves  $S^T = (s_1, \dots, s_T)'$  where  $s_t \in \{1, 2, \dots, K\}$  is a state variable and  $K$  is the number of in sample regimes (see Section 2 of the paper). Notice that the last regime is an absorbing state over the sample period, but PPT relax this in the forecast period.

### Priors

We use priors of the form:

$$\begin{aligned} \beta_j | \beta_0, B_0 &\sim N_m(\beta_0, B_0), \\ \beta_0 &\sim N_m(\underline{\mu}_\beta, \underline{V}_\beta), \\ B_0^{-1} &\sim \text{Wishart}(\underline{\xi}, \underline{B}), \\ \sigma_j^{-2} | v_0, d_0 &\sim \text{Gamma}(v_0, d_0), \\ v_0 &\sim \text{Gamma}(\underline{\lambda}, \underline{\rho}), \\ d_0 &\sim \text{Gamma}(\underline{c}, \underline{d}) \\ p_i &\sim \text{Beta}(\underline{a}, \underline{b}). \end{aligned}$$

In particular, in the forecasting exercise we set  $\underline{\mu}_\beta = 0$ ,  $\underline{V}_\beta = I_m$ ,  $\underline{B} = 10I_m$ ,  $\underline{\xi} = m + 1$  (where  $m$  is the dimension of  $Z_t$ ),  $\underline{\lambda} = 1$ ,  $\underline{\rho} = 0.1$ ,  $\underline{c} = 1$ ,  $\underline{d} = 0.1$ , and  $\underline{a} = \underline{b} = 1$ . This implies that all priors are proper but little informative.

### Posterior simulator

The posterior simulation algorithm is a Gibbs sampler. Given initial conditions, the data, and in each block the other parameters, the sampling is done as follows:

1. Draw  $S^T$  using Chib's (1998) algorithm.
2. Draw  $p_i$  from  $\text{Beta}(\underline{a} + T_i, \underline{b} + 1)$  for  $i = 1, \dots, K$ , where  $T_i$  is the number of observations in regime  $i$ .
3. Draw  $\beta_i | \sigma_i^2$  from Normal and  $\sigma_i^2 | \beta_i$  from Gamma, for  $i = 1, 2, \dots, K$ .
4. Draw  $\beta_0 | B_0$  from Normal and  $B_0^{-1} | \beta_0$  from Wishart.
5. Draw  $d_0 | v_0$  from Gamma and  $v_0 | d_0$  by numerical evaluation and inversion of its cdf.

## Appendix B: Technical Details for KP Approach

In this appendix, we describe posterior and predictive simulation as well as prior elicitation for our implementation of the KP approach.

It is convenient to write the model equation as  $y_t = Z_t\beta_{s_t} + \exp(\omega_{s_t}/2)\varepsilon_t$ . The transition probabilities between the states are defined in equation (5) of the paper so that the last diagonal element of the transition matrix is equal to  $p_K$  rather than one as in the PPT approach.

### Priors

We use priors of the form:

$$\begin{aligned}\beta_j &\sim N_m(\beta_{j-1}, B_0) \\ \omega_j &\sim N(\omega_{j-1}, \delta) \\ \beta_0 &\sim N_m(\mathbf{0}, \underline{V}_\beta) \\ \omega_0 &\sim N(0, \underline{V}_\omega) \\ B_0^{-1} &\sim \text{Wishart}(\underline{\xi}, \underline{B}) \\ \delta^{-1} &\sim \text{Gamma}(\underline{\kappa}_1, \underline{\kappa}_2) \\ p_{i,i} &\sim \text{Beta}(\underline{a}, \underline{b}).\end{aligned}$$

In particular, in the forecasting exercise we set  $\underline{V}_\beta = I_m$ ,  $\underline{V}_\omega = 1$ ,  $\underline{B} = 10I_m$ ,  $\underline{\xi} = m + 1$ ,  $\underline{\kappa}_1 = \underline{\kappa}_2 = 0.5$ , and  $\underline{a} = \underline{b} = 1$ . This implies that all priors are proper but very little informative.

### Posterior simulator

The posterior simulation algorithm is a Gibbs sampler. Given initial conditions, the data, and in each block the other parameters, the sampling is done as follows:

1. Draw  $S^T$  using Chib's (1998) algorithm.
2. Draw  $p_i$  from  $\text{Beta}(\underline{a} + T_i, \underline{b} + 1)$  for  $i = 1, \dots, K$ , where  $T_i$  is the number of observations in regime  $i$ .
3. Draw  $[\beta_{s_t}]_{t=1}^T$  using the modified Kalman filter algorithm (see below).
4. Draw  $[\omega_{s_t}]_{t=1}^T$  using the modified Kalman filter algorithm, after writing the model in appropriate linear state space form using the Kim, Shephard and Chib (1998) algorithm.
5. Draw  $B_0^{-1}$  and  $\delta^{-1}$ , conditional on the draws of  $\beta_t$  and  $\omega_t$ , using standard expressions.

### Modified Kalman filter algorithm

Consider a state-space model of the following form:

$$y_t = z_t a_{s_t} + \varepsilon_t \tag{1a}$$

$$a_j = a_{j-1} + \eta_{s_t} \tag{1b}$$

$$\varepsilon_t \sim N(0, \gamma_1^2), \eta_j \sim N(0, \gamma_2^2)$$



conditional on knowing  $s_t$ , where (1a) is the measurement equation and (1b) is the state equation, with observed data  $y_t$  and unobserved state  $a_{s_t}$ . If the errors  $\epsilon_t, \eta_t$  are *iid* and uncorrelated with each other, we can use the Kalman filter to estimate the state  $a$ .

Let  $a_{t|s}$  denote the expected value of  $a_t$  and  $P_{t|s}$  its corresponding variance, using data up to time  $s$ . Given starting values  $a_{0|0}$  and  $P_{0|0}$ , the Kalman filter recursions provide us with initial filtered estimates:

$$\begin{aligned} a_{t|t-1} &= a_{t-1|t-1} \\ P_{t|t-1} &= \begin{cases} P_{t-1|t-1} + \gamma_2^2 & , \text{ if } s_{t-1} \neq s_t \\ P_{t-1|t-1} & , \text{ otherwise} \end{cases} \end{aligned} \quad (2)$$

$$\begin{aligned} K_t &= P_{t|t-1} z_t' (z_t P_{t|t-1} z_t + \gamma_1^2)^{-1} \\ a_{t|t} &= a_{t|t-1} + K_t (y_t - z_t a_{t|t-1}) \\ P_{t|t} &= P_{t|t-1} - K_t z_t P_{t|t-1}. \end{aligned} \quad (3)$$

Once we reach the last period ( $t = T$ ) we take the standard draw  $a_{s_T} \sim N(a_{T|T}, P_{T|T})$ . If  $s_T = T$  then a break occurs in each observation and we have a full tvp model, so that the Carter and Kohn smoother applies to all observations  $t$ . However with structural breaks models it will be the case that  $s_T \ll T$  (i.e. the number of breaks is smaller than the number of observations, i.e. we do not have a full tvp model), we can only simulate  $a_j$  for  $j = s_T + 1, \dots, T$  (i.e. the “out-of-sample breaks” in  $a$ ) using equation (1b). For  $j = 1, \dots, s_T$  we can use a standard smoother to get smoothed estimates. To do that, we run the backward recursions for  $t = T - 1, \dots, 1$ :

$$\begin{aligned} a_{t|t+1} &= a_{t|t} + P_{t|t} P'_{t+1|t} (a_{t+1} - a_{t|t}), \text{ iff } s_{t+1} \neq s_t \\ P_{t|t+1} &= P_{t|t} - P_{t|t} P'_{t+1|t} P_{t|t}, \text{ iff } s_{t+1} \neq s_t \end{aligned}$$

and draw  $a_{s_t} \sim N(a_{t|t+1}, P_{t|t+1})$  iff  $s_{t+1} \neq s_t$ .

## Appendix C: Predictive Simulator for PPT and KP models

### Forecasting with no breaks out-of-sample (PPT model)

Since the PPT model implies that observations following  $T$  (the last sample date) are generated from  $y_{T+h}|Y_{T+h-1}, \theta_K$  where  $\theta_K = (\beta_K, \sigma_K^2)$ , i.e. under the last operating regime, we can compute predictive densities as follows:

$$p(y_{T+h}|s_{T+h} = K, s_T = K, Y_T) = \int \dots \int \prod_{j=0}^{h-1} p(y_{T+h-j}|Y_{T+h-1-j}, \theta_K) p(\theta_K|\theta_0, S_T, Y_T) p(\theta_0|S_T, Y_T, \underline{A}) p(S_T|Y_T) dy_{T+h-1} \dots dy_{T+1} d\theta_K d\theta_0 dS_{T-1}, \quad (4)$$

where the integration is done with respect to  $S_{T-1}$  rather than  $S_T$  since  $s_T = K$ . This is implemented by simulation within the Gibbs sampler for the posterior density: for each Gibbs draw of  $\theta_K$ ,  $\theta_0$  and  $S_{T-1}$ , we generate sequentially future values  $y_{T+1}, \dots, y_{T+h}$ , each from  $y_{T+h-j} \sim p(y_{T+h-j}|Y_{T+h-1-j}, \theta_K)$ , and we keep  $y_{T+h}$  as a draw of the corresponding predictive density  $p(y_{T+h}|s_{T+h} = K, s_T = K, Y_T)$ . Doing this for e.g.  $h = 4$  provides also the draws of the predictive densities for  $h \leq 4$ .

### Forecasting with breaks out-of-sample (PPT & KP models)

The previous discussion does not allow for a break to occur in the forecast period. In order to allow in the PPT for the possibility of occurrence of one new regime after  $T$ , we lift the restriction  $p_K = 1$  (something already done in the KP model) and extend the transition matrix to

$$\begin{pmatrix} p_1 & 1-p_1 & 0 & \dots & 0 & 0 & 0 \\ 0 & p_2 & 1-p_2 & \dots & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & p_{K-1} & 1-p_{K-1} & 0 \\ 0 & 0 & 0 & \dots & 0 & p_K & 1-p_K \\ 0 & 0 & 0 & \dots & 0 & 0 & 1 \end{pmatrix}.$$

Additional regimes can be added by extending further the transition matrix, but here we consider the predictive density subject to one break occurring after date  $T$ . Assume that the break occurs at date  $T + d$  where  $d$  can take any value in the set  $\{1, 2, \dots, h\}$ . For the predictive simulation of  $y_{T+h}$  with  $h < d$  (the no-post-sample break case), we proceed as above. For  $h \geq d$ , the break occurrence implies that  $y_{T+h} \sim p(y_{T+h}|Y_{T+h-1}, \theta_{K+1})$  where  $\theta_{K+1}$  is the parameter characterizing the new regime, and is drawn from its hierarchical prior density  $p(\theta_{K+1}|\theta_0)$ . The observed sample does not provide information about  $\theta_{K+1}$  and thus does not directly update this prior, but it does so indirectly by updating the prior information about  $\theta_0$  since this is drawn from its posterior distribution in the Gibbs sampler.

Assume first that  $h = d = 1$ . Then, given  $\theta_0$  (drawn in the Gibbs sampler),  $\theta_{K+1}$  is drawn from  $p(\theta_{K+1}|\theta_0)$  and given this draw,  $y_{T+1}$  is drawn from  $p(y_{T+1}|Y_T, \theta_{K+1})$ . This procedure is repeated at each iteration of the Gibbs sampler and delivers a sample of draws from the predictive density  $p(y_{T+1}|s_{T+1} = K + 1, s_T = K, Y_T)$ .

Next assume that  $h = 2$  and  $d = 1$ :  $y_{T+1}$  is simulated as explained just above, and  $y_{T+2}$  is drawn from  $p(y_{T+2}|y_{T+1}, Y_T, \theta_{K+1})$  where  $y_{T+1}$  is set at its simulated value and  $\theta_{K+1}$  is maintained to be the value used for drawing this  $y_{T+1}$ . For  $h$  larger than 2, one proceeds sequentially in the same way, i.e. freezing  $\theta_{K+1}$  and using the simulated lagged values  $y_{T+h-j}$  ( $j = 1, 2, \dots, h - 1$ ) in the conditioning of  $p(y_{T+h}|Y_{T+h-1}, \theta_{K+1})$ .

Finally if  $h \geq d \geq 1$ , the values  $y_{T+j}$  for  $j = 1, 2, \dots, d-1$  are sequentially simulated as in the no-post-sample break case. Then for  $j = d$ ,  $\theta_{K+1}$  is drawn from  $p(\theta_{K+1}|\theta_0)$  and given this draw,  $y_{T+j}$  for  $j = d, d+1, \dots, h$  are drawn sequentially. The next formula validates this simulation procedure for known break date  $|\tau_K$  equal to  $T+d$ :

$$\begin{aligned} p(y_{T+h}|\tau_K = T+d, s_{T+h} = K+1, s_T = K, Y_T) = \\ \int \dots \int \prod_{j=0}^{h-1} p(y_{T+h-j}|Y_{T+h-1-j}, \theta_{K+1}1_{\{h \geq d\}} + \theta_K 1_{\{h < d\}}) \\ p(\theta_{K+1}|\theta_0, S_T, Y_T) p(\theta_K|\theta_0, S_T, Y_T) p(\theta_0|S_T, Y_T, \underline{A}) p(S_T|Y_T) \\ dy_{T+h-1} \dots dy_{T+1} d\theta_{K+1} d\theta_K d\theta_0 dS_{T-1} \end{aligned} \quad (5)$$

where  $1_{\{h \geq d\}}$  is equal to 1 if  $h \geq d$  and 0 otherwise, and  $1_{\{h < d\}} = 1 - 1_{\{h \geq d\}}$ . To marginalize this density with respect to the break date  $d$ , we sum over all values of  $d$  as follows:  $p(y_{T+h}|s_{T+h} = K+1, s_T = K, Y_T) =$

$$\begin{aligned} \sum_{d=1}^h p(y_{T+h}|\tau_K = T+d, s_{T+h} = K+1, s_T = K, Y_T) \\ \times \Pr[\tau_K = T+d|s_{T+h} = K+1, s_T = K, Y_T] \end{aligned} \quad (6)$$

with  $\Pr[\tau_K = T+d|s_{T+h} = K+1, s_T = K, Y_T] = p_K^{d-1}(1-p_K)/(1-p_K^h)$ . Finally, we can integrate  $p(y_{T+h}|s_{T+h}, s_T = K, Y_T)$  with respect to the number of post-sample breaks (0 or 1):  $p(y_{T+h}|s_T = K, Y_T) =$

$$\begin{aligned} p(y_{T+h}|s_{T+h} = K, s_T = K, Y_T) p(s_{T+h} = K|s_T = K, Y_T) \\ p(y_{T+h}|s_{T+h} = K+1, s_T = K, Y_T) [1 - p(s_{T+h} = K|s_T = K, Y_T)] \end{aligned} \quad (7)$$

where  $p(s_{T+h} = K|s_T = K, Y_T) = p_K^h$ . This is simulated by drawing  $s_{T+h}$  from its discrete distribution, and then  $y_{T+h}$  from (4) if  $s_{T+h} = K$  and from (6) if  $s_{T+h} = K+1$ . To sample the discrete distribution, we need a value of  $p_K$ . This is simulated in the Gibbs sampler from its full conditional posterior density, which is  $\text{Beta}(\underline{a} + T_K, \underline{b} + 1)$ , where  $T_K$  is the number of observations in regime  $K$  according to the sampled  $S_T$  vector.

As an example, to implement the simulation of  $y_{T+1}$ , we substitute (4), (6) and (5) in (7) and obtain  $p(y_{T+1}|s_T = K, Y_T) =$

$$\begin{aligned} p_K \int \dots \int p(y_{T+1}|Y_T, \theta_K) p(\theta_K|\theta_0, S_T, Y_T) p(\theta_0|S_T, Y_T, \underline{A}) p(S_T|Y_T) \\ d\theta_K d\theta_0 dS_{T-1} \\ + (1-p_K) \int \dots \int p(y_{T+1}|Y_T, \theta_{K+1}) p(\theta_{K+1}|\theta_0, S_T, Y_T) p(\theta_K|\theta_0, S_T, Y_T) \\ p(\theta_0|S_T, Y_T, \underline{A}) p(S_T|Y_T) d\theta_{K+1} d\theta_K d\theta_0 dS_{T-1}. \end{aligned}$$

This formula shows that the simulation for one predictive draw in the KP model, and the PPT model with the possibility of breaks occurring out-of-sample, is performed as follows:

1. Draw  $S_T$ ,  $\theta_0$  and  $\theta_K$  from the posterior (i.e. use a draw of the Gibbs sampler once it has converged).
2. Draw  $p_K \sim \text{Beta}(\underline{a} + T_K, \underline{b} + 1)$ .
3. Draw  $s_{T+1} = K$  or  $K+1$  with respective probabilities  $(p_K, 1-p_K)$ .
4. If  $s_{T+1} = K$ , draw  $y_{T+1} \sim p(y_{T+1}|Y_T, \theta_K)$ . If  $s_{T+1} = K+1$ , draw  $\theta_{K+1} \sim p(\theta_{K+1}|\theta_0, S_T, Y_T)$  and  $y_{T+1} \sim p(y_{T+1}|Y_T, \theta_{K+1})$ .

