



25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39

**Abstract**

The paper develops an innovative risk evaluation methodology to address the challenges of multi-criteria decision-making problem of project evaluation and selection. The methodology considers Fuzzy Analytic Network Process (FANP) to incorporate the inter-dependencies of different risk factors, and Failure Mode and Effect Analysis to conduct the rating analysis of projects to develop the decision matrix. Finally, evaluation based on the distance from average solution compares alternative projects and reports the optimal solution. The proposed approach allows project managers to engage in the evaluation process and to use fuzzy linguistic values in the assessment process. A case study from the construction sector is selected to verify the efficacy of the proposed approach over other popular approaches in literature.

**Keywords:** Multi-criteria decisions; Failure mode and effect analysis; Fuzzy analytical network process; Risk assessment; Construction projects.

40 **Introduction**

41

42 In industrial projects, the risk assessment exercise has strategic importance, and can decide the success  
43 or failure of the project. Risk assessment involves the analysis of the whole project in order to reduce  
44 the impact of potential risk factors. It begins by identifying the potential risks that could influence the  
45 project. During the project planning phase, the project manager usually forms a team of experts and  
46 relevant stakeholders to assess the potential risk factors that could affect the successful completion of  
47 the project. The team uses techniques like brainstorming, discussions and tools such as flowcharts, root  
48 cause analysis, histogram and cause-effect analysis to release potential problems. Several tools are  
49 utilized by different risk management teams to develop the risk-breakdown structure and risk-profile.  
50 This paper is primarily focused on the risk evaluation and assessment of construction projects.

51 Scenario analysis is one of the most popularly used techniques for evaluating project risks. The project  
52 team evaluates the impact of each risk factor in terms of the probability of its occurrence and the  
53 influence on the project. A structured approach is needed to recognize potential / known failure modes  
54 at different levels of the project and investigate the effect on the next sub-system level (Sharma et al.  
55 2005). Failure Mode and Effect Analysis (FMEA) is considered as a fundamental tool and a part of the  
56 risk assessment methodology in several studies, and is established as one of the most reliable  
57 techniques (Dinmohammadi and Shafiee, 2013). This technique can help in understanding different  
58 failure modes within a system, evaluating their impacts, and deciding for corrective actions  
59 (Abdelgawad and Fayek, 2010). However, reported applications of this technique in the construction  
60 industry are limited (Andery et al., 2000; Nielsen, 2002). Evaluating different risk factors in  
61 construction projects is a complex task since the objective functions may change during the project life  
62 cycle (Dikmen et al. 2008). Further, Tserng et al. (2009) discussed an ontology based risk management  
63 framework for construction projects based on the project life cycle variance and covariance. However,  
64 FMEA provides a better approach to assess the severity of a potential risk, and by identifying the “risk  
65 priority” of a project, the key stakeholders can adopt a suitable risk management strategy to manage

66 potential risks (Safari et al. 2016). In practice, it is necessary to address technical, external and internal  
67 (organizational) issues through a risk breakdown structure. When developing this structure, it is  
68 important to reduce the chance of a risk event being missed, and to develop a comprehensive view of  
69 the project.

### 70 ***Research significance***

71

72 Multi-criteria decision-making (MCDM) techniques are amongst the most efficient approaches to  
73 evaluate risk factors and assist in real-life decision problems. In recent years, there is growing trend in  
74 integrating different MCDM approaches to develop hybrid techniques with better performance to  
75 address risk assessment problems in different projects (Chan and Kumar 2007; Chan et al. 2008; Chang  
76 2013; Prakash and Barua, 2016). It enables experts to be flexible in choosing relevant methods and  
77 creating integrated structures. Past literature (such as Gu and Zhu 2006; Tzeng et al. 2007; Yang and  
78 Tzeng, 2011; Liu et al. 2012; Liu et al. 2013) have provided further evidence to support the novelty of  
79 integrated and hybrid methods in order to take the advantage of two or more decision making  
80 approaches.

81 Moreover, Franceschini and Galetto (2001) presented a multi-expert MCDM model to analyze the risk  
82 preferences of failures in FMEA. In this model, risk factors were transformed as evaluation criteria,  
83 while failure modes were considered as different alternatives to be decided. This method contemplated  
84 each decision-making criterion as a fuzzy subset over the set of alternatives. Chin et al. (2009)  
85 discussed a FMEA model using the group-based evidential reasoning (ER) approach to collate diverse  
86 opinions and prioritize failure modes under uncertainties such as incomplete assessment, ignorance  
87 and intervals. Hu et al. (2009) developed a green component risk priority number to analyze the risks  
88 involved due to hazardous substances. In their study, Fuzzy analytic hierarchy process (FAHP) was  
89 used to identify the relative weights of risk factors. Then the green component risk priority number  
90 (RPN) was calculated for each component to assess the risks derived from them. In this study, the

91 application of fuzzy value FMEA in the context of risk evaluation is discussed, where FMEA forms  
92 an initial decision matrix for evaluation process.

93 The novelty of the proposed approach lies in the way it analyzes the anatomy of a project framework.

94 One of the important activities in decision modelling is to find logical ways to weigh different decision

95 attributes. In past literature, mostly Analytic hierarchy process (AHP), Delphi and entropy based

96 approaches are used to determine the weights of different influencing factors. However, in many

97 decision problems, the decision criteria are strictly dependent on each other. Analytic network process

98 (ANP) is the method that undertakes the interrelationship of risk factors in a ratio scale and aids in

99 overcoming the drawbacks of the decision levels and clusters (Tavana et al. 2016). The advantages of

100 ANP can be summarized as follows (Ignatius et al. 2016) : 1) ANP converts qualitative values into

101 numerical values for relative analysis of preferences, 2) It has a simple and intuitive structure, and 3)

102 it allows the participation of stakeholders and experts in the decision process.

103 In addition, risk evaluation in real life problems usually confronts low levels of information and

104 certainty. In the literature, the *fuzzy approach* is recognized as an effective tool for tackling uncertainty

105 stemming from inaccurate information (Wang et al. 2009). In multi-criteria decision-making problems,

106 where some of the criteria cannot be quantitatively represented, the fuzzy set theory can be helpful to

107 enable project assessors to express their linguistic preferences, and to convert those preferences into

108 numerical values for comparative analysis (Ho et al. 2012). He et al. (2015) studied the complexity of

109 mega construction projects in China using Fuzzy ANP methodology and argued that the methodology

110 can help decision makers to develop effective strategy for the project execution.

111 In this paper, an integrated decision-making approach, combining ANP and FMEA in a fuzzy

112 environment is proposed for the risk evaluation process. Very limited studies are available in the

113 literature which attempt to integrate FMEA and ANP with fuzzy variables for risk assessment.

114 Additionally, the ‘evaluation based on the distance from the average solution’ (EDAS) method is

115 adopted to compare alternative projects and rank them based on risk priority. A case study is also  
116 discussed to explain the implementation process of the proposed approach.

117 The rest of the paper is organized as follows: Next section discusses the proposed integrated approach  
118 (combining fuzzy set theory, ANP and FMEA) for risk assessment. Further, the case study and risk  
119 management methodology are presented, along with the analysis and findings. The managerial  
120 implications of the proposed approach is also discussed. At the end, paper concludes with a discussion  
121 on future research directions.

## 122 **Research Background**

123 This section discusses different methods for addressing multi-criteria decision-making problems.  
124 Particular attention has been given to approaches that are closely related to the integrated approach for  
125 risk evaluation proposed in this paper.

### 126 ***Fuzzy set theory***

127 In real world decision problems, there are many instances where decision makers are faced with  
128 multiple criteria when reaching to a decision. However, estimating the impact of these criteria on  
129 potential decision outcomes is cumbersome, and this sometimes results in extremely pessimistic or  
130 optimistic decisions being made. In every decision environment two types of systems can be proposed  
131 based on the availability of information. In white systems, all internal information is completely  
132 known, whereas in a black system, it is difficult to obtain any information and characteristics about the  
133 system (Zavadskas et al. 2010). Saaty (1980) introduced the analytic hierarchy process (AHP) to  
134 accurately represent the consensus of experts and is one of the most widely applied methods in practical  
135 applications. In his study, the geometric mean is used as the reference for triangular fuzzy numbers.  
136 Zadeh (1965) provided the fuzzy set theory for dealing with the uncertainty due to imprecise and vague  
137 information. The theory also allows mathematical operations and programming to be applied in the  
138 fuzzy domain. A fuzzy set is a class of objects with a continuum of grades of membership (degree of  
139 compatibility) (Peng and Selvachandran 2017). Such a set is characterized by a membership function,

140 which reflects the degree of compatibility assigned to each object with the grade of membership  
 141 between 0 and 1.