If this is repeated as many times as one iterates in the Gibbs sampler, one obtains as many draws of the predictive of  $y_{T+1}$ . Generalizing this algorithm to  $h \geq 2$  is not difficult but requires lengthy formulas.

## Appendix D: Additional Tables

These tables are providing detailed results on which Tables and comments in the paper are based. For each series in Table 1 of the paper, we provide in the following tables the RMSE (Tables 1-4) and APL (Tables 13-16) values obtained from the recursive forecasting exercise described in Section 5 of the paper.

Tables 5-8 (respectively 17-20) are giving details about Question 2 for RMSE (respectively APL) results, Tables 9-12 and 21-24, are giving details about Question 3.

Table 1: Root mean squared errors at horizon 1 on last sixty percent of sample (quarterly data)

series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO140	RO120	RO440	RO420	REC1	REC4	UC-SV	
1	GDPC96	0.719	0.725	0.733	0.724	0.722	0.726	0.778	0.775	0.744	0.785	0.761	0.947	0.730	0.726	0.782
2	PINCOME	0.886	0.918	0.888	0.971	0.873	0.853	0.923	0.906	0.903	0.904	0.871	1.120	0.890	0.885	0.918
3	PCECC96	0.609	0.586	0.601	0.655	0.604	0.603	0.601	0.594	0.602	0.655	0.625	0.807	0.609	0.595	0.634
4	PCECTPI	0.382	0.383	0.376	0.382	0.361	0.445	0.364	0.356	0.372	0.398	0.365	0.489	0.385	0.373	0.478
5	GPDIC96	1.050	1.060	1.040	1.050	1.060	1.060	1.060	1.350	1.050	1.110	1.110	1.210	1.060	1.070	1.080
6	OPHPBS	0.716	0.702	0.719	0.710	0.714	0.715	0.728	0.722	0.745	0.741	0.778	0.831	0.717	0.706	0.716
7	IMPGSC96	0.644	0.660	0.635	0.658	0.669	0.689	0.677	0.741	0.641	0.708	0.698	0.848	0.693	0.700	0.677
8	EXPGSC96	0.586	0.590	0.576	0.595	0.633	0.673	0.583	0.612	0.548	0.585	0.552	0.715	0.696	0.700	0.562
9	CBIC96	0.879	0.900	0.926	0.962	0.948	0.921	0.886	0.896	0.897	0.954	0.917	1.100	0.876	0.881	0.910
10	GCEC96	0.863	0.839	0.861	0.842	0.858	0.859	0.985	0.919	0.891	0.894	0.896	0.978	0.861	0.841	0.850
11	WASCUR	0.722	0.717	0.726	0.730	0.721	0.703	0.717	0.736	0.740	0.818	0.773	0.964	0.725	0.721	0.848
12	DIVIDEND	0.972	1.150	0.983	1.460	0.919	0.942	1.130	1.360	1.070	1.130	2.260	2.750	0.949	1.000	0.937
13	PSAVE	0.516	0.573	0.541	0.573	0.501	0.499	0.510	0.539	0.529	0.542	0.566	0.686	0.511	0.521	0.516
14	DPIC96	0.883	0.886	0.900	0.931	0.872	0.864	0.880	0.916	0.907	0.918	0.965	1.090	0.883	0.891	0.862
15	GDPDEF	0.229	0.222	0.229	0.221	0.237	0.426	0.231	0.219	0.248	0.251	0.238	0.291	0.235	0.223	0.414
16	ULCNFB	0.991	0.938	0.942	0.944	0.931	0.980	0.990	0.983	0.963	0.984	0.955	1.100	1.020	0.946	0.962
17	PRFI	0.926	0.966	0.919	0.960	0.932	0.943	1.100	1.180	0.958	1.020	1.030	1.380	0.934	0.959	1.170
18	GSAVE	0.992	0.983	0.996	0.983	0.990	0.989	1.030	0.995	1.010	1.070	0.985	1.080	0.990	0.985	1.010
19	CPIAUCSL	0.579	0.582	0.542	0.591	0.564	0.581	0.550	0.542	0.566	0.620	0.564	0.724	0.585	0.562	0.535
20	FEDFUNDS	0.243	0.304	0.244	0.285	0.258	0.280	0.248	0.284	0.248	0.273	0.306	0.435	0.245	0.293	0.333
21	BOGNONBR	0.501	0.551	0.514	1.070	0.537	0.533	1.030	1.020	0.579	0.638	1.340	1.430	0.568	1.290	0.518
22	M2SL	0.760	0.815	0.745	0.744	0.740	0.773	0.742	0.748	0.763	0.742	0.757	0.857	0.745	0.748	0.733
23	INDPRO	0.281	0.272	0.296	0.282	0.299	0.301	0.283	0.275	0.286	0.306	0.291	0.376	0.292	0.276	0.317
24	UTLL1	0.081	0.060	0.077	0.061	0.074	0.068	0.071	0.059	0.079	0.090	0.061	0.085	0.076	0.061	0.150
25	UNRATE	0.092	0.064	0.088	0.065	0.073	0.103	0.082	0.066	0.087	0.101	0.071	0.093	0.085	0.065	0.183
26	HOUST	0.084	0.081	0.084	0.082	0.091	0.081	0.081	0.082	0.086	0.090	0.085	0.108	0.084	0.082	0.148
27	PPIFCG	1.340	1.340	1.350	1.530	1.310	1.300	1.610	1.560	1.330	1.400	1.340	1.660	1.330	1.340	1.460
28	AHEMAN	0.492	0.426	0.475	0.419	0.470	0.469	0.452	0.417	0.464	0.458	0.437	0.496	0.527	0.427	0.444
29	M1SL	1.200	1.250	1.210	1.220	1.210	1.250	1.220	1.350	1.240	1.380	1.320	1.620	1.200	1.210	1.240
30	PMCP	0.089	0.085	0.088	0.081	0.096	0.460	0.087	0.079	0.088	0.092	0.083	0.106	0.088	0.081	0.114
31	SP500	0.160	0.163	0.160	0.168	0.164	0.163	0.160	0.165	0.161	0.173	0.176	0.256	0.159	0.163	0.166
32	GS10	0.157	0.156	0.145	0.145	0.166	0.172	0.139	0.140	0.149	0.158	0.157	0.190	0.143	0.147	0.209
33	EXUSUK	1.170	1.180	1.170	1.180	1.170	1.170	1.170	1.490	1.200	1.280	1.230	1.590	1.170	1.180	1.300
34	PAYEMS	0.271	0.261	0.275	0.264	0.290	0.324	0.270	0.262	0.273	0.310	0.277	0.372	0.275	0.266	0.370
35	NAPMNOI	0.054	0.053	0.054	0.053	0.055	0.427	0.054	0.053	0.056	0.065	0.059	0.092	0.054	0.054	0.064
36	TB3MS	0.216	0.220	0.211	0.213	0.231	0.255	0.214	0.207	0.219	0.236	0.223	0.293	0.213	0.216	0.292
37	BUSLOANS	0.355	0.373	0.362	0.387	0.368	0.397	0.349	0.368	0.358	0.402	0.391	0.528	0.349	0.368	0.425
38	TOTALSL	0.168	0.171	0.167	0.169	0.166	0.320	0.167	0.169	0.173	0.186	0.182	0.211	0.168	0.170	0.219
39	AAA	0.115	0.129	0.112	0.117	0.122	0.108	0.108	0.114	0.117	0.128	0.127	0.167	0.111	0.120	0.177

See Table 4 of the paper for model definitions.

Table 2: Root mean squared errors at horizon 4  
on last sixty percent of sample (quarterly data)

series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO140	RO120	RO440	RO420	REC1	REC4	UC-SV	
1	GDPC96	0.754	0.766	0.757	0.754	0.741	0.741	0.831	0.780	0.773	0.865	0.836	1.740	0.761	0.755	0.743
2	PINCOME	0.997	1.010	0.946	1.120	0.933	0.909	1.110	0.957	0.951	1.090	0.956	1.780	1.010	1.000	0.877
3	PCECC96	0.599	0.578	0.603	0.622	0.590	0.585	0.594	0.590	0.615	0.659	0.638	1.200	0.603	0.588	0.584
4	PCECTPI	0.445	0.453	0.418	0.438	0.407	0.598	0.404	0.411	0.446	0.429	0.429	0.522	0.450	0.444	0.414
5	GPDIC96	1.040	1.040	1.050	1.070	1.040	1.040	1.210	2.420	1.090	1.410	1.270	2.000	1.040	1.040	1.040
6	OPHPBS	0.698	0.701	0.698	0.702	0.703	0.702	0.712	0.715	0.716	0.737	0.721	0.767	0.701	0.700	0.705
7	IMPGSC96	0.634	0.653	0.637	0.650	0.622	0.626	0.957	2.530	0.705	1.120	0.762	2.200	0.621	0.625	0.622
8	EXPGSC96	0.583	0.582	0.591	0.595	0.576	0.578	0.623	0.905	0.616	0.687	0.620	1.420	0.581	0.589	0.761
9	CBIC96	1.290	1.560	1.420	1.390	1.270	1.280	1.400	1.540	1.440	2.020	1.520	3.060	1.290	1.320	1.630
10	GCEC96	0.843	0.842	0.849	0.841	0.849	0.844	0.924	0.889	0.892	0.870	0.871	0.918	0.848	0.838	0.850
11	WASCUR	0.911	0.876	0.893	0.957	0.852	0.830	0.859	0.862	0.863	0.973	0.893	2.000	0.927	0.885	0.835
12	DIVIDEND	0.951	1.110	0.971	1.170	0.986	0.961	1.350	1.020	1.010	1.140	12.900	13.900	0.944	0.947	0.948
13	PSAVE	0.532	0.863	0.534	0.882	0.525	0.524	0.528	0.630	0.554	0.575	0.770	1.440	0.529	0.551	0.523
14	DPIC96	0.858	0.857	0.872	0.891	0.841	0.840	0.855	0.883	0.854	0.860	0.905	1.450	0.864	0.864	0.841
15	GDPDEF	0.300	0.307	0.286	0.304	0.319	0.598	0.290	0.302	0.366	0.338	0.330	0.404	0.315	0.312	0.334
16	ULCNFB	0.952	0.969	0.980	1.010	0.951	0.942	1.040	1.080	0.997	0.994	1.020	1.280	1.000	0.971	0.936
17	PRFI	1.030	1.080	1.070	1.120	1.060	1.060	1.290	2.890	1.080	1.150	1.170	1.710	1.070	1.110	1.090
18	GSAVE	1.010	1.020	1.010	1.020	1.000	1.000	1.060	1.060	1.020	1.100	1.090	1.220	1.010	1.020	1.000
19	CPIAUCSL	0.597	0.657	0.601	0.645	0.620	0.684	0.586	0.618	0.629	0.659	0.630	0.782	0.634	0.635	0.632
20	FEDFUNDS	0.508	0.612	0.493	0.545	0.560	0.558	0.531	0.558	0.527	0.641	0.607	0.849	0.523	0.569	0.578
21	BOGNONBR	0.640	0.700	0.651	2.080	0.632	0.631	84.10	2.130	3.930	72.80	4.730	233.0	1.380	2.960	0.618
22	M2SL	0.893	1.210	0.887	0.901	0.846	0.967	0.843	0.858	0.895	0.842	0.868	0.935	0.891	0.905	0.845
23	INDPRO	0.356	0.349	0.394	0.348	0.336	0.334	0.359	0.357	0.413	0.590	0.377	0.967	0.344	0.341	0.417
24	UTLL1	0.250	0.245	0.218	0.210	0.317	0.240	0.219	0.197	0.246	0.415	0.224	0.688	0.219	0.211	0.253
25	UNRATE	0.311	0.232	0.284	0.232	0.250	0.300	0.280	0.248	0.314	0.518	0.284	0.644	0.276	0.231	0.338
26	HOUST	0.209	0.220	0.210	0.228	0.393	0.232	0.208	0.214	0.273	0.292	0.269	0.357	0.210	0.229	0.254
27	PPIFCG	1.430	1.490	1.460	1.510	1.390	1.330	1.700	1.740	1.450	1.450	1.450	1.630	1.380	1.460	1.770
28	AHEMAN	0.575	0.432	0.543	0.429	0.495	0.433	0.473	0.436	0.541	0.482	0.440	0.476	0.636	0.438	0.426
29	M1SL	1.550	1.610	1.550	1.560	1.610	1.600	1.670	2.240	1.530	4.020	1.630	6.370	1.530	1.550	1.670
30	PMCP	0.170	0.159	0.166	0.159	0.211	0.577	0.172	0.159	0.167	0.187	0.163	0.211	0.164	0.159	0.167
31	SP500	0.173	0.172	0.168	0.169	0.170	0.171	0.169	0.173	0.172	0.190	0.183	0.481	0.168	0.169	0.180
32	GS10	0.372	0.419	0.359	0.380	0.349	0.359	0.355	0.371	0.383	0.449	0.453	0.521	0.366	0.391	0.359
33	EXUSUK	1.220	1.230	1.220	1.240	1.210	1.220	1.230	1.430	1.230	1.310	1.280	2.140	1.220	1.240	1.430
34	PAYEMS	0.520	0.516	0.538	0.518	0.505	0.514	0.520	0.527	0.584	0.900	0.572	1.550	0.509	0.529	0.597
35	NAPMNOI	0.079	0.077	0.079	0.077	0.116	0.519	0.088	0.082	0.087	0.149	0.087	0.229	0.079	0.077	0.090
36	TB3MS	0.460	0.507	0.443	0.480	0.480	0.544	0.465	0.489	0.475	0.562	0.527	0.733	0.466	0.489	0.514
37	BUSLOANS	0.584	0.601	0.612	0.607	0.586	0.574	0.569	0.582	0.603	0.682	0.632	1.060	0.571	0.575	0.675
38	TOTALSL	0.277	0.286	0.272	0.281	0.279	0.460	0.271	0.274	0.293	0.337	0.301	0.409	0.276	0.288	0.319
39	AAA	0.307	0.360	0.290	0.313	0.282	0.272	0.292	0.314	0.333	0.457	0.383	0.482	0.301	0.322	0.307

See Table 4 of the paper for model definitions.

Table 3: Root mean squared errors at horizon 1 on last sixty percent of sample (monthly data)

Series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO110Y	RO15Y	RO13Y	RO410Y	RO45Y	RO43Y	REC1	REC4	UC-SV	
19	CPIAUCSL	0.252	0.264	0.251	0.277	0.249	0.277	0.249	0.251	0.253	0.252	0.257	0.256	0.262	0.275	0.252	0.264	0.259
20	FEDFUNDS	0.063	0.064	0.066	0.060	0.063	0.110	0.062	0.059	0.063	0.065	0.066	0.062	0.075	0.083	0.063	0.060	0.094
21	BOGNONBR	0.307	0.338	0.337	0.325	0.337	0.334	0.500	0.615	0.403	0.410	0.417	0.750	0.854	0.865	0.400	0.735	0.312
22	M2SL	0.346	0.373	0.341	0.352	0.341	0.417	0.338	0.337	0.344	0.340	0.341	0.336	0.346	0.356	0.349	0.345	0.342
23	INDPRO	0.681	0.658	0.693	0.690	0.677	0.678	0.700	0.703	0.690	0.709	0.736	0.671	0.697	0.755	0.684	0.675	0.685
24	UTL11	0.061	0.053	0.059	0.054	0.057	0.055	0.055	0.054	0.059	0.063	0.064	0.053	0.057	0.062	0.059	0.055	0.119
25	UNRATE	0.018	0.017	0.018	0.017	0.020	0.065	0.017	0.017	0.018	0.019	0.019	0.017	0.018	0.018	0.018	0.017	0.039
26	HOUST	0.079	0.075	0.079	0.075	0.086	0.088	0.081	0.076	0.079	0.082	0.082	0.077	0.081	0.083	0.079	0.075	0.093
27	PIIFCG	0.720	0.749	0.729	0.752	0.712	0.711	0.725	0.746	0.729	0.727	0.738	0.751	0.761	0.796	0.715	0.729	0.753
28	AHEMAN	0.450	0.437	0.448	0.441	0.450	0.448	0.439	0.427	0.463	0.452	0.451	0.437	0.440	0.452	0.476	0.453	0.456
29	M2SL	0.808	0.850	0.816	0.889	0.798	0.816	0.819	0.887	0.838	0.839	0.853	0.839	0.939	1.010	0.814	0.792	0.836
30	PMCP	0.050	0.048	0.051	0.048	0.053	0.070	0.050	0.048	0.050	0.051	0.052	0.048	0.050	0.052	0.050	0.048	0.403
31	SP500	0.370	0.373	0.371	0.378	0.370	0.369	0.370	0.373	0.370	0.376	0.379	0.376	0.388	0.399	0.367	0.368	0.381
32	GS10	0.036	0.036	0.036	0.032	0.046	0.068	0.034	0.032	0.035	0.035	0.036	0.033	0.035	0.036	0.034	0.032	0.056
33	EXUSUK	0.240	0.240	0.241	0.245	0.243	0.242	0.242	0.244	0.242	0.244	0.249	0.244	0.256	0.270	0.240	0.240	0.255
34	PAYEMS	0.150	0.132	0.148	0.132	0.158	0.169	0.148	0.132	0.150	0.154	0.154	0.136	0.142	0.152	0.158	0.134	0.138
35	NAPMNOI	0.038	0.038	0.038	0.038	0.042	0.172	0.039	0.039	0.038	0.039	0.040	0.039	0.042	0.043	0.038	0.038	0.050
36	TB3MS	0.054	0.053	0.657	0.049	0.055	0.147	0.052	0.050	0.053	0.054	0.054	0.051	0.057	0.061	0.052	0.050	0.081
37	BUSLOANS	0.681	0.709	0.671	0.645	0.676	0.680	0.670	0.650	0.675	0.699	0.695	0.662	0.704	0.735	0.670	0.643	0.637
38	TOTALSL	0.367	0.328	0.678	0.355	0.367	0.409	0.362	0.330	0.371	0.379	0.382	0.334	0.356	0.367	0.373	0.327	0.329
39	AAA	0.029	0.028	0.446	0.026	0.039	0.064	0.027	0.026	0.028	0.029	0.029	0.027	0.028	0.029	0.028	0.026	0.045

See Table 4 of the paper for model definitions.

Table 4: Root mean squared errors at horizon 12 on last sixty percent of sample (monthly data)

Series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO110Y	RO15Y	RO13Y	RO410Y	RO45Y	RO43Y	REC1	REC4	UC-SV	
19	CPIAUCSL	0.292	0.293	0.306	0.310	0.298	0.314	0.299	0.296	0.305	0.305	0.307	0.300	0.306	0.317	0.298	0.298	0.310
20	FEDFUNDS	0.216	0.424	0.221	0.218	0.322	0.305	0.220	0.239	0.235	0.304	0.303	0.231	0.295	0.470	0.229	0.235	0.227
21	BOGNONBR	0.336	0.340	0.352	0.380	0.336	0.333	29.90	382.0	4.100	7.690	9.710	66.00	180.0	3400.	3.980	64.10	0.355
22	M2SL	0.409	1.910	0.416	0.448	0.382	0.526	0.383	0.380	0.404	0.388	0.381	0.401	0.386	0.375	0.407	0.403	0.395
23	INDPRO	0.686	0.696	0.718	1.000	0.681	0.678	0.784	0.779	0.690	0.715	0.744	0.716	0.812	6.200	0.686	0.685	0.855
24	UTL11	0.432	0.414	0.359	0.342	0.815	0.602	0.376	0.358	0.408	0.654	1.370	0.360	0.548	1.360	0.359	0.344	0.394
25	UNRATE	0.116	0.102	0.115	0.102	0.288	0.162	0.114	0.114	0.131	0.200	0.226	0.107	0.167	0.233	0.112	0.102	0.127
26	HOUST	0.243	0.225	0.245	0.223	0.506	0.341	0.231	0.228	0.275	0.298	0.281	0.296	0.316	0.412	0.247	0.223	0.239
27	PIIFCG	0.756	0.767	0.756	0.806	0.738	0.735	0.757	0.756	0.764	0.767	0.768	0.763	0.760	0.791	0.741	0.742	0.881
28	AHEMAN	0.460	0.459	0.459	0.463	0.442	0.452	0.448	0.449	0.469	0.458	0.451	0.464	0.454	0.449	0.475	0.474	0.447
29	MISL	0.831	1.180	0.825	2.800	0.853	0.843	0.838	1.870	0.831	0.844	0.849	0.827	2.750	8.000	0.828	0.827	0.839
30	PMCP	0.173	0.162	0.179	0.162	0.389	0.163	0.191	0.183	0.176	0.196	0.239	0.163	0.175	0.232	0.169	0.161	0.401
31	SP500	0.379	0.385	0.381	0.398	0.378	0.380	0.381	0.382	0.380	0.387	0.388	0.380	0.393	0.423	0.378	0.379	0.378
32	GS10	0.143	0.231	0.150	0.152	0.147	0.177	0.144	0.150	0.158	0.190	0.202	0.164	0.190	0.188	0.150	0.152	0.142
33	EXUSUK	0.256	0.257	0.258	0.287	0.255	0.256	0.258	0.260	0.256	0.262	0.263	0.256	0.268	0.897	0.256	0.255	0.281
34	PAYEMS	0.209	0.204	0.225	0.214	0.202	0.196	0.206	0.226	0.201	0.229	0.282	0.214	0.333	0.385	0.212	0.202	0.231
35	NAPMNOI	0.081	0.080	0.080	0.079	1.160	0.233	0.097	0.102	0.087	0.110	0.160	0.084	0.136	0.204	0.081	0.079	0.105
36	TB3MS	0.200	0.275	0.547	0.187	0.220	0.306	0.188	0.204	0.202	0.248	0.252	0.197	0.241	1.450	0.196	0.195	0.201
37	BUSLOANS	0.955	2.420	0.994	0.967	0.959	0.895	0.991	0.953	0.932	1.020	1.040	0.941	1.040	1.080	0.947	0.922	1.030
38	TOTALSL	0.489	0.465	0.588	0.465	0.483	0.537	0.491	0.465	0.508	0.520	0.549	0.473	0.528	0.727	0.523	0.460	0.484
39	AAA	0.123	0.329	0.320	0.126	0.169	0.153	0.126	0.131	0.142	0.225	0.225	0.146	0.212	0.204	0.125	0.126	0.117

See Table 4 of the paper for model definitions.



Table 5: RMSE ( $h = 1$ ) relative performance of break models on last sixty percent of sample (quarterly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVP1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVP1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVP1</u>	<u>GK1B</u> <u>TVP1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVP4</u>	<u>KP4</u> <u>TVP4</u>	
1	GDPC96	-1.93	-0.436	-1	-7.64	1.52	0.944	-5.83	-0.567	-7.24	-6.71	0.139	-6.45	-6.58
2	PINCOME	-0.249	1.49	3.84	-4.03	1.74	4.1	-3.79	2.32	-5.44	-7.58	-5.51	1.25	7.15
3	PCECC96	1.33	0.802	1.08	1.46	-0.516	-0.244	0.132	0.274	0.652	0.377	-10.6	-1.43	10.2
4	PCECTPI	1.61	5.88	-14.1	4.97	4.2	-15.4	3.31	-18.8	-0.858	22.1	0.205	7.38	7.16
5	GPDIC96	0.447	-0.809	-0.633	-0.925	-1.25	-1.08	-1.37	0.178	-0.117	-0.294	1.06	-21.4	-22.2
6*	OPHPBS	-0.3	0.366	0.261	-1.64	0.668	0.563	-1.35	-0.104	-2	-1.9	-1.07	-2.7	-1.65
7	IMPGSC96	1.51	-3.74	-6.53	-4.88	-5.17	-7.92	-6.29	-2.9	-1.18	1.76	0.394	-10.9	-11.2
8	EXPGSC96	1.71	-7.46	-12.9	0.526	-9.01	-14.4	-1.17	-5.92	8.63	15.5	-0.737	-3.51	-2.8
9	CBIC96	-5.04	-7.22	-4.5	-0.788	-2.3	0.564	4.48	2.93	6.93	3.89	-6.47	0.411	7.35
10	GCEC96	0.16	0.551	0.483	-12.4	0.391	0.323	-12.5	-0.0678	-12.9	-12.8	-0.336	-8.66	-8.35
11	WASCUR	-0.552	0.183	2.67	0.636	0.739	3.24	1.19	2.48	0.453	-1.98	-1.77	-2.57	-0.817
12	DIVIDEND	-1.09	5.77	3.22	-14.3	6.93	4.36	-13.4	-2.41	-19	-17	-21.4	-15.7	7.3
13	PSAVE	-4.62	3.02	3.46	1.21	8.01	8.47	6.11	0.43	-1.76	-2.18	0.0159	6.38	6.36
14*	DPIC96	-1.85	1.31	2.19	0.367	3.22	4.11	2.26	0.865	-0.936	-1.78	-4.86	-3.26	1.68
15	GDPDEF	0.134	-3.07	<u>-46.1</u>	-0.565	-3.2	<u>-46.2</u>	-0.698	<u>-44.4</u>	2.59	<u>84.6</u>	0.555	1.71	1.15
16	ULCNFB	5.17	6.48	1.06	0.0494	1.24	-3.91	-4.87	-5.09	-6.04	-0.997	-0.599	-4.56	-3.98
17	PRF I	0.827	-0.632	-1.77	-16	-1.45	-2.58	-16.5	-1.15	-15.5	-14.5	0.592	-18.4	-18.9
18*	GSAVE	-0.345	0.213	0.351	-3.72	0.561	0.699	-3.39	0.138	-3.93	-4.06	-0.00192	-1.2	-1.2
19	CPIAUCSL	6.86	2.72	-0.337	5.3	-3.88	-6.73	-1.46	-2.97	2.51	5.65	-1.42	7.34	8.89
20	FEDFUNDS	-0.334	-5.91	-13.4	-2.18	-5.6	-13.1	-1.85	-7.92	3.97	12.9	6.5	7.08	0.544
21	BOGNONBR	-2.42	-6.59	-5.97	<u>-51.5</u>	-4.27	-3.64	<u>-50.3</u>	0.655	<u>-48.1</u>	<u>-48.4</u>	<u>-48.3</u>	<u>-46.1</u>	4.15
22*	M2SL	2.08	2.77	-1.57	2.54	0.683	-3.57	0.451	-4.22	-0.23	4.17	9.51	8.97	-0.495
23	INDPRO	-4.98	-6.05	-6.68	-0.803	-1.12	-1.79	4.4	-0.675	5.58	6.3	-3.75	-1.24	2.6
24*	UTL11	5.95	10.2	19.9	13.9	3.99	13.1	7.47	8.8	3.35	-5.01	-2.9	1.41	4.44
25	UNRATE	5.06	27.4	-10.5	12.7	21.3	-14.8	7.26	-29.7	-11.6	25.9	-0.595	-2.76	-2.18
26*	HOUST	-0.208	-7.73	3.19	3.4	-7.54	3.41	3.61	11.8	12.1	0.2	-1.39	-0.58	0.822
27	PPIFCG	-1.19	2.3	3.24	-17	3.53	4.48	-16	0.922	-18.9	-19.6	-11.9	-13.8	-2.23
28	AHEMAN	3.65	4.7	4.93	8.87	1.01	1.24	5.03	0.22	3.98	3.75	1.59	2.01	0.411
29	MISL	-0.706	-1.09	-4.2	-1.81	-0.386	-3.52	-1.11	-3.15	-0.729	2.49	2.56	-7.29	-9.6
30	PMCP	0.626	-7.3	<u>-80.7</u>	1.57	-7.88	<u>-80.8</u>	0.939	<u>-79.2</u>	9.57	426	4.86	6.4	1.47
31*	SP500	0.437	-2.31	-1.88	-0.152	-2.74	-2.31	-0.586	0.438	2.21	1.77	-2.61	-0.789	1.87
32	GS10	8.36	-5.48	-8.63	12.8	-12.8	-15.7	4.07	-3.33	19.3	23.4	7.59	11.1	3.29
33	EXUSUK	0.178	0.491	0.465	-0.0445	0.312	0.286	-0.222	-0.0261	-0.533	-0.507	-0.46	-21	-20.7
34	PAYEMS	-1.51	-6.83	-16.5	0.24	-5.4	-15.3	1.78	-10.4	7.59	20.1	-0.964	-0.296	0.675
35*	NAPMNOI	0.443	-0.695	<u>-87.3</u>	1.02	-1.13	<u>-87.4</u>	0.576	<u>-87.2</u>	1.73	697	0.456	0.72	0.262
36	TB3MS	2.48	-6.63	-15.2	0.951	-8.89	-17.2	-1.49	-9.13	8.12	19	2.94	6.25	3.21
37	BUSLOANS	-1.77	-3.35	-10.4	1.86	-1.6	-8.77	3.7	-7.28	5.39	13.7	-3.71	1.27	5.17
38*	TOTALSL	0.515	1.62	<u>-47.4</u>	0.978	1.1	<u>-47.6</u>	0.461	<u>-48.2</u>	-0.631	<u>91.9</u>	1.12	0.836	-0.285
39	AAA	2.76	-5.26	6.74	6.81	-7.8	3.88	3.95	12.7	12.7	0.0615	10.1	12.5	2.17
	Mean	0.595	-0.265	<u>-2.275</u>	<u>-0.177</u>	-0.841	<u>-2.806</u>	<u>-0.866</u>	<u>-2.019</u>	0.206	1.078	<u>-0.865</u>	<u>-1.72</u>	-0.637
	t-stat.	0.203	-0.041	<u>-0.307</u>	<u>-0.026</u>	-0.146	<u>-0.371</u>	<u>-0.148</u>	<u>-0.268</u>	<u>-0.604</u>	0.077	<u>-0.154</u>	<u>-0.207</u>	-0.084

See Table 4 of the paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. A \* means no break was detected for the series. Results computed from Table 1.