142 A triangular fuzzy number (TFN) is defined simply as  $(l, m, u)$  where parameters  $l$ ,  $m$ , and  $u$  represent  
 143 the smallest possible value, the most promising value and the largest possible value that denotes a  
 144 fuzzy event. The triangular fuzzy numbers  $\tilde{a}_{ij}$  can be established as:

145 
$$\tilde{a}_{ij} = (l_{ij}, m_{ij}, u_{ij}) \tag{1}$$

146 
$$l_{ij} \leq m_{ij} \leq u_{ij}, l_{ij}, m_{ij}, u_{ij} \in (0,1) \tag{2}$$

147 To establish the fuzzy pair-wise comparison matrix, the following procedure must be followed:

148 Suppose  $\tilde{A} = [\tilde{a}_{ij}]$  denotes a triangular fuzzy number for depicting the relative importance of criteria  $C_1$   
 149 ,  $C_2, \dots, C_n$ . In this way,  $\tilde{a}_{ij}$  represents a matrix constructed by triangular fuzzy numbers.

150 
$$\tilde{A} = [\tilde{a}_{ij}] = \begin{matrix} & C_1 & & & \\ & \begin{bmatrix} 1 & \tilde{a}_{12} & \dots & \tilde{a}_{1n} \\ \frac{1}{\tilde{a}_{12}} & 1 & & \tilde{a}_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{1}{\tilde{a}_{1n}} & \frac{1}{\tilde{a}_{2n}} & \dots & 1 \end{bmatrix} & & & \\ & C_2 & & & \\ & \vdots & & & \\ & C_n & & & \end{matrix} \tag{3}$$

151 Defuzzification is a technique to convert the fuzzy number into crisp real numbers and the procedure  
 152 of defuzzification is to locate the Best Non-fuzzy Performance (BNP) value (Tsaur and Wang 2007).  
 153 Methods such as the Mean-of-Maximum, the Centre-of-Area, and the  $\alpha$ -cut method are the most  
 154 common defuzzification approaches. In this research, fuzzy risk criteria are defuzzified with the help  
 155 of the Centre-of-Area method. This was chosen due to its simplicity and its less reliance on the personal  
 156 judgement of analysts. A defuzzified value of a TFN can be produced using the equation below:

157 
$$BNP = [(U_{ij} - L_{ij}) + (M_{ij} - L_{ij})] / 3 + L_{ij} \tag{4}$$

158  
 159 **Fuzzy ANP**

160 ANP is a popular MCDM technique useful to deal with interdependency of complex decision factors.  
 161 It helps decision makers (DMs) to define complex relationships among several decision levels and

162 their corresponding attributes (Saaty 1996). It helps in overcoming the drawbacks of AHP in  
163 addressing interrelationships issues among different decision levels using a super-matrix which detects  
164 the composite weights (Shyur, 2006; Kang et al. 2012).

165 By structuring the problem as an ANP model, the uncertain vague elements of matrix A used for pair-  
166 wise comparisons can be redefined by fuzzy membership functions reflecting the degree of  
167 compatibility for both the quantitative and the qualitative criteria. By pair-wise comparisons using a  
168 fuzzy membership function e.g. with triangular fuzzy numbers, the fuzzy pair-wise comparison matrix

169  $\tilde{A}$  with elements  $\tilde{a}_{ij}$ , is constructed where  $\tilde{a}_{ij} = (l_{ij}, m_{ij}, u_{ij})$  reflects the influence of element i over  
170 element j that could be a criterion/alternative in the network with lower ( $l_{ij}$ ), mean ( $m_{ij}$ ) and higher  
171  $u_{ij}$  values respectively. The value  $u_{ij} - l_{ij}$  could reflect the domain/degree of fuzziness. The greater

172 that  $u_{ij} - l_{ij}$  is, the fuzzier the degree is. When  $u_{ij} - l_{ij} = 0$ , the judgment is a non-fuzzy number (crisp  
173 value) with  $m_{ij}$  importance value. Contrarily, assuming that  $\tilde{A}$  is a positive  $n \times n$  reciprocal matrix,

174  $\tilde{a}_{ij} = \tilde{a}_{ij}^{-1} = (\frac{1}{u_{ij}}, \frac{1}{m_{ij}}, \frac{1}{l_{ij}})$  that represents influence of element j over element i with lower  $\frac{1}{u_{ij}}$ , mean  $\frac{1}{m_{ij}}$

175 , and higher  $\frac{1}{l_{ij}}$  values respectively. As a result, the fuzzification increases the complexity of the

176 computation for synthesis judgments based on the fuzzy elements  $a_{ij}$ s. To be able to evaluate a fuzzy

177 ANP model through standard pair-wise comparisons, the fuzzy values are standardized into a single-  
178 pattern fuzzy set dealing with both linguistic and/or quantifiable criteria (Abdi, 2009). Accordingly,

179 the importance weights are defined with five triangular fuzzy sets:  $\hat{1}, \hat{3}, \hat{5}, \hat{7}, \hat{9}$  with their

180 corresponding lower, mean, and upper values defined in equation (5) and represented in **Table 1** (Abdi  
181 and Labib, 2004).



$$\tilde{a}_{ji} = \begin{cases} \hat{1} & ; \in (1, 1, 3) \\ \hat{x} & ; \in (x-2, x, x+2) \\ \hat{9} & ; \in (7, 9, 9) \end{cases} \quad (5)$$

<< Insert Table 1 about here >>

The fuzzy range of ( $\hat{1}, \hat{3}, \hat{5}, \hat{7}, \hat{9}$ ) are used to express linguistic preferences for evaluation criteria in terms of Equal (EQ), Low (L), Medium (M), High (H), and Very High (VH) as decision linguistic variables (**Table 1**), respectively. EQ can also represent equal to very low importance. If criterion ( $c_i$ ) is assigned one of the fuzzy numbers above when compared with criterion ( $c_j$ ), then  $c_j$  has the reciprocal value when compared with  $c_i$ . To simplify the weighting process, the priority values are put in a reciprocal comparison bar for each pair of attributes with respect to a criterion/alternative. For example, if value 5 is assigned on the right-hand side criterion ( $c_j$ ), then criterion  $c_j$  is more important than  $c_i$  with a moderate degree. Similarly, if value 5 is assigned on the left criterion ( $c_i$ ), then the criterion  $c_i$  is more important than  $c_j$  with a moderate degree (Abdi and Labib, 2004).

The synthesized fuzzy degree of criterion  $i$  influenced by criterion  $j$ , where  $i, j = 1, 2, \dots, n$ , each with a triangular fuzzy number  $\tilde{a}_{ij}$  in an ANP structure, can be derived from formula (5). In the ANP with a ( $n \times n$ ) super-matrix, in which any element can influence on another element based on the influence flow from a component/cluster to another component/cluster, or from a component to itself (inner dependency loop), the number of elements influencing on or being influenced by criterion  $i$  could be up to  $n$  elements. In the fuzzy environment, the comparison ratios  $\tilde{a}_{ij}$  are represented by the membership functions that indicate the degree of compatibility/possibility.

206 **Fuzzy FMEA**

207 Failure mode and effects analysis (FMEA) is a risk measurement tool, which is used in various  
208 engineering and management problems such as project risk management. Accordingly, a risk priority  
209 number (RPN) is constructed for measuring key risk elements and prioritizes several risky  
210 problems/projects, for which the largest RPN corresponds to the riskiest problem/project being  
211 considered. The purpose of this section is to explain the logic and shortcomings of RPN values.

212 In the FMEA, risk value is evaluated by grading the data according to key risk elements: 1) severity of  
213 effect (S), 2) frequency of occurrence (P), and 3) detectability (D). The multiplied sum of these figures  
214 produces the risk priority number. Failure mode and effects analysis extends the risk priority matrix  
215 that includes RPN for each project:

$$216 \quad RPN = \text{Severity} \times \text{Probability} \times \text{Detection} \quad (6)$$

217 In typical RPN problems, a rating of 1 to 10 on each scale will be assigned to each risk element, with  
218 10 being severe, very likely to occur, and impossible to detect. These ratings are then multiplied  
219 together to obtain RPN values, which are used to assess the projects. The idea is that the problem with  
220 the highest *RPN* value is the critical one (with a highest priority) that needs to be focused on. However,  
221 there are two logical difficulties with calculating the RPN. As argued by Wheeler (2011),  
222 multiplication of the RPN elements is nonsense; with having assigned a range of 1 to 10 to each  
223 element, RPN varies from 1 to 1,000 with only 125 possible values, which are not uniformly distributed  
224 between 1 and 1,000. In the typical RPN, the three elements are assumed to be of the same importance  
225 while being given crisp values ranging from 1 to 10. RPN values gained from multiplication of the  
226 three elements are not meaningful because each value is an interval scale and not a ratio scale as a  
227 requirement for multiplication. However, in a ratio scale, the values can be ordered with consistently  
228 identical distance between two values (the distance between 1 and 3 is the same of the distance between  
229 5 and 7, and etc.), and with an absolute zero point (starting from zero rather than 1).

230 To overcome the shortcomings of using certain value and illogical multiplication, the elements can be  
 231 considered as linguistic values ranging from Very Low (VL), Low (L), Medium (M), High (H), and  
 232 Very High (VH) respectively. By using RPN linguistic scores, 125 problem descriptions ( $5^3$ ) can be  
 233 obtained; each with the 5 options above e.g. a risk score of HMH (High, Medium High) reflect values  
 234 of (Severity, Occurrence, Detectability) respectively. So far, all the values for RPN elements are  
 235 assumed to be crisp ranging in [1,5]. Conversely, the elements can be considered as criteria with fuzzy  
 236 number as described earlier. Therefore, the fuzzy range of  $(\hat{1}, \hat{3}, \hat{5}, \hat{7}, \hat{9})$  can be used to express  
 237 linguistic priorities. Using fuzzy number ranging from  $\hat{1}, \hat{3}, \hat{5}, \hat{7}$ , to  $\hat{9}$ , each problem description can  
 238 be seen as a fuzzy linguistic value, and a ratio fuzzy scale can be achieved by a synthesized fuzzy  
 239 number. Adopting from the extent analysis (Chang, 1996), the synthesized result for criterion  $i$  will  
 240 remain fuzzy as shown in formula (7).

$$241 \quad S_i = \sum_{j=1}^n \tilde{a}_{ij} \otimes \left( \sum_{i=1}^n \sum_{j=1}^n \tilde{a}_{ij} \right)^{-1} = (l_{si}, m_{si}, u_{si}); \quad i, j = 1, 2, \dots, n \quad (7)$$

$$242 \quad V(M \geq L) = \sup_{x \geq y} [\min \mu_L(x), \mu_M(y)] \quad (8)$$

243 Where  $V$  is the possibility of  $M \geq L$  and a pair  $(x,y)$  exists, If  $x \geq y$  and  $\mu_L(x) = \mu_M(y) = 1$ , then  $V(M$   
 244  $\geq L) = 1$  where  $V$  is the possibility distribution. Considering  $M$  and  $L$  are convex fuzzy numbers

245  $(l, m, u)$  and  $L = (1, 3, 5)$  and  $M = (3, 5, 7)$ :

$$246 \quad V(M \geq L) = 1 \quad \text{as } m_M = 5 \text{ and } \geq m_L = 3 \quad (9)$$

$$247 \quad V(L \geq M) = \mu_L(d) = D = 0.5 \quad (10)$$

248  $D$  is equal to  $\mu(d)$ , and  $d$  is the intersection point of two sides of triangles of fuzzy number  $M$  and  $L$ .

249 we have:

$$250 \quad \text{Line 1: } p1: (5,0), p2: (3,1) \text{ then } (Y-0)/(1-0) = (X-5)/(3-5) \text{ then } -2Y = X-5 \quad (11)$$

$$251 \quad \text{Line 2: } p1: (3,0), p2: (5,1) \text{ then } (Y-0)/(1-0) = (X-3)/(5-3) \text{ then } 2Y = X-3 \quad (12)$$

252 Value 'd' can be found by equalizing the simultaneous equations by adding equations for Line 1 and  
253 line 2, therefore:

254  $0 = 2X - 8$ , then  $X = 4$  so,  $d = 4$ , and therefore by substituting  $d$  in Line 1 or Line 2:

255  $Y = D = 0.5$ , therefore:

256  $V(L \geq M) = 0.5$

257 Interestingly, the degree possibility for  $M \geq L$  equals 1 whereas it is 0.5 for  $L \geq M$ .

258 We also have:

259  $V(L \geq M, H, VH) = V(\hat{1} \geq \hat{3} \text{ and } \hat{5} \text{ and } \hat{7} \text{ and } \hat{9}) = \text{Min}(V(L \geq M), V(L \geq H) \text{ and } V(L \geq VH) = V(L \geq M) = V(\hat{1} \geq \hat{3}) = 0$  (13)

261 That means the fuzzy number  $\hat{1}$ (Low) cannot be greater than fuzzy values (M, H, VH) at once as the  
262 degree possibility is zero.

263 The synthesized fuzzy number for comparison matrix  $\tilde{A}$  can be derived using formula (14):

264  $\text{Fuzzy RPN} = \text{Fuzzy Severity (S)} * \text{Fuzzy Occurrence (P)} * \text{Fuzzy Detection (D)}$  (14)

265 To avoid the logical failure of the multiplication of the three risk elements Severity (S), Occurrence  
266 (P), and Detection (D) in obtaining RPN the linguistic scales can be replaced for ranking projects with  
267 regards to their risks and the impacts. As shown in **Table 2**, the risk values can be classified to 5 fuzzy  
268 numbers which reflect the linguistic scales with fuzzy range possibility for each scale. By ordering of  
269 these three risk aspects, a fuzzy RPN value for each project with combination of three fuzzy numbers  
270 for three risk elements is allocated. All the possible combinations will be 125 ( $= 5*5*5$ ) with different  
271 scores which can be ordered based on their centred average in a descending order to see the most  
272 critical (risky) projects at the top of the table. In this approach, equal importance is given to each risk  
273 element.

274 The final rating will range from extremely high (EXH), very high (VH), high (H), medium (M), low  
275 (L) and very low (VL). The combinations of the three elements in a descending order from EXH, VH,

276 to H are presented in Appendix 1. combinations from 125 possible combinations are ranked from H to  
277 EXH. The same combination of elements is defined for medium (M), low (L) and very low (VL). The  
278 table presented in Appendix 1 facilitates the collection of data related to pair-wise comparison of risks  
279 factors and sub-factors from the group of experts and decision makers.

280

### 281 ***Evaluation based on distance from average solution (EDAS) method***

282 In order to solve the MCDM problems, the alternatives must be ranked by computing the distance of  
283 the possible solutions from the ideal and worst solutions using the EDAS tool (Ghorabae et al. 2015).  
284 The most preferred alternative will have the lowest distance from ideal solution and the highest distance  
285 from the nadir solution in VIKOR and TOPSIS methods (Yazdani and Payam, 2015). However, in the  
286 proposed approach, the best alternative is related to the distance from the average solution (*AV*). This  
287 method does not need to calculate the ideal and the nadir solution, instead two measures dealing with  
288 the desirability of the alternatives will be computed. The first measure is the positive distance from  
289 average (PDA), and the second is the negative distance from average (NDA). These measures can  
290 illustrate the difference between each solution (alternative) and the average solution. As suggested by  
291 Ghorabae et al. (2016), the evaluation of alternatives is made according to the higher values of PDA  
292 and lower values of NDA.

293

294 << *Insert Table 2 about here* >>

295

296 The EDAS ranking score can be obtained as follows (Ghorabae et al. (2016):

297 *Step 1* – Select the most relevant attributes, which describe the alternatives for the specific decision  
298 problem.

299 Step 2 - Let  $x_{ij}$  be the performance rating of  $i^{th}$  alternative  $A_1, A_2, \dots, A_n, (i = 1, 2, \dots, n)$  with respect to the  
 300  $j^{th}$  criterion  $C_1, C_2, \dots, C_m (j = 1, 2, \dots, m)$ . Form the interval decision matrix  $X$  and weight of each  
 301 criterion  $W$  as follows:

$$302 \quad X = [x_{ij}]_{n \times m} = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1m} \\ x_{21} & x_{22} & \dots & x_{2m} \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ x_{n1} & x_{n2} & \dots & x_{nm} \end{bmatrix}, \quad (15)$$

$$303 \quad W = [w_1, w_2, \dots, w_m]$$

304 For  $(i = 1, 2, \dots, n)$  and  $(j = 1, 2, \dots, m)$

305 where  $w_j$  is the weight of criterion  $j^{th}$

306 Step 3 - The average solution with respect to all criteria must be determined as shown following the  
 307 formula:

$$308 \quad AV_j = \frac{\sum_{i=1}^n x_{ij}}{n}; \quad (16)$$

309 Step 4 - The positive distance from average (PDA) and the negative distance from average (NDA)  
 310 matrices can be calculated as:

$$311 \quad PDA_{ij} = \frac{\max(0, (x_{ij} - AV_j))}{AV_j} \quad (17)$$

$$312 \quad NDA_{ij} = \frac{\max(0, (AV_j - x_{ij}))}{AV_j} \quad (18)$$

313 In this way  $PDA_{ij}$  and  $NDA_{ij}$  represent the positive and negative distance of the  $i^{th}$  alternative from the  
 314 average solution in terms of the  $j^{th}$  criterion for the lower level of decision matrix, respectively.

315 Step 5 – Compute the weighted summation of the positive and negative distances from the average  
 316 matrix:

317 
$$SP_i = \sum_{j=1}^m w_j PDA_{ij} \quad (19)$$

318 
$$SN_i = \sum_{j=1}^m w_j NDA_{ij} \quad (20)$$

319 *Step 6* – Find the normalized values of  $SP_i$  and  $SN_i$  for all alternatives as follows:

320 
$$NSP_i = \frac{SP_i}{Max_i(SP_i)} \quad (21)$$

321 
$$NSN_i = 1 - \frac{SN_i}{Max_i(SN_i)} \quad (22)$$

322 *Step 7* – Calculate the appraisal score  $AS$  for all alternatives as:

323 
$$AS = \frac{1}{2}(NSP_i + NSN_i), \quad (23)$$

324 where  $0 \leq AS \leq 1$

325 *Step 8* - Rank the alternatives according to the decreasing values of the appraisal score ( $AS$ ). The  
326 alternative with the highest  $AS$  is the best choice.