Table 6: RMSE ( $h = 4$ ) relative performance of break models on last sixty percent of sample (quarterly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVP1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVP1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVP1</u>	<u>GK1B</u> <u>TVP1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVP4</u>	<u>KP4</u> <u>TVP4</u>	
1	GDPC96	-0.442	1.68	1.77	-9.28	2.14	2.22	-8.88	0.0794	-10.8	-10.9	1.53	-1.87	-3.35
2	PINCOME	5.4	6.82	9.65	-10.3	1.35	4.03	-14.9	2.65	-16	-18.2	-9.6	5.37	16.6
3	PCECC96	-0.755	1.57	2.37	0.879	2.34	3.15	1.65	0.793	-0.68	-1.46	-7.08	-2.04	5.42
4	PCECTPI	6.48	9.5	-25.6	10.3	2.84	-30.1	3.61	-32	0.743	<u>48.2</u>	3.28	10.2	6.73
5	GPDIC96	-1.3	-0.0047	0.182	-13.8	1.31	1.5	-12.7	0.186	-13.8	-13.9	-2.43	-56.9	-55.8
6*	OPHPBS	0.0433	-0.608	-0.54	-1.95	-0.651	-0.583	-2	0.0687	-1.35	-1.42	-0.0193	-1.9	-1.88
7	IMPGSC96	-0.502	1.98	1.36	-33.7	2.5	1.87	-33.4	-0.612	-35	<u>-34.6</u>	0.444	<u>-74.2</u>	<u>-74.3</u>
8	EXPGSC96	-1.4	1.15	0.863	-6.44	2.59	2.3	-5.11	-0.283	-7.5	-7.24	-2.15	<u>-35.7</u>	<u>-34.3</u>
9	CBIC96	-9.25	1.94	0.933	-8.05	12.3	11.2	1.32	-0.988	-9.8	-8.9	12.1	1.25	-9.71
10	GCEC96	-0.734	-0.668	-0.142	-8.78	0.0661	0.597	-8.11	0.53	-8.17	-8.65	0.201	-5.3	-5.49
11	WASCUR	1.91	6.83	9.73	6.03	4.83	7.67	4.04	2.72	-0.751	-3.37	-8.5	1.59	11
12	DIVIDEND	-2.05	-3.52	-0.985	-29.8	-1.5	1.08	-28.3	2.62	-27.2	-29.1	-5.25	8.84	14.9
13	PSAVE	-0.499	1.28	1.42	0.641	1.79	1.93	1.15	0.137	-0.631	-0.767	-2.23	<u>36.9</u>	<u>40</u>
14*	DPIC96	-1.59	2.06	2.15	0.294	3.7	3.8	1.91	0.0897	-1.73	-1.81	-3.8	-3	0.837
15	GDPDEF	4.78	-5.97	<u>-49.8</u>	3.4	-10.3	<u>-52.1</u>	-1.32	<u>-46.7</u>	9.96	<u>106</u>	0.938	1.81	0.867
16	ULCNFB	-2.85	0.0528	1.02	-8.72	2.99	3.98	-6.04	0.962	-8.77	-9.64	-4.14	-10.6	-6.76
17	PRFI	-3.07	-2.81	-2.02	-19.7	0.264	1.08	-17.1	0.813	-17.3	-18	-3.56	<u>-62.5</u>	<u>-61.1</u>
18*	GSAVE	-0.143	0.755	0.728	-4.77	0.899	0.872	-4.63	-0.0269	-5.48	-5.45	-0.313	-4.12	-3.81
19	CPIAUCSL	-0.654	-3.67	-12.7	1.89	-3.04	-12.1	2.56	-9.36	5.77	16.7	1.98	6.36	4.3
20	FEDFUNDS	3.22	-9.27	-8.87	-4.16	-12.1	-11.7	-7.15	0.443	5.63	5.16	12.4	9.6	-2.46
21	BOGNONBR	-1.62	1.24	1.4	<u>-99.2</u>	2.92	3.07	<u>-99.2</u>	0.151	<u>-99.2</u>	<u>-66.4</u>	<u>-67.2</u>	<u>-67.2</u>	-2.26
22*	M2SL	0.665	5.54	-7.73	5.82	4.84	-8.34	5.12	-12.6	0.265	14.7	<u>34.5</u>	<u>41.3</u>	5.04
23	INDPRO	-9.81	5.95	6.39	-0.883	17.5	18	9.9	0.419	-6.45	-6.84	0.344	-2.05	-2.39
24*	UTL11	14.6	-21.3	4.13	13.8	<u>-31.3</u>	-9.13	-0.716	<u>32.3</u>	44.6	9.26	16.5	24.1	6.55
25	UNRATE	9.71	24.6	3.69	11.2	13.5	-5.48	1.39	-16.8	-10.7	7.27	0.131	-6.16	-6.28
26*	HOUST	-0.549	-46.8	-9.92	0.674	<u>-46.5</u>	-9.43	1.23	<u>69.3</u>	89.2	11.8	-3.54	2.65	6.41
27	PPIFCG	-1.61	3.17	7.75	-15.5	4.86	9.52	-14.2	4.44	-18.1	-21.6	-1.26	-14.3	-13.2
28	AHEMAN	5.9	16.2	32.9	21.6	9.71	25.5	14.9	14.4	4.7	-8.46	0.511	-1.03	-1.54
29	MISL	0.0875	-3.54	-2.85	-6.96	-3.62	-2.94	-7.04	0.709	-3.55	-4.23	3.29	-28	-30.3
30	PMCP	2.23	-19.5	<u>-70.6</u>	-1.05	-21.2	<u>-71.2</u>	-3.2	<u>-63.4</u>	22.9	<u>236</u>	0.229	0.113	-0.116
31*	SP500	2.73	1.66	1.3	2.28	-1.04	-1.39	-0.444	-0.354	0.604	0.961	1.84	-0.672	-2.47
32	GS10	3.8	6.53	3.61	4.86	2.64	-0.179	1.03	-2.75	-1.57	1.21	10.2	12.9	2.52
33	EXUSUK	-0.269	0.453	0.236	-0.614	0.725	0.507	-0.346	-0.216	-1.06	-0.848	-0.208	-13.9	-13.8
34	PAYEMS	-3.34	2.87	1.18	0.013	6.43	4.68	3.47	-1.64	-2.78	-1.15	-0.345	-2.11	-1.77
35*	NAPMNOI	0.19	<u>-31.7</u>	<u>-84.8</u>	-9.87	<u>-31.9</u>	<u>-84.8</u>	-10	<u>-77.7</u>	32.1	<u>493</u>	-0.55	-6.81	-6.3
36	TB3MS	4.01	-4.09	-15.4	-0.928	-7.79	-18.6	-4.75	-11.8	3.3	17.1	5.52	3.7	-1.72
37	BUSLOANS	-4.45	-0.309	1.78	2.67	4.34	6.52	7.46	2.09	2.99	0.88	-1.06	3.26	4.37
38*	TOTALSL	1.56	-0.795	<u>-39.8</u>	2.05	-2.32	<u>-40.8</u>	0.48	<u>-39.3</u>	2.87	<u>69.6</u>	1.76	4.36	2.56
39	AAA	6.04	9.06	13.1	5.28	2.85	6.62	-0.72	3.67	-3.47	-6.88	15	14.7	-0.316
	Mean	0.679	<u>-0.262</u>	<u>0.654</u>	<u>-2.673</u>	<u>1.352</u>	<u>0.335</u>	<u>-3.417</u>	<u>-1.559</u>	<u>-4.369</u>	<u>-4.862</u>	<u>0.869</u>	<u>-0.663</u>	<u>-0.818</u>
	t-stat.	0.151	<u>-0.024</u>	<u>0.071</u>	<u>-0.249</u>	<u>0.195</u>	<u>0.034</u>	<u>-0.363</u>	<u>-0.203</u>	<u>-0.416</u>	<u>-0.315</u>	<u>0.147</u>	<u>-0.060</u>	<u>-0.095</u>

See Table 4 of the paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. A \* means no break was detected for the series. Results computed from Table 2.

Table 7: RMSE ( $h = 1$ ) relative performance of break models on last sixty percent of sample (monthly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVP1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVP1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVP1</u>	<u>GK1B</u> <u>TVP1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVP4</u>	<u>KP4</u> <u>TVP4</u>	
19	CPIAUCSL	0.437	0.949	-9.3	1.14	0.509	-9.7	0.699	-10.2	0.189	11.5	-4.38	5.46	10.3
20	FEDFUNDS	-4.35	-0.0516	<u>-42.5</u>	2.5	4.49	<u>-39.9</u>	7.16	<u>-42.5</u>	2.55	<u>78.4</u>	6.82	8.22	1.31
21	BOGNONBR	-8.96	-8.84	-8.14	<u>-38.6</u>	0.13	0.895	<u>-32.5</u>	0.764	<u>-32.6</u>	<u>-33.1</u>	4.08	<u>-45.1</u>	<u>-47.2</u>
22	M2SL	1.53	1.57	-17	2.2	0.0401	-18.2	0.666	-18.3	0.625	23.1	6.21	10.9	4.45
23	INDPRO	-1.79	0.52	0.422	-2.7	2.35	2.25	-0.924	-0.098	-3.2	-3.11	-4.65	-6.45	-1.89
24	UTL11	3.65	6.23	9.75	9.91	2.49	5.89	6.04	3.32	3.47	0.143	-3	-2.56	0.461
25	UNRATE	1.86	-9.4	<u>-72.6</u>	3.44	-11.1	<u>-73.1</u>	1.55	<u>-69.7</u>	14.2	<u>277</u>	-0.206	-1.75	-1.54
26*	HOUST	-0.0325	-8.55	-10.6	-2.75	-8.52	-10.6	-2.72	-2.23	6.35	8.78	0.102	-0.22	-0.322
27	PPIFCG	-1.21	1.15	1.26	-0.665	2.39	2.51	0.556	0.113	-1.79	-1.9	-0.456	0.399	0.858
28	AHEMAN	0.458	-0.00926	0.403	2.58	-0.465	-0.0548	2.12	0.412	2.59	2.17	-0.928	2.5	3.47
29	M1SL	-1.02	1.32	-1.01	-1.29	2.36	0.0115	-0.278	-2.3	-2.58	-0.29	-4.44	-4.2	0.251
30	PMCP	-1.05	-5.79	-27.7	0.8	-4.78	-27	1.87	-23.3	6.99	<u>39.5</u>	0.113	1.01	0.897
31*	SP500	-0.223	0.152	0.34	0.0136	0.375	0.564	0.237	0.188	-0.138	<u>-0.325</u>	-1.27	-0.00883	1.28
32	GS10	-0.218	-23	<u>-47.7</u>	5.22	-22.9	<u>-47.6</u>	5.45	<u>-32</u>	<u>36.7</u>	<u>101</u>	9.72	11.5	1.61
33	EXUSUK	-0.304	-1.17	-0.683	-0.891	-0.871	-0.38	-0.589	0.496	0.285	-0.21	-1.73	-1.45	0.286
34	PAYEMS	1.6	-4.89	-11.3	1.41	-6.38	-12.6	-0.191	-6.69	6.61	14.3	-0.276	-0.341	-0.0655
35*	NAPMNOI	-0.27	-8.76	<u>-77.9</u>	-1.63	-8.51	<u>-77.8</u>	-1.37	<u>-75.8</u>	7.81	<u>345</u>	0.0893	-1.84	-1.92
36	TB3MS	<u>-91.8</u>	-1.93	<u>-63.2</u>	5.01	<u>1.09E+3</u>	<u>347</u>	<u>1.18E+3</u>	<u>-62.5</u>	7.09	<u>186</u>	7.06	5.8	-1.17
37	BUSLOANS	1.47	0.774	0.219	1.6	-0.689	-1.24	0.129	-0.551	0.824	1.38	9.93	9.01	-0.842
38	TOTALSL	<u>-45.9</u>	0.0419	-10.4	1.24	<u>84.9</u>	<u>65.7</u>	<u>87.1</u>	-10.4	1.2	12.9	-7.6	-0.72	7.45
39	AAA	<u>-93.5</u>	-26.2	<u>-54.5</u>	6.67	<u>1.04E+3</u>	<u>601</u>	<u>1.54E+3</u>	<u>-38.3</u>	<u>44.6</u>	<u>134</u>	6.14	4.79	-1.27
Mean		<u>-0.468</u>	-4.090	<u>-8.215</u>	<u>1.690</u>	<u>-2.727</u>	<u>-4.832</u>	<u>1.200</u>	<u>-4.585</u>	<u>2.949</u>	<u>5.264</u>	1.016	<u>2.002</u>	<u>-1.124</u>
t-stat.		<u>-0.171</u>	-0.509	<u>-0.596</u>	<u>0.526</u>	<u>-0.406</u>	<u>-0.514</u>	<u>0.447</u>	<u>-0.591</u>	<u>0.662</u>	<u>0.656</u>	0.204	<u>0.395</u>	<u>0.376</u>

See Table Table 4 of the paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. A \* means no break was detected for the series. Results computed from Table 3.

Table 8: RMSE ( $h = 12$ ) relative performance of break models on last sixty percent of sample (monthly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVP1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVP1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVP1</u>	<u>GK1B</u> <u>TVP1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVP4</u>	<u>KP4</u> <u>TVP4</u>	
19	CPIAUCSL	-4.55	-1.81	-6.93	-2.3	2.87	-2.49	2.36	-5.21	-0.498	4.97	-5.57	-1.05	4.79
20	FEDFUNDS	-2.41	-33.1	-29.2	-1.93	<u>-31.4</u>	-27.5	0.491	5.72	<u>46.5</u>	<u>38.6</u>	<u>94.8</u>	<u>77.6</u>	-8.87
21	BOGNONBR	-4.71	-0.126	0.726	<u>-98.9</u>	4.81	5.71	<u>-98.8</u>	0.853	<u>-98.9</u>	<u>-98.9</u>	-10.6	<u>-99.9</u>	<u>-99.9</u>
22	M2SL	-1.53	7.2	-22.1	6.94	8.87	-20.9	8.59	-27.4	<u>-0.251</u>	<u>37.3</u>	<u>327</u>	<u>403</u>	17.7
23	INDPRO	-4.49	0.699	1.08	-12.5	5.44	5.84	-8.41	0.383	-13.1	-13.5	<u>-30.4</u>	-10.6	28.4
24	UTL11	20.3	<u>-47</u>	-28.3	14.9	<u>-56</u>	<u>-40.4</u>	-4.5	<u>35.4</u>	<u>117</u>	<u>60.2</u>	20.9	15.7	-4.3
25	UNRATE	0.673	<u>-59.7</u>	-28.3	1.89	<u>-59.9</u>	-28.7	1.2	<u>77.8</u>	<u>153</u>	<u>42</u>	0.168	-10.8	-11
26*	HOUST	-0.934	<u>-52</u>	-28.8	5.19	<u>-51.6</u>	-28.1	6.19	<u>48.4</u>	<u>119</u>	<u>47.7</u>	0.94	-1.17	-2.09
27	PPIFCG	-0.116	2.38	2.8	-0.162	2.5	2.92	-0.0458	0.409	-2.48	-2.88	-4.81	1.48	6.61
28	AHEMAN	0.13	4.1	1.71	2.66	3.96	1.58	2.52	-2.3	-1.39	0.933	-0.709	2.2	2.93
29	M1SL	0.752	-2.65	-1.42	-0.815	-3.38	-2.15	-1.55	1.27	1.89	0.61	-58	-37	50.1
30	PMCP	-3.35	<u>-55.6</u>	5.61	-9.82	<u>-54</u>	9.27	-6.69	<u>138</u>	<u>103</u>	-14.6	-0.147	-11.3	-11.2
31*	SP500	-0.571	0.317	-0.256	-0.343	0.893	0.316	0.229	-0.571	-0.657	-0.0868	-3.24	0.852	4.23
32	GS10	-4.41	-2.42	-18.9	-0.353	2.08	-15.2	4.24	-16.9	2.12	22.9	<u>52</u>	<u>53.6</u>	1.04
33	EXUSUK	-0.832	0.365	-0.33	-0.94	1.21	0.506	-0.109	-0.692	-1.3	-0.612	-10.4	-1.2	10.3
34	PAYEMS	-7.09	3.83	6.6	1.53	11.8	14.7	9.29	2.66	-2.21	-4.75	-4.72	-9.82	-5.36
35*	NAPMNOI	0.502	<u>-93.1</u>	<u>-65.5</u>	-17	<u>-93.1</u>	<u>-65.7</u>	-17.4	<u>397</u>	<u>1.10E+3</u>	<u>141</u>	0.877	-22.2	-22.9
36	TB3MS	-63.5	-9.13	<u>-34.8</u>	6.17	<u>149</u>	<u>78.6</u>	<u>191</u>	-28.2	<u>16.8</u>	<u>62.8</u>	<u>46.9</u>	<u>35</u>	-8.14
37	BUSLOANS	-3.91	-0.437	6.64	-3.68	3.62	11	0.239	7.11	-3.26	-9.68	<u>151</u>	<u>154</u>	1.49
38	TOTALSL	-16.8	1.23	-8.87	-0.447	21.6	9.5	19.6	-9.97	-1.65	9.24	0.0115	-0.119	-0.131
39	AAA	-61.5	-27.2	-19.4	-2.35	<u>88.9</u>	<u>109</u>	<u>153</u>	<u>10.6</u>	<u>34.1</u>	<u>21.2</u>	<u>160</u>	<u>152</u>	-3.25
	Mean	-7.540	<u>-3.547</u>	<u>-8.823</u>	<u>-0.668</u>	<u>5.098</u>	<u>-3.747</u>	<u>0.902</u>	<u>-3.890</u>	<u>-0.460</u>	<u>1.057</u>	<u>-1.331</u>	<u>-3.694</u>	<u>0.013</u>
	t-stat.	-0.390	<u>-0.322</u>	<u>-0.653</u>	<u>-0.096</u>	<u>0.823</u>	<u>-0.257</u>	<u>0.115</u>	<u>-0.343</u>	<u>-0.072</u>	<u>0.092</u>	<u>-0.166</u>	<u>-0.399</u>	<u>0.001</u>

See Table 4 of the paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. A \* means no break was detected for the series. Results computed from Table 4.

Table 9: RMSE ( $h = 1$ ) relative performance of lag orders  
on last sixty percent of sample (quarterly data)

Series	$\frac{PPT12}{PPT41}$	$\frac{KPI}{KPA}$	$\frac{TVPI}{TVPA}$	$\frac{RO140}{RO440}$	$\frac{RO120}{RO420}$	$\frac{RECI}{RECA}$	
1	GDPC96	-0.834	1.25	0.44	-2.27	-17.1	0.547
2	PINCOME	-3.5	-8.58	1.8	3.76	-18.9	0.578
3	PCECC96	4.01	-8.21	1.05	-3.6	-18.8	2.42
4	PCECTPI	-0.0787	-1.46	2.21	1.74	-18.7	3.24
5	GPDIC96	-1.38	-0.776	-21.8	-4.9	-7.96	-0.762
6*	OPHPBS	2	1.22	0.909	-4.25	-10.8	1.46
7	IMPGSC96	-2.46	-3.54	-8.62	-8.17	-16.4	-1.04
8	EXPGSC96	-0.772	-3.16	-4.76	-0.665	-18.2	-0.544
9	CBIC96	-2.28	-3.74	-1.1	-2.23	-13.6	-0.599
10	GCEC96	2.82	2.31	7.21	-0.532	-8.68	2.38
11	WASCUR	0.665	-0.569	-2.55	-4.29	-15.2	0.561
12	DIVIDEND	-15.3	-32.7	-16.6	-52.8	-59	-5.1
13	PSAVE	-9.92	-5.55	-5.32	-6.57	-21	-1.86
14*	DPIC96	-0.306	-3.37	-3.91	-6.04	-15.4	-0.894
15	GDPDEF	3.09	3.52	5.45	4.27	-13.6	5.15
16	ULCNFB	5.64	-0.159	0.772	0.835	-10.3	7.48
17	PRFI	-4.1	-4.32	-6.87	-6.74	-26.6	-2.57
18*	GSAVE	0.941	1.29	3.58	2.29	-0.888	0.524
19	CPIAUCSL	-0.477	-8.18	1.46	0.364	-14.4	4.1
20	FEDFUNDS	-20	-14.5	-12.5	-19.2	-37.3	-16.4
21	BOGNONBR	-9.05	-51.8	0.987	-56.6	-55.2	-55.9
22*	M2SL	-6.7	0.0888	-0.854	0.881	-13.4	-0.396
23	INDPRO	3.44	4.78	2.98	-1.74	-18.7	6
24*	UTL11	36.5	25.1	21.5	28.7	5.59	25
25	UNRATE	43.6	35.9	23.9	21.5	8.54	31.1
26*	HOUST	2.92	1.7	-1.04	0.38	-16.1	2.14
27	PPIFCG	-0.455	-11.2	3.36	-0.692	-15.4	-1.07
28	AHEMAN	15.6	13.3	8.29	6.06	-7.62	23.3
29	M1SL	-3.82	-0.655	-9.18	-6.15	-14.7	-1.44
30	PMCP	5.06	9.48	10.1	6.68	-12.8	8.84
31*	SP500	-1.82	-4.8	-2.45	-8.09	-32.5	-2.49
32	GS10	0.43	-0.28	-1.03	-5.29	-17.1	-2.62
33	EXUSUK	-0.29	-0.926	-21.2	-2.65	-19.5	-0.885
34	PAYEMS	3.52	4.1	2.97	-1.27	-16.6	3.22
35*	NAPMNOI	1.71	1.73	1.41	-4.5	-29.2	1.09
36	TB3MS	-1.63	-1.18	3.53	-1.97	-19.3	-1.07
37	BUSLOANS	-4.75	-6.62	-5.3	-8.41	-23.9	-5.11
38*	TOTALSL	-1.39	-0.791	-1.53	-4.66	-11.9	-1.42
39	AAA	-10.3	-3.88	-5.53	-7.88	-23.8	-7.57
	Mean	0.778	-1.928	-0.724	-3.967	-17.857	0.497
	t-stat.	0.070	-0.146	-0.081	-0.278	-1.413	0.040

See Table 4 of paper for model definitions. A \* means no break was detected for the series.  
Results computed from Table 1.