327

### 328 **Problem context and proposed approach**

329 Projects' failure could be the result of poor planning of risk management and a lack of proper risk  
330 analysis (Kerzner, 2001). On the other hand, risk management could be seen as a cost-containment tool  
331 rather than a systematic process and technique for handling various aspects of the projects (Zwikael  
332 and Globerson, 2006). It has been shown that risk management incorporates cost, time, quality and  
333 scope are unavoidably connected and interdependent ( Lavender 2013, Mantel et al. 2011; Chan et al.  
334 2004). Therefore, if the risk management is considered for controlling cost, then it is similarly  
335 concerned with controlling time, quality and scope that could result in successful project delivery.

336 In the past, clients or contractors rarely formally requested risk analysis for their projects (even for  
337 infrastructural projects) (Akintoye and MacLeod 1997). An independent investigation undertaken by

338 British Airports Authority (BAA) indicates that any UK construction project with over £1 billion in  
339 value for construction over 10 years, in addition to all international airport projects completed in the  
340 previous 15 years, had not been delivered on time, on budget, safely or met their specified quality  
341 standards (Lowe 2013). Due competitive environment for contracting projects, customers are now able  
342 to get involved with project, insisting contractors to assume higher levels of risk through various types  
343 of contracts: Lump sum, Guaranteed Maximum Price (GMP), or Not-To-Exceed price (NTE). With  
344 increasing project size, complexity and competition, the management of risks, particularly at the early  
345 stage of the project is becoming an ever more important challenge (Maytorena et al. 2007). Therefore,  
346 it is crucial to improve both organizational and project performance with developing risk assessment  
347 methodologies that can be mutually accepted as a critical component of successful project delivery  
348 (PwC, 2013; KPMG and PMI 2012).

349 The proposed model integrates analytical network process (ANP) and, failure mode and effect analysis  
350 (FMEA) with fuzzy approach in order to develop a meaningful and practical solution to the project  
351 risk evaluation problem. These three methods have been integrated to complete three tasks: ANP to  
352 weight decision criteria, FMEA to shape the performance-rating matrix (decision table), and the  
353 outputs of these two methods are used as input to EDAS (third method) which produces the ranking of  
354 the projects considering the risk factors. Each method has its particular advantage, and the intelligent  
355 integration of them provides a robust methodology for risk evaluation.

356 The proposed model to evaluate construction projects based on risk variables can be presented in  
357 three phases (**Figure 1**):

358 **Phase I** - In the first phase, a team of experts will define the risk attributes, decision alternatives and  
359 level of complexity. In this phase, the proposed integrated model will be explained to the experts.

360 **Phase II** - The second phase based on the ANP principles represents the relationship and interaction  
361 among the decision variables and constructs the pairwise comparison matrix (shown in **Figure 2**). The  
362 fuzzy ANP utilizes this matrix to estimate weights of the decision factors and sub-factors. Further in



363 this phase, the initial risk matrix for alternative projects is decided through a new fuzzy FMEA scoring,  
364 Three decision makers (DMs) present their views over projects considering risk determination values.  
365 The fuzzy FMEA procedure is explained earlier in the paper. The outputs of this phase will be the input  
366 (weights of the attributes and performance rating of projects) of phase III.

367

368 << *Insert Figure 1 about here* >>

369

370 **Phase III** - At last, in the third phase, the EDAS method (as described earlier) evaluates projects and  
371 ranks them from the best to worst. Comparisons with other MCDM methods and sensitivity analysis  
372 are performed in order to test the consistency and stability of the results.

373

#### 374 **Implementation of the proposed approach**

375 In this section, the implementation process of the proposed approach is discussed. Six projects  
376 considered in this study are medium to large scale construction projects. These projects are related to  
377 building water reservoirs and dams in one of the European countries. Due to the lack of rain and  
378 decreasing water resources, the need to construct water reservoirs and dams to improve water  
379 availability for agriculture is one of the important issues in this country. All of these projects are from  
380 different regions of the country with varying degree of resources availability, weather conditions,  
381 geographical features and political situations. Assessing and measuring the risks in developing these  
382 construction projects are vital for the successful completion of the projects. Also for planning purpose,  
383 it is important to understand the risks involved due to limited resources available for these projects.  
384 The risk evaluation of these construction projects in this study is based on measuring the risks with the  
385 help of the proposed decision analysis model and then rate them according to different risk parameters.  
386 The proposed approach is implemented in consultation with the practitioners and planners to  
387 understand the real -life challenges in risk evaluation of constructions projects.

388

<< Insert Figure 2 about here >>

389  
390

391 **Phase I** - This study examines the hierarchical risk breakdown structure (RBS) for risk assessment of  
392 construction projects. Organizations use RBS in conjunction with Work Breakdown Structure (WBS)  
393 to help management team and eventually analyze risks (Mantel et al. 2011). For the six construction  
394 projects, specific risks must be identified and analyzed. In this phase, ANP tool is used to produce the  
395 weights of risk factors and sub factors. ANP is an applied tool in MCDM which considers the inter-  
396 relationship among risk elements using pairwise comparison. The ANP network (**Figure 2**) presents  
397 the criteria and sub-criteria for the risk assessment of the construction projects. Different decision  
398 variables for risk evaluation in construction projects are identified based on past literature such as  
399 Antuchevičiene et al. (2010) and Zavadskas et al. 2010). However, these factors and sub-factors are  
400 later verified during the interviews with the key decision makers in the construction projects. The risk  
401 factors in this study are classified into three groups : a) *Technical*, b) *External* and c) *internal /*  
402 *organisational* risk factors. The *technical* factors include: C<sub>1</sub>) construction requirements; C<sub>2</sub>)  
403 technology; C<sub>3</sub>) complexity and interfaces; C<sub>4</sub>) quality and C<sub>5</sub>) cost; *external* factors include C<sub>6</sub>)  
404 subcontractors and suppliers; C<sub>7</sub>) economic and market; C<sub>8</sub>) weather; and C<sub>9</sub>) political; and *internal*  
405 factors include C<sub>10</sub>) resources; C<sub>11</sub>) funding; and C<sub>12</sub>) project site.

406 Later on, the pairwise comparisons among different decision factors and sub-factors are performed,  
407 which help to get global weighs of each factors and sub-factors to decide the final risk assessment of  
408 the projects. The project risk ratings are determined using fuzzy linguistic variables.

409

410 **Phase II** - In order to obtain the weights of factors and sub-factors using ANP, the pairwise comparison  
411 matrix must be performed between factors and sub-factors. To shape the global weight matrix for all  
412 the factors, primarily pairwise comparison must be made between each factor and sub-factors based  
413 on the defined inter-dependency.

414 For the FMEA process, three experts / decision makers (DM) deliver their judgments for six projects  
415 regarding each decision variable. These decision makers were selected based on their wide experience  
416 in managing large scale construction projects. The decision makers selected for this study for providing  
417 pairwise comparison of different risk factors and sub-factors have more than 20 years of working  
418 experience. **Appendix 1** shows the fuzzy FMEA pre-defined values (FMEA reference rating scales).  
419 In this phase the experts carefully consider probability, severity and number of detection parameters  
420 using fuzzy linguistic variables. For example DM<sub>1</sub> explains for project 1 corresponding C<sub>2</sub> the severity  
421 (S), probability of happening (O) and detection are (1,1,3), (3,5,7) and (1,1,3), respectively. **Appendix**  
422 **2** presents the information of projects expressed by decision experts. Then linguistic variables are  
423 translated to fuzzy values and also the defuzzification process is established.

424

425 With the help of the decision makers, pairwise comparisons are performed for the three factors to find  
426 independent weights of factors (shown in **Table 3**). To design Table 3, experts are asked to compare  
427 three factors to realize their influence. This task is done using reference scales in Table 1. After that  
428 comparison between each factor is performed with regard to the single factor. Table 3 is developed  
429 based on the experts' judgment over the importance of different risk factors. For example, as the  
430 external factors were identified 5 times more important than technical factors. Therefore, the priority  
431 of technical factors over external are 0.2 times. After the pair wise comparison of each factor, sum of  
432 each column is obtained. Then, each element is divided by the sum of the column. Finally, average of  
433 each row produces the weights which are seen in the last column. Similar process is followed for each  
434 pairwise matrix of the decision variables.

435

436

<< *Insert Table 3 about here* >>

437

438 In ANP, when decision system contains factors and sub-factors, pairwise comparisons must be  
439 performed in order to find importance (weight) of one over another. The weight of different factors are  
440 obtained through multiplication of factors inter-dependence vector and the vector of factors  
441 interrelationship with respect to each one. As there are three key decision factors ( Technical, External,  
442 and Internal) in this study, four vectors (one for inter dependence and one each for three factors) should  
443 be multiplied to calculate the final weight of the factor (as shown in equation 24).

$$444 \quad w_{factors} = \begin{bmatrix} 0.667 & 0.245 & 0.525 \\ 0.15 & 0.428 & 0.334 \\ 0.183 & 0.327 & 0.142 \end{bmatrix} \times \begin{bmatrix} 0.102 \\ 0.686 \\ 0.211 \end{bmatrix} = \begin{bmatrix} 0.347 \\ 0.38 \\ 0.273 \end{bmatrix} \quad (24)$$

445  
446 Similarly, the pair-wise comparison of 12 sub-factors are performed to find the local-weight of each  
447 sub-factor. It is then multiplied to the weight of the corresponding risk factor ( Technical, External, or  
448 Internal - as calculated in equation 24) to generate the global weights of each sub-factors. Finally, the  
449 normalised weights of each sub-factor are presented in Table 4. The normalized global weights of sub-  
450 factors are utilized in the project evaluation process by EDAS in Phase III. EDAS needs the weights  
451 of decision factors and sub-factors to find the final ranking of the projects.

452 << Insert Table 4 about here >>

453  
454  
455 **Phase III** - This section ranks projects using the EDAS method. The aggregated defuzzified matrix  
456 (Appendix 3) is used as the initial decision matrix for the EDAS method. The process of ranking  
457 alternative projects using EDAS first involves developing the positive distance from average (PDA)  
458 and negative distance from average (NDA) matrices as described in equation 17 and 18 (See Appendix  
459 4). Then, the weighted summation of the positive distance (SP) and negative distance (SN) from the  
460 average matrix are obtained (as shown in equation 19 and 20). Further, the normalised values of SP  
461 and SN for all alternatives (NSP and NSN) are calculated. Finally the appraisal scores (AS) of each  
462 alternative are computed according to equation 23. The project with highest appraisal score is

463 considered as the riskiest project. The summary results obtained by the EDAS method and the ranking  
464 of the projects are presented in **Table 5**.

465 << *Insert Table 5 about here* >>  
466

467 The ranking of projects based on EDAS shows this arrangement:

468 Project 4 > Project 6 > Project 1 > Project 3 > Project 5 > Project 2

469 Therefore, it is observed that project 4 is the riskiest project based on the judgments of experts and  
470 corresponding risk factors. Project 2 is considered as the least risky project among all. It is observed

471 Appendix 3), that Project 4 has the maximum value regarding the criteria “subcontractors and  
472 suppliers” (C<sub>6</sub>) which is the most important criterion among all. Also, this project has considered as

473 one of the low cost project among others. The results are confirmed through observing the initial data.

474 In this phase, to check the consistency and the accuracy of the obtained ranking outcomes, a  
475 comparison of the proposed approach with other popular methods is conducted. EDAS ranking scores

476 are compared with other MCDM tools such as SAW, TOPSIS, VIKOR, COPRAS and WASPAS. The  
477 consistency of the proposed method is evident among the ranking orders of the different methods.

478 **Table 6** shows the comparative results, and tests the stability of the model.

479

480

481 << *Insert Table 6 about here* >>  
482

483

484

484 Further, sensitivity analysis is conducted on the decision parameters to study the changes in the ranking

485 of the projects. To conduct the sensitivity analysis, relative preferences of experts over the risk factors

486 and sub-factors are altered and weights of decision variables are replaced by random weights. The

487 performance of proposed approach has been then compared and analyzed for each scenario. Each

488 scenario is represented by a “set” of alternative sub-factors weights. In total, 12 sets of weights are

489 generated to analyze the impact on project ranking (as shown in figure 3). **Table 7** shows the weight  
490 replacement scenarios for six projects with respect to the decision variables. Figure 3 shows that  
491 significant changes were observed in the ranking orders of the projects. Based on the sensitivity  
492 analysis outcomes, it could be concluded that on average, Project 1, Project 4, and Project 6 are the top  
493 3 riskiest projects.

<< *Insert Table 7 about here* >>

<< *Insert Figure 3 about here* >>

498 **Discussion**

499 The approach proposed for the risk evaluation of projects in this study embraces multi-level internal,  
500 external and organizational factors. The proposed decision framework can help to provide suggestions  
501 and improvements for practitioners to improve their decision making capabilities. Generally the  
502 interrelationships among different levels of project evaluation are not considered by project managers.  
503 This partially blocks the decision-making process from its most accurate route and enhances the  
504 complexity of the computations. This paper essentially insists on the importance of taking into  
505 consideration such interrelationships and shows how it can be done though utilizing ANP. The  
506 proposed approach offers the additional opportunity for practitioners to express their comparisons  
507 using fuzzy linguistic values with ANP.

508 This paper introduces a new FMEA structure utilizing fuzzy linguistic variables. The paper argues that  
509 this novel pattern offers a unique anatomy, which increases judgment's preciseness and facilitates  
510 efficient decision-making procedure. The FMEA rating classification easily converts solid fuzzy values  
511 to the meaningful and informative codes that are exhibited in **Appendix 1**. Moreover, it gives reliable  
512 combination of fuzzy scales to constant alarm codes (EXH as extremely high, VH as very high). This

513 will decrease the complexity of the judging process and allow the DM to perform a better analysis of  
514 the existing project.

515

### 516 **Conclusion and future research direction**

517

518 Project risk management is increasingly becoming challenging due to the number of variables and  
519 parameters with quantitative and qualitative characteristics. Uncertainty and impreciseness have  
520 emerged as influential factors at the core of risk evaluation computations. Mitigating complexity,  
521 interrelationship and transaction among risk variables is a serious concern for project managers. In this  
522 paper, a new integrated model of combining FANP and FMEA in a fuzzy decision-making  
523 environment has been proposed to evaluate the potential risks of projects considering internal /  
524 organizational, external and technical factors. The ANP with fuzzy linguistic scales is applied in order  
525 to obtain relative weights of the sub-criteria and to resolve internal dependencies. In addition, failure  
526 mode and effect analysis (FMEA) has been conducted to comprehensively measure fundamental  
527 factors such as the likelihood, severity and detection of potential risk for each project. Explaining and  
528 rating these factors by verbal codes is crucial. Therefore, the utilization of fuzzy linguistic scales is  
529 appropriate to deal with such vagueness and uncertainty in comparing the priority of variables. The  
530 proposed FMEA coding improves the decision process and increases the flexibility and efficiency of  
531 risk evaluation. In this paper, decision makers offered their opinions regarding FMEA codes and then  
532 through defuzzification process, the consequences assessed by them provided the main decision matrix  
533 for MCDM process. The proposed framework provides a robust decision-making tool which can aid  
534 project managers and investors to analyze different risk factors in multiple levels of a project.

535 The paper contributes in developing the body of knowledge in MCDM field. A new feature is the  
536 integration of the EDAS method in to the risk evaluation process – something that was not considered  
537 in past studies. However, the study is highly reliant on the experts' opinions over the priority of the

538 decision variables. Depending on the dimensions and levels of decision, a large pairwise comparison  
539 needs to be carried out and, in such cases; fatigue is a serious concern that may cause some reliability  
540 issues. In this situation, involving more decision makers in the research could be advantageous.  
541 The proposed integrated MCDM model for risk evaluation can be applied to other decision-making  
542 problems such as supply chain risk assessment, productivity and ergonomic risk evaluation in human  
543 resource management studies. Although, ANP is a method which analyzes the interactions among  
544 decision variables, it cannot recognize the direction of that interaction. In order to tackle that  
545 shortcoming future research could expand the scope of this study by addressing the inter-relationships  
546 among the criteria using Decision Making Trial and Evaluation Laboratory (DEMATEL) or  
547 interpretive structural modeling (ISM) (Hashemi et al. 2015). Another potential improvement in the  
548 project evaluation exercise could be the consideration of the risk of investment and, the satisfaction of  
549 stakeholders and external customers. Integration of MCDM methods with Quality Function  
550 Deployment (QFD) could be considered in future research to address this issue. Moreover, due to the  
551 increasing awareness of environmental and social issues, incorporating ecological and sustainability  
552 factors in the risk measurement model could be included in the proposed model.