Table 10: RMSE ( $h = 4$ ) relative performance of lag orders on last sixty percent of sample (quarterly data)

	Series	$\frac{PPT12}{PPT41}$	$\frac{KP1}{KPA}$	$\frac{TVPI}{TVPA}$	$\frac{RO140}{RO440}$	$\frac{RO120}{RO420}$	$\frac{RECI}{RECA}$
1	GDPC96	-1.57	0.376	6.47	-7.47	-50.3	0.811
2	PINCOME	-1.17	-15.2	16.1	-0.539	-38.6	1.17
3	PCECC96	3.67	-2.94	0.665	-3.51	-45.1	2.53
4	PCECTPI	-1.65	-4.61	-1.73	3.9	-17.9	1.37
5	GPDIC96	-0.107	-1.25	-50.1	-14.3	-29.2	0.256
6*	OPHPBS	-0.45	-0.512	-0.395	-0.753	-3.98	0.134
7	IMPGSC96	-2.87	-1.95	-62.2	-7.5	-49.1	-0.686
8	EXPGSC96	0.161	-0.595	-31.1	-0.767	-51.7	-1.36
9	CBIC96	-17.3	2.23	-8.9	-5.04	-34.1	-2.1
10	GCEC96	0.112	1.05	3.94	2.41	-5.2	1.22
11	WASCUR	3.98	-6.65	-0.374	-3.32	-51.5	4.8
12	DIVIDEND	-14.1	-16.9	33.1	-92.2	-91.8	-0.254
13	PSAVE	-38.4	-39.4	-16.2	-28.1	-60	-3.96
14*	DPIC96	0.118	-2.14	-3.17	-5.61	-40.7	0.0248
15	GDPDEF	-2.25	-5.83	-3.75	10.7	-16.4	1.01
16	ULCNFB	-1.73	-3.04	-3.78	-2.37	-22.3	3.47
17	PRFI	-4.5	-4.99	-55.4	-8.18	-32.8	-3.9
18*	GSAVE	-1.14	-1.3	-0.459	-6.04	-10.2	-0.898
19	CPIAUCSL	-9.17	-6.76	-5.18	-0.12	-15.7	-0.202
20	FEDFUNDS	-16.9	-9.55	-4.98	-13.1	-24.5	-8.13
21	BOGNONBR	-8.5	-68.8	<u>3.84E+3</u>	-16.9	-68.7	-53.2
22*	M2SL	-26.3	-1.57	-1.65	3.15	-9.95	-1.54
23	INDPRO	1.83	13.3	0.626	9.61	-38.9	0.968
24*	UTL11	1.93	3.58	11.2	10	-39.8	3.52
25	UNRATE	34.1	22.4	13.1	10.6	-19.6	19.3
26*	HOUST	-4.84	-7.7	-2.97	1.67	-18.2	-7.99
27	PPIFCG	-4.1	-3.76	-2.71	-0.0154	-11.6	-5.44
28	AHEMAN	33.2	26.4	8.38	23	1.12	45.3
29	M1SL	-3.6	-0.515	-25.4	-6.59	-36.9	-0.918
30	PMCP	6.66	4.57	7.91	2.92	-11.1	3.53
31*	SP500	0.651	-0.22	-2.25	-6.13	-60.6	-0.677
32	GS10	-11.2	-5.77	-4.38	-15.4	-13.7	-6.33
33	EXUSUK	-1.19	-1.13	-14.4	-4.37	-38.7	-1.55
34	PAYEMS	0.701	3.82	-1.44	2.12	-41.9	-3.86
35*	NAPMNOI	2.92	2.16	6.42	-0.645	-35.1	2.86
36	TB3MS	-9.13	-7.81	-4.88	-9.92	-23.3	-4.76
37	BUSLOANS	-2.7	0.756	-2.14	-4.65	-35.6	-0.689
38*	TOTALSL	-3.36	-3.17	-1.17	-2.51	-17.7	-4
39	AAA	-14.6	-7.39	-7.01	-13.1	-5.16	-6.38
	Mean	-2.892	-3.867	<u>-5.532</u>	-5.104	-31.192	-0.681
	t-stat.	-0.237	-0.264	<u>-0.300</u>	-0.302	-1.547	-0.056

See Table 4 of paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. A \* means no break was detected for the series. Results computed from Table 2.

Table 11: RMSE ( $h = 1$ ) relative performance of lag orders  
on last sixty percent of sample (monthly data)

	Series	$\frac{PPT12}{PPT41}$	$\frac{KPI}{KPA}$	$\frac{TVPI}{TVPA}$	$\frac{RO110Y}{RO410Y}$	$\frac{RO15Y}{RO45Y}$	$\frac{RO13Y}{RO43Y}$	$\frac{REC1}{RECA}$
19	CPIAUCSL	-4.86	-9.42	-0.793	-1.34	-3.94	-6.48	-4.27
20	FEDFUNDS	-1.27	10.2	4.23	2.22	-13	-20.5	4.21
21	BOGNONBR	-9.13	3.88	-18.8	-46.3	-52	-51.8	-45.5
22	M2SL	-7.39	-3.11	0.53	2.3	-1.61	-4.23	1.1
23	INDPRO	3.49	0.475	-0.505	2.8	1.69	-2.48	1.26
24	UTL11	15.5	8.07	2.39	11.6	10.3	4.59	7.58
25	UNRATE	7.69	5.5	2.28	5.92	4.09	1.68	5.74
26*	HOUST	4.8	4.94	7.52	3.8	0.414	-1.69	5.05
27	PIIFCG	-3.85	-3.11	-2.82	-2.93	-4.48	-7.31	-1.9
28	AHEMAN	2.93	1.51	2.85	5.8	2.69	-0.151	5.19
29	M1SL	-4.91	-8.19	-7.7	-0.144	-10.6	-15.7	2.74
30	PMCP	3.67	4.89	3.89	5.25	3.69	0.0636	4.63
31*	SP500	-0.774	-1.82	-0.796	-1.63	-3.14	-5.16	-0.459
32	GS10	-0.127	9.82	5.82	5.69	2.76	0.355	6.33
33	EXUSUK	-0.14	-1.57	-0.707	-0.968	-4.49	-7.67	-0.168
34	PAYEMS	13.8	11.7	11.8	10.5	8.38	1.47	18.2
35*	NAPMNOI	-0.185	0.175	-0.389	-1.49	-6.6	-7.6	-0.0798
36	TB3MS	2.85	<u>1.24E+3</u>	3.62	3.19	-4.59	-10.6	4.31
37	BUSLOANS	-3.92	4.08	3.07	1.96	-0.817	-5.46	4.25
38	TOTALSL	11.9	91.1	9.74	11.2	6.33	4.09	13.8
39	AAA	4.97	<u>1.62E+3</u>	3.12	5.78	2.92	0.385	6.28
	Mean	1.504	<u>6.796</u>	1.262	0.871	-3.246	-6.729	1.601
	t-ratio	0.222	<u>0.320</u>	0.196	0.073	-0.251	-0.545	0.131

See Table 4 of the paper for model definitions. Results computed from Table 3. A \* means no break was detected for the series.

Table 12: RMSE ( $h = 12$ ) relative performance of lag orders on last sixty percent of sample (monthly data)

	Series	$\frac{PPT12}{PPT41}$	$\frac{KPI}{KPA}$	$\frac{TVPI}{TVPA}$	$\frac{RO110Y}{RO410Y}$	$\frac{RO15Y}{RO45Y}$	$\frac{RO13Y}{RO43Y}$	$\frac{REC1}{RECA}$
19	CPIAUCSL	-0.127	-1.19	1.16	1.7	-0.225	-3.4	-0.0734
20	FEDFUNDS	-49.1	1.56	-7.89	1.78	3.06	-35.5	-2.43
21	BOGNONBR	-1.15	-7.27	-92.2	-93.8	-95.7	-99.7	-93.8
22	M2SL	-78.6	-7.11	0.717	0.723	0.589	1.47	0.993
23	INDPRO	-1.47	-28.2	0.667	-3.62	-11.9	-88	0.116
24	UTL11	4.33	4.83	5.05	13.3	19.4	0.883	4.31
25	UNRATE	14.1	13.5	-0.131	21.7	20.1	-2.96	10.4
26*	HOUST	7.9	9.94	1.37	-6.86	-5.75	-31.9	10.8
27	PPIFCG	-1.47	-6.1	0.151	0.212	0.937	-2.9	-0.0991
28	AHEMAN	0.0829	-0.756	-0.366	0.994	0.742	0.404	0.0511
29	M1SL	-29.3	-70.5	-55.1	0.398	-69.3	-89.4	0.0891
30	PMCP	6.66	10.2	4.85	8	12.2	2.86	4.95
31*	SP500	-1.54	-4.19	-0.363	0.0359	-1.47	-8.14	-0.204
32	GS10	-37.9	-1.24	-4.27	-4.11	0.0232	7.07	-0.974
33	EXUSUK	-0.609	-10.2	-0.87	0.0859	-2.06	-70.7	0.115
34	PAYEMS	2.71	5.33	-8.78	-6.24	-31.1	-26.7	4.84
35*	NAPMNOI	1.12	1.5	-5.3	3.23	-18.8	-21.9	2.09
36	TB3MS	-27.5	192	-7.78	2.75	2.55	-82.6	0.619
37	BUSLOANS	-60.6	2.77	4.05	-1	-1.49	-4.04	2.71
38	TOTALSL	5.19	26.4	5.53	7.27	-1.53	-24.4	13.7
39	AAA	-62.6	153	-3.44	-2.61	6.1	10.2	-1.29
	Mean	-12.364	6.564	-7.975	-2.673	-8.986	-28.978	-2.090
	t-ratio	-0.480	0.138	-0.337	-0.119	-0.322	-0.800	-0.095

See Table 4 of the paper for model definitions. Results computed from Table 4. A \* means no break was detected for the series. .



Table 13: Average predictive likelihoods at horizon 1 on last sixty percent of sample (quarterly data)

series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO140	RO120	RO440	RO420	REC1	REC4	UC-SV	
1	GDPG96	0.422	0.402	0.425	0.416	0.452	0.353	0.439	0.437	0.435	0.44	0.419	0.385	0.354	0.356	0.446
2	PINCOME	0.364	0.363	0.363	0.371	0.344	0.343	0.377	0.382	0.36	0.378	0.36	0.332	0.368	0.385	0.38
3	PCECC96	0.431	0.439	0.442	0.468	0.454	0.397	0.485	0.495	0.497	0.506	0.509	0.464	0.434	0.446	0.469
4	PCECTPI	0.86	0.876	0.894	0.91	0.688	0.514	0.729	0.761	0.919	0.96	0.908	0.86	0.898	0.943	0.648
5	GPDIC96	0.257	0.245	0.267	0.261	0.309	0.277	0.312	0.272	0.292	0.294	0.284	0.265	0.251	0.251	0.313
6	OPHPBS	0.339	0.337	0.362	0.345	0.385	0.343	0.39	0.388	0.38	0.381	0.362	0.335	0.343	0.347	0.385
7	IMPGSC96	0.501	0.485	0.533	0.529	0.458	0.352	0.514	0.472	0.545	0.584	0.554	0.551	0.346	0.341	0.46
8	EXPGSC96	0.499	0.456	0.534	0.494	0.465	0.351	0.495	0.475	0.533	0.542	0.508	0.459	0.338	0.338	0.42
9	CBIC96	0.401	0.379	0.373	0.37	0.337	0.36	0.36	0.358	0.357	0.344	0.338	0.291	0.414	0.407	0.271
10	GCEC96	0.276	0.282	0.282	0.289	0.312	0.296	0.263	0.282	0.313	0.315	0.307	0.274	0.28	0.292	0.329
11	WASCUR	0.421	0.421	0.415	0.421	0.411	0.37	0.445	0.441	0.45	0.443	0.42	0.401	0.427	0.438	0.386
12	DIVIDEND	0.534	0.523	0.541	0.666	0.515	0.447	0.543	0.57	0.587	0.578	0.669	0.721	0.569	0.565	0.439
13	PSAVE	0.882	0.836	0.872	0.9	0.634	0.637	0.675	0.678	0.81	0.799	0.762	0.703	0.958	0.936	0.64
14	DPIC96	0.32	0.309	0.319	0.33	0.373	0.328	0.356	0.349	0.325	0.333	0.316	0.3	0.326	0.317	0.373
15	GDPDEF	1.19	1.12	1.29	1.18	0.868	0.471	0.894	0.915	1.24	1.26	1.26	1.14	1.05	1.09	0.73
16	ULCNFB	0.293	0.289	0.28	0.3	0.325	0.302	0.301	0.307	0.326	0.33	0.323	0.294	0.283	0.294	0.329
17	PRFI	0.372	0.343	0.41	0.386	0.415	0.314	0.425	0.347	0.408	0.436	0.393	0.401	0.298	0.295	0.383
18	GSAVE	0.283	0.285	0.286	0.292	0.287	0.291	0.302	0.302	0.282	0.276	0.291	0.266	0.287	0.293	0.286
19	CPIAUCSL	0.616	0.632	0.702	0.67	0.568	0.444	0.592	0.618	0.689	0.7	0.69	0.612	0.637	0.696	0.45
20	FEDFUNDS	1.78	2.06	2.21	1.72	0.993	1.08	1.26	1.21	1.72	1.74	2.22	2.25	1.24	1.29	0.574
21	BOGNONBR	21.9	21.2	21.8	21	3.76	4.17	3.28	2.78	24.1	24.7	22.7	21	27.6	26.4	1.16
22	M2SL	0.457	0.441	0.451	0.455	0.416	0.382	0.452	0.45	0.46	0.478	0.448	0.405	0.462	0.457	0.349
23	INDPRO	1.09	0.997	1.08	1.05	0.851	0.617	0.879	0.839	1.14	1.21	1.07	1.07	0.814	0.895	0.576
24	UTLL1	3.81	4.31	3.29	4.05	0.837	1.38	1.83	1.55	4.27	4.3	5.13	4.53	3.34	4.07	0.789
25	UNRATE	3.45	4.27	3.54	4.39	1.32	1.61	1.88	1.85	4.08	4.04	4.72	4.31	3.51	4.43	0.738
26	HOUST	3.3	3.35	3.33	3.45	0.697	1.24	1.64	1.32	3.77	3.93	3.74	3.45	3.35	3.5	0.809
27	PPIFCG	0.246	0.262	0.253	0.267	0.289	0.285	0.276	0.282	0.262	0.267	0.255	0.223	0.277	0.284	0.234
28	AHEMAN	0.572	0.555	0.606	0.615	0.491	0.42	0.538	0.583	0.634	0.637	0.669	0.591	0.443	0.559	0.405
29	M1SL	0.256	0.24	0.265	0.284	0.28	0.289	0.292	0.279	0.27	0.266	0.254	0.224	0.305	0.298	0.233
30	PMCP	3.59	3.74	3.56	3.88	1.34	0.45	1.75	1.81	3.53	3.34	3.95	3.61	3.68	3.92	0.832
31	SP500	2.01	1.91	2.04	1.93	1.14	1.06	1.23	1.21	1.97	1.92	1.88	1.65	2.06	1.99	0.758
32	GS10	1.9	1.84	1.85	2.17	1.01	1.14	1.3	1.3	2.2	2.22	2.15	2.03	2.17	2.19	0.678
33	EXUSUK	0.294	0.256	0.298	0.268	0.304	0.31	0.32	0.314	0.276	0.284	0.257	0.239	0.285	0.28	0.258
34	PAYEMS	1.11	1.08	1.17	1.11	0.811	0.564	0.945	0.85	1.19	1.26	1.15	1.21	0.888	0.947	0.538
35	NAPMNOI	5.36	5.53	5.39	5.66	1.68	0.489	2.25	2.17	5.5	5.35	5.45	5.47	5.49	5.72	1
36	TB3MS	1.81	2.27	1.97	1.63	1.03	1.11	1.32	1.26	1.92	1.91	2.33	2.35	1.55	1.63	0.6
37	BUSLOANS	0.892	0.852	0.884	0.888	0.642	0.563	0.72	0.713	0.903	0.88	0.834	0.802	0.926	0.917	0.489
38	TOTALSL	1.65	1.61	1.69	1.66	1.1	0.57	1.13	1.15	1.69	1.81	1.62	1.74	1.68	1.68	0.651
39	AAA	2.53	2.36	2.35	2.8	1.13	1.32	1.52	1.47	2.85	2.94	2.8	2.69	2.75	2.81	0.746

See Table 4 of the paper for model definitions.

Table 14: Average predictive likelihoods at horizon 4 on last sixty percent of sample (quarterly data)

series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO140	RO120	RO440	RO420	REC1	REC4	UC-SV	
1	GDPC96	0.375	0.328	0.386	0.374	0.431	0.345	0.406	0.39	0.403	0.411	0.377	0.335	0.34	0.333	0.448
2	PINCOME	0.312	0.304	0.324	0.327	0.306	0.326	0.346	0.341	0.341	0.334	0.326	0.283	0.329	0.351	0.372
3	PCECC96	0.397	0.371	0.458	0.402	0.44	0.389	0.459	0.434	0.46	0.46	0.428	0.387	0.418	0.415	0.463
4	PCECTPI	0.539	0.556	0.596	0.629	0.485	0.399	0.491	0.534	0.691	0.782	0.724	0.678	0.584	0.645	0.624
5	GPDIC96	0.247	0.226	0.256	0.249	0.303	0.277	0.301	0.185	0.284	0.277	0.266	0.227	0.251	0.248	0.306
6	OPHPBS	0.327	0.306	0.341	0.332	0.376	0.343	0.391	0.371	0.379	0.367	0.356	0.311	0.343	0.34	0.379
7	IMPGSC96	0.426	0.372	0.442	0.435	0.44	0.355	0.454	0.342	0.47	0.493	0.44	0.41	0.35	0.341	0.446
8	EXPGSC96	0.457	0.387	0.493	0.451	0.446	0.344	0.456	0.417	0.5	0.503	0.459	0.408	0.328	0.329	0.163
9	CBIC96	0.313	0.278	0.294	0.282	0.272	0.297	0.287	0.271	0.282	0.262	0.253	0.214	0.331	0.317	0.117
10	GCEC96	0.267	0.258	0.275	0.279	0.312	0.295	0.207	0.25	0.307	0.316	0.298	0.267	0.277	0.285	0.324
11	WASCUR	0.323	0.313	0.331	0.328	0.313	0.321	0.366	0.35	0.369	0.363	0.345	0.329	0.343	0.353	0.381
12	DIVIDEND	0.436	0.394	0.447	0.41	0.367	0.396	0.415	0.391	0.449	0.414	0.424	0.338	0.478	0.474	0.388
13	PSAVE	0.808	0.721	0.813	0.798	0.605	0.629	0.638	0.626	0.775	0.726	0.708	0.611	0.922	0.909	0.622
14	DPIC96	0.311	0.287	0.313	0.306	0.354	0.329	0.349	0.335	0.335	0.32	0.306	0.266	0.325	0.32	0.363
15	GDPDEF	0.739	0.764	0.817	0.875	0.595	0.387	0.584	0.674	0.884	1	0.989	0.924	0.647	0.792	0.71
16	ULCNFB	0.263	0.246	0.328	0.266	0.295	0.287	0.238	0.261	0.303	0.317	0.294	0.266	0.259	0.273	0.32
17	PRFI	0.282	0.239	0.295	0.277	0.333	0.273	0.326	0.216	0.309	0.334	0.293	0.288	0.25	0.243	0.355
18	GSAVE	0.272	0.26	0.282	0.278	0.285	0.289	0.291	0.282	0.277	0.262	0.267	0.231	0.282	0.284	0.285
19	CPIAUCSL	0.436	0.412	0.519	0.466	0.403	0.352	0.449	0.449	0.583	0.612	0.562	0.522	0.444	0.487	0.282
20	FEDFUNDS	0.651	0.533	0.668	0.554	0.398	0.511	0.534	0.417	0.657	0.621	0.58	0.574	0.572	0.529	0.281
21	BOGNONBR	14.6	14.2	18	18	3.8	4.02	2.05	1.13	20.3	20.5	19.7	16.8	23.6	24.7	0.737
22	M2SL	0.321	0.303	0.323	0.332	0.278	0.301	0.332	0.329	0.352	0.368	0.344	0.315	0.34	0.343	0.212
23	INDPRO	0.827	0.739	0.831	0.806	0.747	0.576	0.715	0.648	0.903	0.913	0.84	0.798	0.732	0.755	0.347
24	UTLL1	1.48	1.27	1.48	1.31	0.266	0.47	0.751	0.447	1.78	1.47	1.58	1.05	1.55	1.39	0.436
25	UNRATE	1.29	1.17	1.34	1.22	0.514	0.765	0.784	0.478	1.59	1.12	1.38	1.09	1.45	1.29	0.396
26	HOUST	1.5	1.25	1.62	1.36	0.203	0.409	0.696	0.434	1.68	1.7	1.64	1.53	1.71	1.44	0.459
27	PPIFCG	0.204	0.207	0.205	0.218	0.241	0.251	0.214	0.225	0.233	0.233	0.22	0.194	0.23	0.237	0.15
28	AHEMAN	0.501	0.485	0.554	0.58	0.465	0.397	0.522	0.551	0.586	0.626	0.636	0.564	0.374	0.532	0.287
29	M1SL	0.189	0.159	0.194	0.2	0.18	0.228	0.198	0.19	0.216	0.196	0.195	0.153	0.225	0.223	0.131
30	PMCP	1.71	1.63	1.72	1.72	0.727	0.4	0.906	0.779	1.79	1.62	1.71	1.38	1.87	1.82	0.498
31	SP500	1.76	1.65	1.83	1.78	1.15	1.02	1.12	1.07	1.83	1.76	1.68	1.47	1.91	1.88	0.491
32	GS10	0.796	0.616	0.814	0.842	0.535	0.627	0.59	0.517	0.987	1.07	0.863	0.865	0.995	0.88	0.381
33	EXUSUK	0.275	0.224	0.273	0.246	0.296	0.295	0.301	0.274	0.251	0.256	0.236	0.215	0.268	0.265	0.161
34	PAYEMS	0.646	0.55	0.676	0.596	0.48	0.447	0.565	0.438	0.684	0.702	0.595	0.666	0.58	0.545	0.29
35	NAPMNOI	3.35	3.3	3.51	3.51	0.999	0.44	1.37	1.17	3.55	3.31	3.28	2.65	3.67	3.68	0.616
36	TB3MS	0.65	0.576	0.661	0.637	0.43	0.547	0.568	0.448	0.719	0.672	0.657	0.556	0.679	0.661	0.298
37	BUSLOANS	0.551	0.508	0.56	0.542	0.43	0.449	0.456	0.421	0.557	0.574	0.488	0.494	0.59	0.576	0.286
38	TOTALSL	0.929	0.847	0.955	0.909	0.605	0.49	0.632	0.59	0.937	0.969	0.887	0.885	0.99	0.925	0.365
39	AAA	1.06	0.758	1.03	1.05	0.575	0.707	0.68	0.537	1.32	1.48	1.13	1.27	1.28	1.1	0.423

See Table 4 of the paper for model definitions.

Table 15: Average predictive likelihoods at horizon 1 on last sixty percent of sample (monthly data)

Series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO110Y	RO15Y	RO13Y	RO410Y	RO45Y	RO43Y	REC1	REC4	UC-SV	
19	CPIAUCSL	1.35	1.38	1.34	1.32	0.902	0.688	0.951	0.967	1.37	1.43	1.46	1.38	1.4	1.41	1.23	1.3	0.64
20	FEDFUNDS	12.2	13.7	9.5	8.77	2.18	2.16	2.78	2.72	10.3	11	12.9	13.4	14.6	16.1	5.52	6.02	0.949
21	BOGNONBR	38.8	38.6	20.4	20.2	4.61	5.17	3.99	3.52	40.8	40.3	41	40.8	39.8	38.7	49.4	48.9	1.14
22	M2SL	1.03	1.04	1.03	1.04	0.786	0.542	0.828	0.843	1.09	1.11	1.13	1.09	1.09	1.06	1.14	1.15	0.559
23	INDPRO	0.45	0.456	0.459	0.453	0.429	0.373	0.455	0.457	0.458	0.468	0.47	0.477	0.477	0.461	0.387	0.39	0.35
24	UTL11	4.93	5.3	4.13	4.5	0.936	1.38	2	1.58	5.04	5.09	5.13	5.58	5.5	5.3	4.11	4.43	0.829
25	UNRATE	15.6	16.3	15.7	16.4	2.43	2.54	3.66	3.28	17.1	16.9	17.3	17.7	17.3	17.2	15.6	16.4	1.09
26	HOUST	3.59	3.71	3.54	3.67	0.904	1.25	1.71	1.57	3.78	3.87	3.97	3.97	3.97	3.91	3.55	3.69	0.881
27	PIIFCG	0.527	0.506	0.514	0.489	0.472	0.417	0.478	0.485	0.501	0.528	0.522	0.503	0.515	0.49	0.477	0.485	0.367
28	AHEMAN	0.607	0.596	0.606	0.594	0.528	0.453	0.542	0.55	0.613	0.629	0.634	0.639	0.638	0.615	0.511	0.527	0.499
29	M2SL	0.508	0.481	0.494	0.483	0.447	0.437	0.493	0.498	0.534	0.527	0.537	0.532	0.516	0.498	0.571	0.588	0.405
30	PMCP	6.08	6.18	6.07	6.31	1.83	1.86	2.43	2.38	6.35	6.3	6.14	6.67	6.53	6.1	6.2	6.38	0.506
31	SP500	0.841	0.842	0.84	0.837	0.645	0.596	0.669	0.679	0.835	0.839	0.841	0.824	0.813	0.795	0.854	0.853	0.629
32	GS10	9.19	9.14	8.47	9.99	2.15	2.11	2.93	2.79	9.61	9.9	9.79	10	10.2	9.88	9.4	10.1	1.02
33	EXUSUK	1.23	1.24	1.25	1.32	0.805	0.795	0.864	0.889	1.22	1.22	1.22	1.22	1.2	1.18	1.34	1.35	0.6
34	PAYEMS	2.18	2.49	2.16	2.3	1.22	0.805	1.26	1.34	2.17	2.29	2.4	2.43	2.47	2.43	1.53	1.72	0.793
35	NAPMNOI	7.41	7.41	7.36	7.44	2.03	2.01	2.65	2.55	7.75	7.75	7.75	7.76	7.61	7.45	7.49	7.45	1.03
36	TB3MS	11.4	12.9	0.397	8.52	2.17	2.09	2.84	2.76	10.4	11	12.4	12.1	13.1	14.3	6.55	7.07	0.972
37	BUSLOANS	0.479	0.484	0.476	0.486	0.421	0.405	0.453	0.466	0.48	0.475	0.485	0.492	0.483	0.476	0.485	0.502	0.355
38	TOTALSL	0.839	0.884	0.477	0.882	0.684	0.508	0.685	0.735	0.802	0.843	0.879	0.888	0.894	0.897	0.762	0.86	0.529
39	AAA	12.4	12.4	0.926	12.9	2.24	2.41	3.2	2.95	12.5	13	13.3	13	13.4	13.2	11.9	13	1.07

See Table 4 of the paper for model definitions.

Table 16: Average predictive likelihoods at horizon 12 on last sixty percent of sample (monthly data)

Series	PPT12	PPT41	KP1	KP4	GK1P	GK1B	TVP1	TVP4	RO110Y	RO15Y	RO13Y	RO410Y	RO45Y	RO43Y	REC1	REC4	UC-SV	
19	CPIAUCSL	0.986	0.755	0.97	0.933	0.692	0.639	0.781	0.743	1.14	1.25	1.3	1.14	1.22	1.19	0.957	0.985	0.163
20	FEDFUNDS	1.17	0.816	1.49	1.27	0.632	0.952	0.635	0.435	1.8	1.61	1.51	1.48	1.56	1.62	1.41	1.24	0.22
21	BOGNONBR	13.6	11.4	17.4	15.8	4.68	5.1	2.3	0.446	38	36.2	36	37	34.3	33.2	46.1	45.8	0.319
22	M2SL	0.6	0.485	0.668	0.662	0.521	0.479	0.597	0.575	0.817	0.852	0.888	0.811	0.827	0.831	0.807	0.811	0.145
23	INDPRO	0.369	0.314	0.402	0.384	0.405	0.359	0.37	0.331	0.443	0.445	0.444	0.427	0.418	0.393	0.364	0.364	0.0899
24	UTL11	0.75	0.642	0.968	0.798	0.137	0.157	0.33	0.182	1.13	0.905	0.878	1.02	0.843	0.87	1.03	0.844	0.168
25	UNRATE	2.84	2.51	3.37	3.03	0.616	1.43	0.765	0.526	3.89	2.73	2.61	3.57	2.73	2.6	3.72	3.19	0.268
26	HOUST	0.982	1.05	1.28	1.44	0.224	0.183	0.493	0.416	1.3	1.38	1.72	1.56	1.6	1.83	1.36	1.52	0.193
27	PIIFCG	0.427	0.338	0.42	0.388	0.426	0.404	0.416	0.406	0.462	0.474	0.47	0.454	0.456	0.428	0.458	0.453	0.106
28	AHEMAN	0.511	0.439	0.557	0.525	0.531	0.449	0.52	0.497	0.591	0.608	0.609	0.585	0.591	0.567	0.507	0.505	0.508
29	M3SL	0.409	0.259	0.369	0.334	0.347	0.411	0.397	0.375	0.447	0.423	0.42	0.444	0.404	0.385	0.494	0.496	0.383
30	PMCP	1.4	1.32	1.67	1.68	0.58	1.03	0.632	0.524	1.75	1.61	1.51	1.74	1.56	1.37	1.81	1.79	0.502
31	SP500	0.718	0.655	0.78	0.767	0.634	0.586	0.636	0.617	0.808	0.8	0.803	0.795	0.772	0.74	0.831	0.824	0.63
32	GS10	1.58	1.17	2.04	2.11	0.959	1.23	0.722	0.559	2.47	2.66	2.63	2.17	2.43	2.47	2.43	2.24	0.253
33	EXUSUK	1.09	0.906	1.09	1.13	0.804	0.785	0.797	0.772	1.15	1.15	1.15	1.13	1.12	1.04	1.25	1.25	0.178
34	PAYEMS	1.2	1.14	1.3	1.47	0.98	0.762	0.917	0.734	1.55	1.51	1.6	1.59	1.49	1.47	1.27	1.29	0.175
35	NAPMNOI	2.77	2.73	3.3	3.3	0.624	1.46	0.93	0.787	3.48	3.26	3.03	3.43	3.15	2.77	3.5	3.5	0.25
36	TB3MS	1.09	0.973	0.331	1.49	0.7	1.04	0.672	0.486	1.95	1.75	1.48	1.62	1.65	1.49	1.66	1.53	0.232
37	BUSLOANS	0.3	0.271	0.311	0.32	0.27	0.328	0.301	0.289	0.338	0.338	0.359	0.338	0.337	0.334	0.343	0.349	0.0907
38	TOTALSL	0.507	0.465	0.312	0.563	0.409	0.439	0.459	0.435	0.555	0.589	0.606	0.578	0.564	0.551	0.545	0.596	0.124
39	AAA	1.84	1.37	0.552	2.71	1.02	1.44	0.767	0.538	3.21	3.65	3.67	2.97	3.44	3.54	3.14	2.87	0.27

See Table 4 of the paper for model definitions.