553

#### 554 **Data Availability Statement**

555 Data generated or analyzed during the study are available from the corresponding author by request.



556 **References**

- 557 Abdi, M.R.(2009). Fuzzy multi-criteria decision model for evaluating reconfigurable machines,  
558 International Journal of Production Economics, 117(1), 1–15.
- 559 Abdi, M.R. and Labib, A.W. (2004). Feasibility study on the tactical-design justification of  
560 Reconfigurable Manufacturing Systems (RMSs) using fuzzy AHP, International Journal of  
561 Production Research, 42(15), 3055-3076.
- 562 Abdelgawad, M., & Fayek, A. R. (2010). Risk management in the construction industry using  
563 combined fuzzy FMEA and fuzzy AHP. Journal of Construction Engineering and  
564 Management, 136(9), 1028-1036.
- 565 Andery, P. R., Vanni, C., & Borges, G. (2000). Failure Analysis Applied To Design Optimisation.  
566 In the proceedings of the Annual Conference Of International Group For Lean  
567 Construction (Vol. 8).
- 568 Antucevičiene, J., Zavadskas, E. K., & Zakarevičius, A. (2010). Multiple criteria construction  
569 management decisions considering relations between criteria. Technological and Economic  
570 Development of Economy, 16(1), 109-125.
- 571 Akintoye, A. S., & MacLeod, M. J. (1997). Risk analysis and management in construction.  
572 International Journal of project management, 15(1), 31-38.
- 573 Chan, A. P., Scott, D., & Chan, A. P. (2004). Factors affecting the success of a construction project.  
574 Journal of construction engineering and management, 130(1), 153-155.
- 575 Chan, F.T.S. and Kumar, N. (2007). Global supplier development considering risk factors using fuzzy  
576 extended AHP-based approach. Omega: The International Journal of Management Science,  
577 35(4) 417-431.
- 578 Chan, F. T.S., Kumar, N., Tiwari, M. K., Lau, H. C. W., and Choy, K. L. (2008). Global supplier  
579 selection: a fuzzy-AHP approach. International Journal of Production Research, 46(14), 3825-  
580 3857.

- 581 Chang, D.Y., 1996, Theory and methodology: application of the extent analysis method on fuzzy AHP.  
582 European Journal of Operational Research, 95, 649–655
- 583 Chang, K. L. (2013). Combined MCDM approaches for century-old Taiwanese food firm new product  
584 development project selection. *British Food Journal*, 115(8), 1197-1210
- 585 Chin, K. S., Wang, Y. M., Poon, G. K. K., & Yang, J. B. (2009). Failure mode and effects analysis  
586 using a group-based evidential reasoning approach. *Computers & Operations Research*, 36(6),  
587 1768-1779.
- 588 Dikmen, I., Birgonul, M. T., Anac, C., Tah, J. H. M., & Aouad, G. (2008). Learning from risks: A tool  
589 for post-project risk assessment. *Automation in construction*, 18(1), 42-50.
- 590 Dinmohammadi, F., & Shafiee, M. (2013). A fuzzy-FMEA risk assessment approach for offshore wind  
591 turbines. *International Journal of Prognostics and Health Management*, 4, 59-68.
- 592 Fallahpour, A., Amindoust, A., Antucheviciene, J., Yazdani, M. (2016). Nonlinear Genetic-Based  
593 Model for supplier selection: A comparative study, *Technological and Economic Development  
594 of Economy*, 22(4), 532-549
- 595 Franceschini, F., and Galetto, M. (2001). A new approach for evaluation of risk priorities of failure  
596 modes in FMEA. *International Journal of Production Research*, 39(13), 2991-3002.
- 597 Ghorabae, M. K., Zavadskas, E. K., Olfat, L., and Turskis, Z. (2015). Multi-Criteria Inventory  
598 Classification Using a New Method of Evaluation Based on Distance from Average Solution  
599 (EDAS). *INFORMATICA*, 26(3), 435-451.
- 600 Ghorabae, M. K., Zavadskas, E. K., Amiri, M., & Turskis, Z. (2016). Extended EDAS Method for  
601 Fuzzy Multi-criteria Decision-making: An Application to Supplier Selection. *International  
602 Journal of Computers Communications & Control*, 11(3), 358-371.
- 603 Gu, X. and Zhu, Q., 2006. Fuzzy multi-attribute decision-making method based on eigenvector of  
604 fuzzy attribute evaluation space. *Decision Support Systems*, 41(2), pp.400-410.

- 605 Hashemi, S. H., Karimi, A., & Tavana, M. (2015). An integrated green supplier selection approach  
606 with analytic network process and improved Grey relational analysis. *International Journal of*  
607 *Production Economics*, 159, 178-191.
- 608 He, Q., Luo, L., Hu, Y. and Chan, A.P. (2015). Measuring the complexity of mega construction projects  
609 in China—A fuzzy analytic network process analysis. *International Journal of Project*  
610 *Management*, 33(3), 549-563.
- 611 Ho, W., He, T., Lee, C. K. M., & Emrouznejad, A. (2012). Strategic logistics outsourcing: An  
612 integrated QFD and fuzzy AHP approach. *Expert Systems with Applications*, 39(12), 10841-  
613 10850.
- 614 Hu, A. H., Hsu, C. W., Kuo, T. C., & Wu, W. C. (2009). Risk evaluation of green components to  
615 hazardous substance using FMEA and FAHP. *Expert Systems with Applications*, 36(3), 7142-  
616 7147.
- 617 Ignatius, J., Rahman, A., Yazdani, M., Šaparauskas, J., & Haron, S. H. (2016). An integrated fuzzy  
618 ANP–QFD approach for green building assessment. *Journal of Civil Engineering and*  
619 *Management*, 22(4), 551-563.
- 620 Isaac, S., & Navon, R. (2009). Modeling building projects as a basis for change control. *Automation*  
621 *in Construction*, 18(5), 656-664.
- 622 Kang, H. Y., Lee, A. H., & Yang, C. Y. (2012). A fuzzy ANP model for supplier selection as applied  
623 to IC packaging. *Journal of Intelligent Manufacturing*, 23(5), 1477-1488.
- 624 Kerzner, H. R. (2011). *Project management metrics, KPIs, and dashboards: a guide to measuring and*  
625 *monitoring project performance*. John Wiley & Sons.
- 626 Lavender, S. A., Mehta, J. P., & Allread, W. G. (2013). Comparisons of tibial accelerations when  
627 walking on a wood composite vs. a concrete mezzanine surface. *Applied ergonomics*, 44(5), 824-  
628 827

- 629 Liu, H. C., Liu, L., Liu, N., & Mao, L. X. (2012). Risk evaluation in failure mode and effects analysis  
630 with extended VIKOR method under fuzzy environment. *Expert Systems with*  
631 *Applications*, 39(17), 12926-12934.
- 632 Liu, H. C., Liu, L., & Liu, N. (2013). Risk evaluation approaches in failure mode and effects analysis:  
633 A literature review. *Expert Systems with Applications*, 40(2), 828–838.
- 634 Lowe, D. (2013) *Commercial Management: Theory and Practice*, John Wiley & Sons.
- 635 Mantel Jr, S. J., Meredith, J. R., Shafer, S. M., & Sutton, M. M. (2001). *Project management in practice*.  
636 Wiley.
- 637 Maytorena, E., Winch, G. M., Freeman, J., & Kiely, T. (2007). The influence of experience and  
638 information search styles on project risk identification performance. *IEEE Transactions on*  
639 *Engineering Management*, 54(2), 315-326
- 640 Nielsen, A. (2002). Failure modes and effects analysis (FMEA) used on moisture problems. *Indoor*  
641 *Air*, 38-43.
- 642 Peng, X., and Selvachandran, G. (2017). Pythagorean fuzzy set: state of the art and future directions,  
643 *Artificial Intelligence Review*, 1-55.
- 644 Prakash, C., and Barua, M. K. (2016). A combined MCDM approach for evaluation and selection of  
645 third-party reverse logistics partner for Indian electronics industry. *Sustainable Production and*  
646 *Consumption*, 7, 66-78.
- 647 Saaty, T. L. (1980). *The analytic hierarchy process: planning, priority setting, resources allocation*.  
648 New York: McGraw.
- 649 Saaty, T. L. (1996). *Multi-criteria decision making. The Analytic Hierarchy Process*, Pittsburgh.
- 650 Safari, H., Faraji, Z., & Majidian, S. (2016). Identifying and evaluating enterprise architecture risks  
651 using FMEA and fuzzy VIKOR. *Journal of Intelligent Manufacturing*, 27(2), 475-486.

- 652 Sharma, R. K., Kumar, D., & Kumar, P. (2005). Systematic failure mode effect analysis (FMEA) using  
653 fuzzy linguistic modelling. *International Journal of Quality & Reliability Management*, 22(9),  
654 986-1004.
- 655 Shyur, H. J. (2006). COTS evaluation using modified TOPSIS and ANP. *Applied mathematics and*  
656 *computation*, 177(1), 251-259.
- 657 Tadić, S., Zečević, S., & Krstić, M. (2014). A novel hybrid MCDM model based on fuzzy DEMATEL,  
658 fuzzy ANP and fuzzy VIKOR for city logistics concept selection. *Expert Systems with*  
659 *Applications*, 41(18), 8112-8128.
- 660 Tavana, M., Yazdani, M., & Di Caprio, D. (2016). An application of an integrated ANP-QFD  
661 framework for sustainable supplier selection. *International Journal of Logistics Research and*  
662 *Applications*, 1-22.
- 663 Tsaour, S. H., and Wang, C. H. (2007). The evaluation of sustainable tourism development by analytic  
664 hierarchy process and fuzzy set theory: An empirical study on the Green Island in Taiwan. *Asia*  
665 *Pacific Journal of Tourism Research*, 12 (2), 127-145.
- 666 Tserng, H. P., Yin, S. Y., Dzung, R. J., Wou, B., Tsai, M. D., & Chen, W. Y. (2009). A study of  
667 ontology-based risk management framework of construction projects through project life cycle.  
668 *Automation in Construction*, 18(7), 994-1008.
- 669 Tzeng, G. H., Chiang, C. H., & Li, C. W. (2007). Evaluating intertwined effects in e-learning programs:  
670 A novel hybrid MCDM model based on factor analysis and DEMATEL. *Expert systems with*  
671 *Applications*, 32(4), 1028-1044.
- 672 Wang, Y. M., Chin, K. S., Poon, G. K. K., & Yang, J. B. (2009). Risk evaluation in failure mode and  
673 effects analysis using fuzzy weighted geometric mean. *Expert systems with applications*, 36(2),  
674 1195-1207.