Table 17: APL ( $h = 1$ ) relative performance of break models on last sixty percent of sample (quarterly data)

Series	$\frac{PPT12}{KPI}$	$\frac{PPT12}{GK1P}$	$\frac{PPT12}{GK1B}$	$\frac{PPT12}{TVPI}$	$\frac{KPI}{GK1P}$	$\frac{KPI}{GK1B}$	$\frac{KPI}{TVPI}$	$\frac{GK1P}{GK1B}$	$\frac{GK1P}{TVPI}$	$\frac{GK1B}{TVPI}$	$\frac{PPT41}{KPI}$	$\frac{PPT41}{TVPI}$	$\frac{KPI}{TVPI}$	
1	GDPC96	-0.731	-6.66	19.5	-3.95	-5.97	20.4	-3.24	28	2.9	-19.6	-3.34	-7.97	-4.79
2	PINCOME	0.187	5.75	5.89	-3.65	5.56	5.7	-3.82	0.132	-8.89	-9.01	-2.15	-5.12	-3.03
3	PCECC96	-2.35	-5.06	8.57	-11	-2.78	11.2	-8.82	14.4	-6.22	-18	-6.26	-11.3	-5.4
4	PCECTPI	-3.77	25	67.5	18	29.9	74	22.6	33.9	-5.66	-29.6	-3.7	15.1	19.5
5	GPDIC96	-3.63	-16.9	-7.09	-17.6	-13.8	-3.59	-14.5	11.8	-0.893	-11.4	-6.2	-10	-4.05
6*	OPHPBS	-6.55	-12.1	-1.26	-13.2	-5.93	5.66	-7.14	12.3	-1.28	-12.1	-2.32	-13.3	-11.2
7	IMPGSC96	-6.08	9.24	42.5	-2.51	16.3	51.7	3.8	30.4	-10.8	-31.6	-8.38	2.77	12.2
8	EXPGSC96	-6.5	7.44	42.3	0.971	14.9	52.2	8	32.5	-6.02	-29	-7.78	-4.04	4.07
9	CBIC96	7.46	19.1	11.6	11.6	10.8	3.81	3.82	-6.32	-6.31	0.00335	2.47	5.9	3.35
10	GCEC96	-1.99	-11.4	-6.79	5.11	-9.63	-4.9	7.24	5.23	18.7	12.8	-2.33	-0.0389	2.34
11	WASCUR	1.46	2.62	13.8	-5.26	1.14	12.2	-6.63	10.9	-7.68	-16.8	-0.0513	-4.64	-4.59
12	DIVIDEND	-1.24	3.76	19.6	-1.61	5.07	21.1	-0.368	15.3	-5.17	-17.7	-21.5	-8.24	16.9
13	PSAVE	1.12	39.2	38.4	30.8	37.7	36.9	29.3	-0.571	-6.08	-5.54	-7.17	23.3	32.8
14*	DPIC96	0.19	-14.3	-2.41	-10.2	-14.5	-2.59	-10.4	13.9	4.76	-8.01	-6.4	-11.7	-5.65
15	GDPDEF	-7.99	36.9	152	33	48.7	174	44.5	84.3	-2.83	-47.3	-4.85	22.4	28.7
16	ULCNFB	4.71	-9.83	-3.01	-2.68	-13.9	-7.38	-7.05	7.56	7.94	0.349	-3.83	-5.96	-2.21
17	PRFI	-9.26	-10.3	18.4	-12.5	-1.17	30.5	-3.61	32	-2.46	-26.1	-11.2	-1.09	11.4
18*	GSAVE	-1.2	-1.55	-2.79	-6.48	-0.36	-1.61	-5.35	-1.26	-5.01	-3.8	-2.37	-5.83	-3.54
19	CPIAUCSL	-12.3	8.46	38.7	4.03	23.7	58.2	18.7	27.9	-4.08	-25	-5.66	2.28	8.42
20	FEDFUNDS	-19.5	78.9	65	40.8	122	105	74.9	-7.73	-21.3	-14.7	20.1	70.7	42.1
21	<u>BOGNONBR</u>	0.565	483	425	568	479	422	564	-9.9	14.6	27.2	1.02	662	654
22*	M2SL	1.35	9.97	19.7	1.27	8.51	18.2	-0.0776	8.89	-7.91	-15.4	-3.2	-2.15	1.08
23	INDPRO	0.955	27.9	76.5	23.8	26.7	74.8	22.7	38	-3.21	-29.8	-5.43	18.8	25.6
24*	<u>UTL11</u>	15.9	355	175	109	293	137	80.1	-39.6	-54.2	-24.2	6.36	178	161
25	<u>UNRATE</u>	-2.54	163	115	83.2	169	121	88	-18	-30.2	-14.8	-2.91	131	138
26*	<u>HOUST</u>	-0.681	374	166	102	377	168	103	-43.9	-57.5	-24.2	-2.69	155	162
27	PPIFCG	-2.73	-14.9	-13.6	-10.8	-12.5	-11.2	-8.25	1.5	4.84	3.29	-1.86	-7.08	-5.33
28	AHEMAN	-5.59	16.6	36.2	6.36	23.5	44.3	12.7	16.8	-8.79	-21.9	-9.69	-4.73	5.5
29	M1SL	-3.39	-8.55	-11.4	-12.2	-5.33	-8.34	-9.1	-3.17	-3.98	-0.834	-15.6	-14	1.82
30	PMCP	0.775	169	697	105	167	691	103	197	-23.8	-74.3	-3.65	106	114
31*	SP500	-1.29	76.3	90.3	63.7	78.6	92.8	65.8	7.97	-7.14	-14	-0.821	58.4	59.7
32	GS10	2.95	87.4	66.7	46.6	82	62	42.4	-11	-21.8	-12.1	-15.2	42	67.3
33	EXUSUK	-1.37	-3.33	-5.15	-8.14	-1.99	-3.83	-6.86	-1.88	-4.98	-3.16	-4.48	-18.5	-14.7
34	PAYEMS	-5.79	36.5	96.4	17.1	44.8	108	24.3	43.9	-14.2	-40.4	-1.95	27.4	30
35*	<u>NAPMNOI</u>	-0.449	219	995	139	220	1.00E+03	140	243	-25.2	-78.2	-2.37	155	161
36	TB3MS	-8.09	75.4	63.5	36.6	90.9	77.9	48.6	-6.79	-22.1	-16.5	38.8	79.6	29.4
37	BUSLOANS	0.931	39	58.5	24	37.7	57	22.8	14	-10.8	-21.8	-4.02	19.5	24.5
38*	TOTALSL	-2	50.4	190	46.3	53.5	196	49.2	93	-2.77	-49.6	-2.67	39.9	43.7
39	AAA	7.55	125	92.2	66.6	109	78.7	54.9	-14.5	-25.8	-13.3	-15.5	61.2	90.7
	Mean	-2.876	16.905	37.127	9.008	21.066	42.192	12.692	17.058	-5.288	-16.697	-3.408	9.136	12.684
	t-stat.	-0.556	0.560	0.785	0.422	0.615	0.820	0.530	0.717	-0.645	-1.172	-0.335	0.363	0.616

See Table 4 of the paper for model definitions. Data of underlined series are not used to compute means and standard deviations.

A \* means no break was detected for the series. Results computed from Table 13.

Table 18: APL ( $h = 4$ ) relative performance of break models on last sixty percent of sample (quarterly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVP1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVP1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVP1</u>	<u>GK1B</u> <u>TVP1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVP4</u>	<u>KP4</u> <u>TVP4</u>
1	GDPC96	-2.9	-12.9	8.84	-7.53	-10.3	-4.77	24.9	6.16	-15	-12.3	-15.9	-4.14
2	PINCOME	-3.72	1.82	-4.27	-9.87	5.76	-0.565	-6.38	-5.98	-11.5	-7.21	-11	-4.13
3	PCECC96	-13.3	-9.72	2.03	-13.4	4.11	17.7	-0.153	13	-4.09	-15.1	-7.68	-14.4
4	PCECTPI	-9.59	11.2	35.2	9.69	23	49.5	21.3	21.6	-1.33	-18.9	-11.6	4.04
5	GPDIC96	-3.44	-18.6	-10.8	-18.1	-15.7	-7.59	-15.2	9.56	0.518	-8.26	-9.43	21.7
6*	OPHPBS	-4.21	-13.1	-4.63	-16.2	-9.28	-0.438	-12.6	9.75	-3.61	-12.2	-7.75	-17.4
7	IMPGSC96	-3.47	-3.11	20.1	-6.21	0.374	24.4	-2.84	23.9	-3.2	-21.9	-14.5	8.7
8	EXPGSC96	-7.31	2.27	32.6	0.194	10.3	43	8.09	29.6	-2.03	-24.4	-14	-7.04
9	CBIC96	6.44	15	5.16	9.02	8.04	-1.21	2.42	-8.56	-5.2	3.67	-1.48	2.68
10	GCEC96	-3.19	-14.6	-9.77	28.9	-11.8	-6.8	33.1	5.67	50.9	42.8	-7.52	3.14
11	WASCUR	-2.31	3.09	0.734	-11.7	5.53	3.12	-9.57	-2.29	-14.3	-12.3	-4.51	-10.6
12	DIVIDEND	-2.57	18.6	10.1	4.94	21.7	13	7.71	-7.21	-11.5	-4.65	-4.01	0.54
13	PSAVE	-0.658	33.4	28.4	26.5	34.3	29.2	27.3	-3.77	-5.15	-1.44	-9.67	15.3
14*	DPIC96	-0.67	-12	-5.55	-11	-11.4	-4.92	-10.4	7.34	1.19	-5.73	-6.42	-14.6
15	GDPDEF	-9.52	24.3	91	26.4	37.4	111	39.8	53.7	1.75	-33.8	-12.7	13.3
16	ULCNFB	-19.8	-11	-8.4	10.3	11	14.2	37.5	2.87	23.9	20.4	-7.66	-5.81
17	PRFI	-4.34	-15.4	3.35	-13.5	-11.6	8.04	-9.6	22.2	2.22	-16.3	-13.7	10.7
18*	GSAVE	-3.55	-4.78	-6	-6.73	-1.27	-2.54	-3.29	-1.29	-2.05	-0.768	-6.31	-7.66
19	CPIAUCSL	-16	8.16	23.8	-2.96	28.8	47.4	15.6	14.4	-10.3	-21.6	-11.8	-8.25
20	FEDFUNDS	-2.64	63.6	27.3	21.9	68	30.7	25.2	-22.2	-25.5	-4.22	-3.86	27.8
21	<u>BOGNONBR</u>	-19	284	263	610	373	347	776	-5.53	85	95.9	-21.2	1.15E+03
22*	M2SL	-0.621	15.3	6.65	-3.34	16.1	7.32	-2.74	-7.53	-16.2	-9.37	-8.86	-7.94
23	INDPRO	-0.476	10.8	43.7	15.8	11.3	44.4	16.4	29.8	4.55	-19.4	-8.31	14
24*	<u>UTLL1</u>	-0.207	456	215	97	457	215	97.4	-43.4	-64.5	-37.4	-2.66	185
25	<u>UNRATE</u>	-3.56	151	68.5	64.4	160	74.7	70.5	-32.7	-34.4	-2.44	-3.95	145
26*	<u>HOUST</u>	-7.19	639	267	116	696	296	133	-50.3	-70.8	-41.2	-8.17	187
27	PPIFCG	-0.414	-15.3	-18.6	-4.56	-14.9	-18.3	-4.17	-3.95	12.6	17.3	-5.18	-8.03
28	AHEMAN	-9.54	7.73	26.1	-4.14	19.1	39.4	5.98	17.1	-11	-24	-16.5	-12
29	M1SL	-2.67	4.86	-17.1	-4.97	7.74	-14.9	-2.36	-21	-9.37	14.7	-20.6	-16.2
30	PMCP	-0.505	136	329	89.1	137	331	90.1	81.9	-19.8	-55.9	-5.36	109
31*	SP500	-3.77	52.9	72	57.3	58.9	78.7	63.5	12.5	2.91	-8.51	-7.14	54.7
32	GS10	-2.15	48.7	27	34.9	52	29.8	37.9	-14.6	-9.29	6.19	-26.9	19.2
33	EXUSUK	0.906	-6.99	-6.59	-8.44	-7.83	-7.42	-9.26	0.438	-1.55	-1.98	-8.69	-18.2
34	PAYEMS	-4.4	34.5	44.6	14.3	40.7	51.2	19.6	7.48	-15	-20.9	-7.61	25.6
35*	<u>NAPMNOI</u>	-4.46	235	662	144	251	697	155	127	-27.2	-67.9	-5.94	181
36	TB3MS	-1.6	51.3	18.8	14.4	53.7	20.7	16.2	-21.4	-24.4	-3.73	-9.63	28.7
37	BUSLOANS	-1.58	28.2	22.6	20.7	30.3	24.6	22.6	-4.4	-5.9	-1.57	-6.27	20.9
38*	TOTALSL	-2.72	53.6	89.6	47	57.9	94.9	51.1	23.4	-4.34	-22.5	-6.82	43.4
39	AAA	3.26	84.9	50.5	56.3	79.1	45.7	51.4	-18.6	-15.5	3.88	-27.6	41.1
Mean		-4.016	13.234	18.135	7.754	17.911	23.497	12.405	5.649	-3.200	-6.831	-10.128	5.469
t-stat.		-0.776	0.495	0.642	0.376	0.683	0.766	0.587	0.325	-0.233	-0.443	-1.713	0.280

See Table 4 of the paper for model definitions. Data of underlined series are not used to compute means and standard deviations.

A \* means no break was detected for the series. Results computed from Table 14.

Table 19: APL ( $h = 1$ ) relative performance of break models on last sixty percent of sample (monthly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVPE1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVPE1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVPE1</u>	<u>GK1B</u> <u>TVPE1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVPE4</u>	<u>KP4</u> <u>TVPE4</u>	
19	CPIAUCSL	1.05	49.5	96	41.9	48	94	40.4	31.1	-5.14	-27.6	4.71	42.8	36.4
20	FEDFUNDS	28.5	460	465	338	336	340	241	0.934	-21.7	-22.4	56.7	405	222
21	<u>BOGNOBR</u>	90.6	743	652	872	343	294	410	-10.9	15.3	29.3	91.5	996	472
22	M2SL	0.372	31.1	90	24.4	30.6	89.3	23.9	45	-5.12	-34.5	0.707	23.9	23
23	INDPRO	-2.08	4.74	20.7	-1.12	6.97	23.3	0.985	15.2	-5.59	-18.1	0.648	-0.117	-0.759
24	UTL11	19.4	427	257	146	341	199	106	-32.2	-53.2	-31	17.8	235	184
25	UNRATE	-0.852	541	514	327	547	519	330	-4.24	-33.4	-30.5	-0.497	397	399
26*	HOUST	1.3	297	188	110	292	184	107	-27.5	-47.2	-27.3	1.21	137	134
27	PPIFCG	2.49	11.5	26.2	10.1	8.82	23.1	7.39	13.1	-1.31	-12.8	3.58	4.45	0.831
28	AHEMAN	0.0756	14.8	33.9	11.9	14.8	33.8	11.8	16.6	-2.56	-16.4	0.326	8.23	7.88
29	M1SL	2.89	13.8	16.2	3.08	10.6	13	0.181	2.17	-9.39	-11.3	-0.508	-3.48	-2.99
30	PMCP	0.187	232	228	150	232	227	150	-1.41	-24.7	-23.6	-1.95	160	165
31*	SP500	0.171	30.5	41.1	25.8	30.3	40.8	25.6	8.1	-3.58	-10.8	0.505	23.9	23.3
32	GS10	8.51	327	335	213	294	301	189	1.84	-26.7	-28	-8.43	228	258
33	EXUSUK	-1.35	53.1	55.1	42.5	55.2	57.2	44.5	1.27	-6.9	-8.07	-6.26	39.1	48.3
34	PAYEMS 0.796	79.1	170	72.7	77.7	168	71.3	51.1	-3.57	-36.2	8.1	86.2	72.2	
35*	NAPMNOI	0.675	264	268	180	262	265	178	0.932	-23.2	-23.9	-0.485	190	191
36	TB3MS	2.77E+03	424	445	301	-81.7	-81	-86	4.06	-23.5	-26.5	51.1	366	209
37	BUSLOANS	0.739	13.9	18.4	5.9	13.1	17.5	5.12	3.95	-7.02	-10.6	-0.322	4	4.33
38	TOTALSL	76.1	22.7	65.2	22.6	-30.3	-6.17	-30.4	34.7	-0.073	-25.8	0.201	20.3	20
39	AAA	1.24E+03	452	413	286	-58.7	-61.6	-71.1	-7.1	-30	-24.7	-4.24	319	337
	Mean	0.515	30.204	56.760	23.716	29.609	56.000	23.118	18.759	-5.018	-18.637	1.149	22.898	21.249
	t-stat.	0.341	1.274	1.159	1.030	1.243	1.151	1.001	1.054	-2.109	-1.794	0.304	0.833	0.858

See Table Table 4 of the paper for model definitions. Data of underlined series are not used to compute means and standard deviations. A \* means no break was detected for the series. Results computed from Table 15.