- 675 Wheeler, D.J. 2011, Problems With Risk Priority Numbers, Quality Digest, available at :  
676 [https://www.qualitydigest.com/inside/quality-insider-column/problems-risk-priority-  
678 numbers.html](https://www.qualitydigest.com/inside/quality-insider-column/problems-risk-priority-<br/>677 numbers.html)  
679  
680 Yang, J. L., and Tzeng, G. H. (2011). An integrated MCDM technique combined with DEMATEL for  
681 a novel cluster-weighted with ANP method. *Expert Systems with Applications*, 38(3), 1417-  
682 1424.  
683  
684 Yazdani, M. and Payam, A. F. (2015). A comparative study on material selection of  
685 microelectromechanical systems electrostatic actuators using Ashby, VIKOR and  
686 TOPSIS. *Materials & Design*, 65, 328-334.  
687  
688 Yazdani, M., Hashemkhani Zolfani, S., and Zavadskas, E. K. (2016). New integration of MCDM  
689 methods and QFD in the selection of green suppliers. *Journal of Business Economics and  
690 Management*, 1-17.  
691  
692 Zadeh, L. A. (1965). Fuzzy sets. *Information and control*, 8(3), 338-353.  
693  
694 Zavadskas, E. K., Turskis, Z. and Tamošaitiene, J. (2010). Risk assessment of construction projects.  
695 *Journal of civil engineering and management*, 16(1), 33-46.  
696  
697 Zwikaël, O., & Globerson, S. (2006). Benchmarking of project planning and success in selected  
698 industries. *Benchmarking: An International Journal*, 13(6), 688-700.  
699  
700

693 **List of Figures**

694

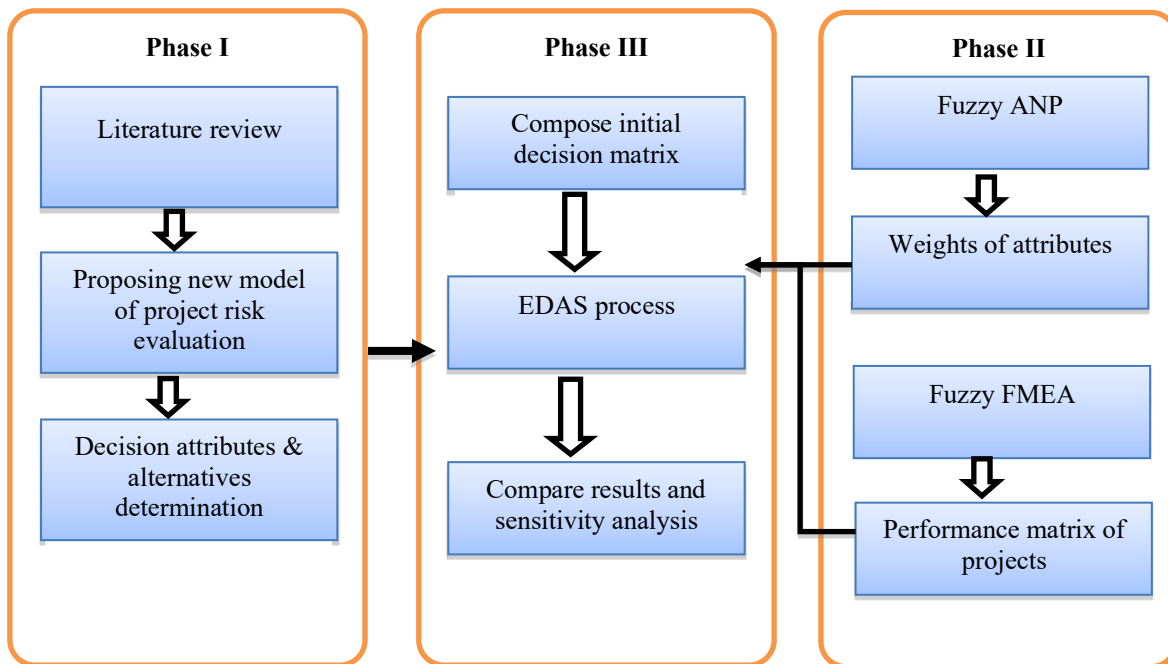
695

696 **Figure 1.** Three phase MCDM model for project risk evaluation problem

697 **Figure 2.** Risk factors and sub-factors relationship and network diagram for ANP

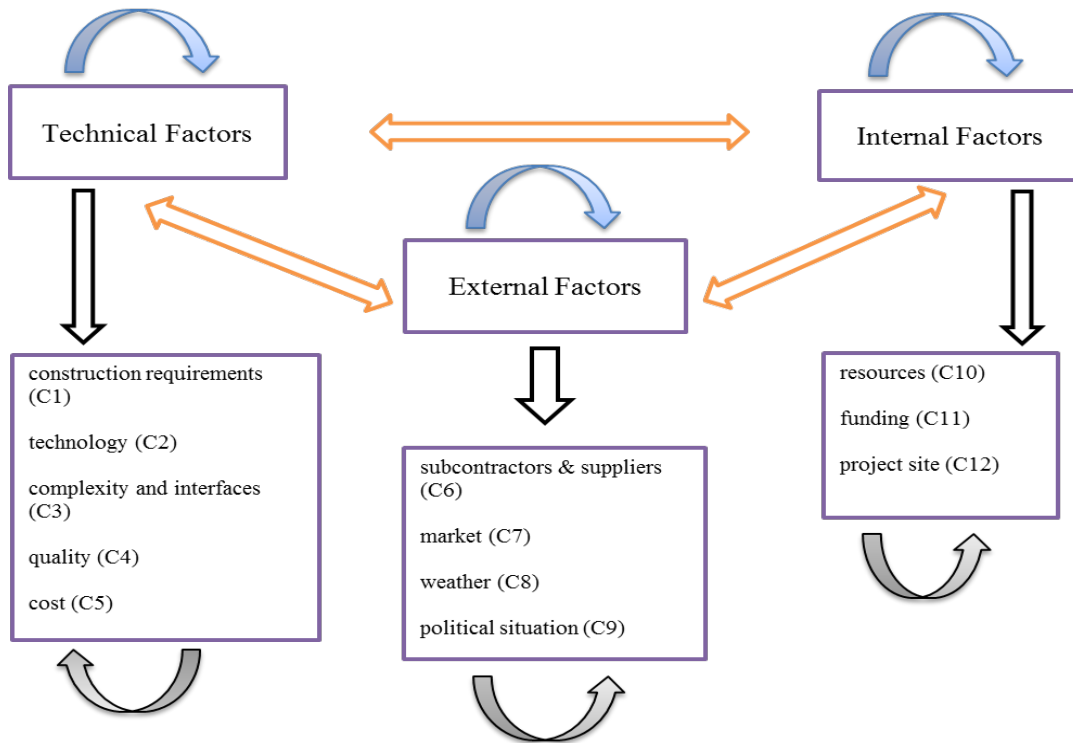
698 **Figure 3.** EDAS ranking outcomes based on different scenarios of sensitivity analysis

699  
700  
701  
702  
703  
704  
705  
706  
707  
708  
709  
710  
711  
712  
713  
714  
715  
716  
717  
718