Table 20: APL ( $h = 12$ ) relative performance of break models on last sixty percent of sample (monthly data)

Series	<u>PPT12</u> <u>KP1</u>	<u>PPT12</u> <u>GK1P</u>	<u>PPT12</u> <u>GK1B</u>	<u>PPT12</u> <u>TVE1</u>	<u>KP1</u> <u>GK1P</u>	<u>KP1</u> <u>GK1B</u>	<u>KP1</u> <u>TVE1</u>	<u>GK1P</u> <u>GK1B</u>	<u>GK1P</u> <u>TVE1</u>	<u>GK1B</u> <u>TVE1</u>	<u>PPT41</u> <u>KP4</u>	<u>PPT41</u> <u>TVE4</u>	<u>KP4</u> <u>TVE4</u>	
19	CPIAUCSL	1.6	42.3	54.2	26.2	40.1	51.8	24.2	8.35	-11.3	-18.2	-19.1	1.71	25.7
20	FEDFUNDS	-21.6	85.6	23.2	84.7	137	57.1	136	-33.6	-0.496	50	-36	87.7	193
21	<u>BOGNONBR</u>	-21.9	191	167	492	273	242	658	-8.2	103	122	-27.5	2.47E+03	3.44E+03
22	M2SL	-10.2	15.2	25.3	0.502	28.3	39.6	12	8.83	-12.7	-19.8	-26.7	-15.7	15.1
23	INDPRO	-8.23	-8.83	2.69	-0.371	-0.658	11.9	8.56	12.6	9.28	-2.98	-18.2	-5.12	16
24	UTLL1	-22.6	447	378	127	606	517	193	-12.7	-58.5	-52.5	-19.5	252	337
25	UNRATE	-15.6	361	98.9	271	446	136	340	-56.9	-19.5	86.7	-17.2	376	475
26*	<u>HOUST</u>	-23.3	339	437	99	472	601	159	22.4	-54.7	-63	-27	153	246
27	PPIFCG	1.57	0.199	5.64	2.61	-1.35	4.01	1.03	5.43	2.41	-2.87	-13	-16.8	-4.34
28	AHEMAN	-8.23	-3.74	13.7	-1.67	4.89	23.9	7.14	18.1	2.15	-13.5	-16.3	-11.6	5.61
29	M1SL	10.9	17.8	-0.412	2.96	6.26	-10.2	-7.14	-15.5	-12.6	3.39	-22.4	-31	-11
30	<u>PMCP</u>	-16.2	141	35.7	122	188	62	165	-43.8	-8.21	63.3	-21.7	151	221
31*	SP500	-7.97	13.3	22.5	12.9	23.1	33.1	22.7	8.13	-0.275	-7.78	-14.6	6.15	24.3
32	<u>GS10</u>	-22.8	64.4	28.2	118	113	66.2	183	-22	32.8	70.2	-44.9	108	278
33	EXUSUK	-0.241	35	38.4	36.3	35.3	38.7	36.6	2.52	0.942	-1.54	-20.1	17.4	46.9
34	PAYEMS -7.8	22.6	57.6	31	32.9	71	42.1	28.6	6.86	-16.9	-22.3	55.4	100	
35*	<u>NAPMNOI</u>	-16	344	90.6	198	429	127	255	-57.1	-32.8	56.6	-17.3	247	319
36	<u>TB3MS</u>	231	56.3	4.89	62.9	-52.7	-68.3	-50.7	-32.9	4.23	55.3	-34.8	100	207
37	BUSLOANS	-3.44	11	-8.37	-0.324	14.9	-5.11	3.22	-17.4	-10.2	8.79	-15.4	-6.29	10.8
38	TOTALSL	62.4	23.9	15.5	10.4	-23.7	-28.9	-32	-6.76	-10.9	-4.39	-17.4	6.71	29.2
39	AAA	234	80.6	27.8	140	-45.9	-61.7	-28.1	-29.2	33	87.9	-49.6	154	403
	Mean	-3.204	14.483	21.125	11.011	18.374	25.870	15.041	5.966	-2.543	-7.139	-18.810	-0.585	22.907
	t-stat.	-0.482	0.893	0.923	0.750	1.180	0.998	0.945	0.429	-0.304	-0.734	-4.477	-0.025	0.725

See Table 4 of the paper for model definitions. Data of underlined series are not used to compute means and standard deviations. A \* means no break was detected for the series. Results computed from Table 16.



Table 21: APL ( $h = 1$ ) relative performance of lag orders  
on last sixty percent of sample (quarterly data)

	Series	$\frac{PPT12}{PPT41}$	$\frac{KPI}{KPA}$	$\frac{TVPI}{TVPA}$	$\frac{ROI40}{ROI40}$	$\frac{ROI20}{ROI40}$	$\frac{REC1}{REC4}$
1	GDPC96	4.99	2.24	0.603	3.76	14.1	-0.41
2	PINCOME	0.182	-2.16	-1.35	-0.149	13.9	-4.34
3	PCECC96	-1.7	-5.64	-2.09	-2.41	9.08	-2.62
4	PCECTPI	-1.81	-1.73	-4.18	1.22	11.7	-4.76
5	GPDIC96	5.07	2.27	14.8	2.72	11.1	-0.0634
6*	OPHPBS	0.549	5.09	0.496	5.17	13.9	-1.35
7	IMPGSC96	3.3	0.768	8.89	-1.62	5.9	1.51
8	EXPGSC96	9.61	8.11	4.18	4.81	18	0.13
9	CBIC96	5.93	1	0.553	5.74	18.1	1.74
10	GCEC96	-2.18	-2.52	-6.97	1.82	14.9	-4.15
11	WASCUR	0.129	-1.37	0.787	7.18	10.5	-2.47
12	DIVIDEND	2.1	-18.8	-4.79	-12.3	-19.8	0.661
13	PSAVE	5.55	-3.11	-0.508	6.24	13.6	2.35
14*	DPIC96	3.69	-3.13	2	2.64	10.9	2.93
15	GDPDEF	6.03	9.64	-2.38	-1.77	11.2	-3.76
16	ULCNFB	1.35	-6.92	-2.07	0.809	12.4	-3.73
17	PRFI	8.4	6.11	22.6	4	8.81	1.02
18*	GSAVE	-0.788	-1.97	-0.0955	-3.28	3.88	-2
19	CPIAUCSL	-2.62	4.8	-4.26	-0.168	14.4	-8.56
20	FEDFUNDS	-13.9	28.5	4.44	-22.4	-22.9	-3.83
21	BOGNONBR	3.34	3.8	17.9	6.27	17.7	4.72
22*	M2SL	3.83	-0.829	0.325	2.53	18.2	1.09
23	INDPRO	9.2	2.3	4.77	6.06	13	-9.02
24*	UTL11	-11.6	-18.8	17.9	-16.8	-5.07	-18
25	UNRATE	-19	-19.3	1.95	-13.7	-6.24	-20.8
26*	HOUST	-1.53	-3.51	24.6	0.878	13.8	-4.36
27	PPIFCG	-6.21	-5.37	-2.35	2.64	19.5	-2.45
28	AHEMAN	3.06	-1.41	-7.67	-5.17	7.85	-20.8
29	M1SL	6.67	-6.76	4.44	6.65	18.5	2.29
30	PMCP	-4.11	-8.32	-3.38	-10.5	-7.52	-6.36
31*	SP500	4.92	5.41	1.53	5.02	16.1	3.44
32	GS10	3.26	-14.9	0.0067	2.1	9.36	-0.832
33	EXUSUK	14.8	11.1	1.79	7.34	18.9	1.79
34	PAYEMS	2.15	6.32	11.1	3.85	4.25	-6.21
35*	NAPMNOI	-3.01	-4.88	3.55	0.933	-2.22	-4.04
36	TB3MS	-20.1	20.6	4.98	-17.7	-18.6	-4.47
37	BUSLOANS	4.69	-0.446	0.897	8.2	9.68	0.926
38*	TOTALSL	2.47	1.77	-2.01	4.15	3.85	0.194
39	AAA	7.17	-15.8	3.64	1.96	9.3	-2.06
	Mean	0.869	-0.714	2.939	-0.084	8.052	-2.991
	t-stat.	0.120	-0.074	0.387	-0.011	0.749	-0.506

See Table 4 of paper for model definitions. A \* means no break was detected for the series. Results computed from Table 13.

Table 22: APL ( $h = 4$ ) relative performance of lag orders  
on last sixty percent of sample (quarterly data)

	Series	$\frac{PPT12}{PPT41}$	$\frac{KP1}{KP4}$	$\frac{TVP1}{TVP4}$	$\frac{RO140}{RO440}$	$\frac{RO120}{RO420}$	$\frac{REC1}{REC4}$
1	GDPC96	14.5	3.42	4.1	6.98	22.8	1.96
2	PINCOME	2.67	-1.06	1.32	4.74	18.2	-6.35
3	PCECC96	7.04	13.9	5.82	7.49	18.7	0.717
4	PCECTPI	-3.06	-5.22	-8.05	-4.58	15.3	-9.5
5	GPDIC96	9.36	2.57	62.5	6.73	22.1	1.12
6*	OPHPBS	6.81	2.87	5.32	6.55	18.1	0.894
7	IMPGSC96	14.6	1.49	32.8	6.87	20.2	2.67
8	EXPGSC96	17.9	9.34	9.34	9.06	23.1	-0.15
9	CBIC96	12.5	4.15	5.98	11.5	22.4	4.24
10	GCEC96	3.23	-1.39	-17.4	2.79	18.6	-2.97
11	WASCUR	3.19	0.862	4.45	6.92	10.5	-2.81
12	DIVIDEND	10.7	9.09	6.09	6.04	22.4	0.718
13	PSAVE	12	1.81	2.04	9.35	18.9	1.43
14*	DPIC96	8.58	2.29	4.2	9.39	20	1.56
15	GDPDEF	-3.29	-6.67	-13.3	-10.6	8.58	-18.4
16	ULCNFB	6.8	23	-8.81	3.02	19	-5.18
17	PRFI	18	6.5	51	5.73	16.1	2.75
18*	GSAVE	4.38	1.39	3.33	3.67	13.5	-0.627
19	CPIAUCSL	5.96	11.4	0.182	3.64	17.3	-8.86
20	FEDFUNDS	22.2	20.7	28.2	13.1	8.15	7.95
21	BOGNONBR	2.99	0.18	81.3	2.77	22.2	-4.5
22*	M2SL	5.89	-2.89	0.85	2.35	16.8	-0.912
23	INDPRO	12	3.17	10.3	7.42	14.4	-3.11
24*	UTL11	16.3	13.5	68.1	12	39.5	11.6
25	UNRATE	9.83	9.39	63.9	14.9	3.22	12.4
26*	HOUST	20.5	19.2	60.3	2.84	10.7	19.4
27	PPIFCG	-1.09	-5.83	-4.68	5.99	20.5	-3.08
28	AHEMAN	3.34	-4.59	-5.17	-7.84	10.9	-29.8
29	M1SL	18.8	-3.16	4.69	10.6	28	0.838
30	PMCP	5.37	0.233	16.3	4.78	17.6	2.63
31*	SP500	6.61	2.88	4.85	8.83	19.6	1.82
32	GS10	29.4	-3.36	14.3	14.3	23.4	13.1
33	EXUSUK	22.7	11.1	9.72	6.22	19.1	1.23
34	PAYEMS	17.4	13.4	28.9	15	5.47	6.53
35*	NAPMNOI	1.53	-0.046	16.9	8.37	24.9	-0.252
36	TB3MS	12.9	3.65	27	9.47	20.8	2.8
37	BUSLOANS	8.36	3.2	8.55	14.2	16.3	2.4
38*	TOTALSL	9.75	5.13	7.08	5.62	9.53	6.96
39	AAA	40.3	-1.6	26.6	16.3	16.3	17
	Mean	10.691	4.205	15.869	6.731	17.773	0.723
	t-stat.	1.209	0.575	0.661	1.183	2.711	0.084

See Table 4 of paper for model definitions. A \* means no break was detected for the series. Results computed from Table 14.

Table 23: APL ( $h = 1$ ) relative performance of lag orders on last sixty percent of sample (monthly data)

	Series	$\frac{PPT12}{PPT41}$	$\frac{KP1}{KP4}$	$\frac{TVP1}{TVP4}$	$\frac{RO110Y}{RO410Y}$	$\frac{RO15Y}{RO45Y}$	$\frac{RO13Y}{RO43Y}$	$\frac{REC1}{RECA}$
19	CPIAUCSL	-2.33	1.21	-1.68	-0.815	2.21	3.56	-4.7
20	FEDFUNDS	-11.1	8.38	2.31	-22.5	-24.4	-19.9	-8.2
21	BOGNONBR	0.519	1.03	13.3	0.192	1.29	5.86	0.973
22	M2SL	-1.41	-1.08	-1.78	-0.723	1.95	6.2	-0.547
23	INDPRO	-1.38	1.37	-0.382	-3.88	-1.81	2.05	-0.683
24	UTL11	-6.96	-8.23	26.5	-9.57	-7.46	-3.2	-7.36
25	UNRATE	-4.2	-3.86	11.5	-3.58	-2.31	0.614	-4.72
26*	HOUST	-3.27	-3.36	9.36	-4.79	-2.63	1.5	-3.77
27	PPIFCG	4.01	5.13	-1.3	-0.335	2.37	6.37	-1.62
28	AHEMAN	1.87	2.13	-1.47	-3.99	-1.33	2.99	-3.07
29	M1SL	5.63	2.14	-1.09	0.47	2.13	7.82	-2.95
30	PMCP	-1.66	-3.75	2.17	-4.84	-3.53	0.6	-2.82
31*	SP500	-0.0639	0.269	-1.56	1.35	3.16	5.88	0.136
32	GS10	0.472	-15.2	5.07	-4.26	-2.89	-0.892	-6.7
33	EXUSUK	-0.292	-5.25	-2.73	0.0911	1.13	3.56	-0.367
34	PAYEMS	-12.6	-6.29	-5.77	-10.8	-7.16	-1.03	-10.8
35*	NAPMNOI	-0.011	-1.16	3.6	-0.0537	1.92	3.97	0.456
36	TB3MS	-11.5	-95.3	3.03	-14	-16.4	-13.4	-7.34
37	BUSLOANS	-1.02	-2.06	-2.79	-2.5	-1.61	1.98	-3.38
38	TOTALSL	-5.08	-46	-6.87	-9.63	-5.71	-1.95	-11.4
39	AAA	0.0678	<u>-92.8</u>	8.44	-4.2	-2.82	0.409	-7.9
	Mean	-2.396	<u>-8.494</u>	2.755	-4.684	-3.043	0.619	-4.132
	t-stat.	-0.499	<u>-0.365</u>	0.359	-0.804	-0.455	0.095	-1.121

See Table 4 of the paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. Results computed from Table 15. A \* means no break was detected for the series.

Table 24: APL ( $h = 12$ ) relative performance of lag orders  
on last sixty percent of sample (monthly data)

Series	$\frac{PPT12}{PPTA1}$	$\frac{KP1}{KPA}$	$\frac{TVPI}{TVPA}$	$\frac{RO110Y}{RO410Y}$	$\frac{RO15Y}{RO45Y}$	$\frac{RO13Y}{RO43Y}$	$\frac{REC1}{RECA}$	
19	CPIAUCSL	30.5	3.96	5.16	0.353	2.94	8.98	-2.85
20	FEDFUNDS	43.7	17.3	46	21.9	3.13	-6.67	13.2
21	BOGNONBR	19.1	10.6	<u>416</u>	2.68	5.44	8.29	0.738
22	M2SL	23.7	0.99	3.84	0.772	3.02	6.81	-0.538
23	INDPRO	17.7	4.85	12.1	3.89	6.34	13.1	-0.0533
24	UTL11	16.8	21.4	<u>81.1</u>	10.5	7.39	0.907	22
25	UNRATE	13.5	11.3	45.4	9.09	-0.241	0.38	16.5
26*	HOUST	-6.65	-11.1	18.7	-16.3	-13.5	-5.87	-10.8
27	PIFCG	26.4	8.2	2.46	1.65	3.9	9.82	1.07
28	AHEMAN	16.3	6.13	4.61	0.971	2.98	7.5	0.36
29	M1SL	57.8	10.4	5.8	0.721	4.62	9.2	-0.328
30	PMCP	6.46	-0.534	20.6	0.598	3.34	10	0.988
31*	SP500	9.63	1.72	3.03	1.63	3.59	8.6	0.876
32	GS10	35.3	-3.35	29.2	13.7	9.75	6.53	8.65
33	EXUSUK	19.8	-4	3.25	1.41	3.28	9.85	0.15
34	PAYEMS	5.21	-11.3	24.8	-2.13	1.44	9.14	-1.8
*35	NAPMNOI	1.67	0.0656	18.2	1.32	3.63	9.45	-0.26
36	TB3MS	12.5	-77.8	38.2	20.1	5.97	-0.459	8.15
37	BUSLOANS	10.8	-2.94	4.18	0.0539	0.199	7.38	-1.66
38	TOTALSL	9.12	-44.5	5.44	-3.89	4.4	9.89	-8.61
39	AAA	35	<u>-79.6</u>	42.7	7.96	5.84	3.48	9.6
Mean		19.254	<u>-2.877</u>	<u>17.562</u>	3.666	3.212	6.015	2.637
t-stat.		1.285	<u>-0.129</u>	<u>1.112</u>	0.444	0.721	1.121	0.337

See Table 4 of the paper for model definitions. Trimmed means and standard deviations are underlined, as the corresponding trimmed observations. Results computed from Table 15. A \* means no break was detected for the series.