**Figure 1.** Three phase MCDM model for project risk evaluation problem

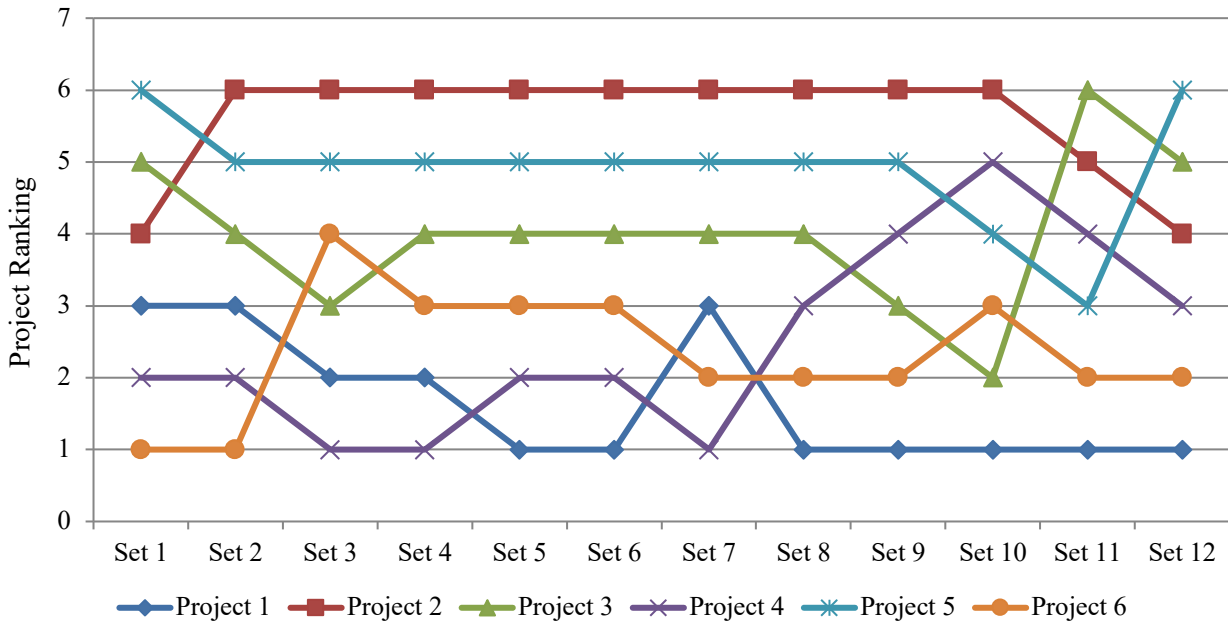




719  
720  
721  
722

**Figure 2.** Risk factors and sub-factors relationship and network diagram for ANP

723  
724  
725



726  
727  
728  
729

**Figure 3.** EDAS ranking outcomes based on different scenarios of sensitivity analysis

730

731

**Table 1.** Fuzzy scale for pairwise comparisons

732

<b>Fuzzy number</b>	<b>Linguistic variables</b>	<b>Triangular fuzzy number</b>
$\tilde{9}$	Extremely important/preferred	(7,9,9)
$\tilde{7}$	Very strongly important/preferred	(5,7,9)
$\tilde{5}$	Strongly important/preferred	(3,5,7)
$\tilde{3}$	Moderately important/preferred	(1,3,5)
$\tilde{1}$	Equally important/preferred	(1,1,3)

733

734

735

**Table 2.** Classification of fuzzy linguistic variables for RPN scoring

736

<b>Linguistic Term</b>	<b>Fuzzy Number</b>	<b>Severity</b>	<b>Occurrence</b>	<b>Detection</b>
Very Low	$\hat{1}$	A failure that has no/ minor effect on the system performance, the operator probably will not notice.	It would be very unlikely for these failures to be observed.	Defect remains undetected until the system performance degrades to the extent that the task will not be completed.
Low	$\hat{3}$	A failure that would cause slight annoyance to the operator, but that cause no deterioration to the system.	Likely to occur once, but unlikely to occur more frequently.	Defect remains undetected until system performance is severely reduced.
Medium	$\hat{5}$	A failure that would cause a high degree of operator dissatisfaction or that causes noticeable but slight deterioration in system performance.	Likely to occur more than once.	Defect remains undetected until system performance is affected.
High	$\hat{7}$	A failure that causes significant deterioration in system performance and/or leads to minor injuries.	Near certain to occur at least once.	Defect remains undetected until an inspection/test is carried out.
Very High	$\hat{9}$	A failure that would seriously affect the ability to complete The task or cause damage, serious injury or death.	Almost certain to occur several times.	Failure remains undetected, until a full inspection and test is completed.

737

738

739

740

741

742

**Table 3.** Pairwise comparison matrix for decision variables

<b>Comparative rating of all factors</b>							
<b>Factors</b>	<b>Technical</b>	<b>External</b>	<b>Internal</b>				<b>weight</b>
Technical	1	0.2	0.33	0.1111	0.1429	0.0526	0.102
External	5	1	5	0.5556	0.7143	0.7895	0.686
Internal	3	0.2	1	0.3333	0.1429	0.1579	0.211
	9	1.4	6.3				
<b>Relative importance of all factors with respect to technical factor</b>							
<b>Technical</b>	Technical	External	Internal				weight
Technical	1	3	7	0.6774	0.5	0.8235	0.667
External	0.33	1	0.5	0.2258	0.1667	0.0588	0.150
Internal	0.14	2	1	0.0968	0.3333	0.1176	0.183
	1.48	6	8.5				
<b>Relative importance of all factors with respect to external factor</b>							
<b>External</b>	Technical	External	Internal				weight
Technical	1	0.14	2	0.1176	0.0455	0.5714	0.245
External	7	1	0.5	0.8235	0.3182	0.1429	0.428
Internal	0.5	2	1	0.0588	0.6364	0.2857	0.327
	8.5	3.1	3.5				
<b>Relative importance of all factors with respect to internal factor</b>							
<b>Internal</b>	Technical	External	Internal				weight
Technical	1	2	3	0.5455	0.6	0.4286	0.525
External	0.5	1	3	0.2727	0.3	0.4286	0.334
Internal	0.33	0.33	1	0.1818	0.1	0.1429	0.142
	1.8	3.3	7				

743  
744  
745  
746  
747  
748

**Table 4.** ANP global weights assigned for each sub-factors

Factors	Sub-factors (Indicators)	Sub-factors local weight	Factors weight	Sub-factors global weights	Normalized global weight
Technical	construction requirements (C <sub>1</sub> )	0.0621	<b>0.347</b>	0.0215	0.063
	technology (C <sub>2</sub> )	0.1093		0.0379	0.11
	complexity and interfaces (C <sub>3</sub> )	0.0867		0.0301	0.088
	quality (C <sub>4</sub> )	0.0446		0.0155	0.045
	cost (C <sub>5</sub> )	0.0599		0.0208	0.061
External	subcontractors & suppliers (C <sub>6</sub> )	0.1235	<b>0.380</b>	0.0469	0.137
	market (C <sub>7</sub> )	0.1067		0.0405	0.118
	weather (C <sub>8</sub> )	0.1006		0.0382	0.111
	political situation (C <sub>9</sub> )	0.0774		0.0294	0.086
Internal	resources (C <sub>10</sub> )	0.0736	<b>0.273</b>	0.0201	0.058
	funding (C <sub>11</sub> )	0.0963		0.0263	0.077
	project site (C <sub>12</sub> )	0.0594		0.0162	0.047

749  
750

751

**Table 5.** Ranking of projects based on EDAS method

	SP	SN	NSP	NSN	AS	RANK
Project 1	0.514	0.366	0.891	0.477	0.684	3
Project 2	0.200	0.699	0.347	0	0.174	6
Project 3	0.317	0.377	0.549	0.461	0.505	4
Project 4	0.576	0.294	1	0.580	0.790	1
Project 5	0.320	0.406	0.555	0.420	0.487	5
Project 6	0.525	0.310	0.911	0.557	0.734	2

752

753

**Table 6.** Comparison of other MCDM techniques with EDAS

	SAW	WASPAS	COPRAS	TOPSIS	VIKOR	EDAS
Project 1	3	3	3	3	4	3
Project 2	6	6	6	6	6	6
Project 3	4	4	4	5	5	4
Project 4	1	1	1	1	1	1
Project 5	5	5	5	4	3	5
Project 6	2	2	2	2	2	2

754

755

**Table 7.** Twelve scenarios for sensitivity analysis

Scenarios	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub>	C <sub>6</sub>	C <sub>7</sub>	C <sub>8</sub>	C <sub>9</sub>	C <sub>10</sub>	C <sub>11</sub>	C <sub>12</sub>
Set 1	0.045	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366
Set 2	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366	0.045
Set 3	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366	0.045	0.0472
Set 4	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366	0.045	0.0472	0.0585
Set 5	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366	0.045	0.0472	0.0585	0.0605
Set 6	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366	0.045	0.0472	0.0585	0.0605	0.0627
Set 7	0.0856	0.0877	0.1104	0.1113	0.1179	0.1366	0.045	0.0472	0.0585	0.0605	0.0627	0.0765
Set 8	0.0877	0.1104	0.1113	0.1179	0.1366	0.045	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856
Set 9	0.1104	0.1113	0.1179	0.1366	0.045	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877
Set 10	0.1113	0.1179	0.1366	0.045	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104
Set 11	0.1179	0.1366	0.045	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113
Set 12	0.1366	0.045	0.0472	0.0585	0.0605	0.0627	0.0765	0.0856	0.0877	0.1104	0.1113	0.1179

756

757

758

759

760 **Appendices:**

761 **Appendix 1:** Fuzzy FMEA rating reference for projects and assigned defuzzified values

762

<b>S</b>	<b>P</b>	<b>D</b>	<b>SPD</b>	<b>Code</b>	<b>Defuzzified Value</b>
(7,9,9)	(7,9,9)	(7,9,9)	(343,729, 729)	EXH1	600.33
(7,9,9)	(5,7,9)	(5,7,9)	(175,441, 729)	EXH2	448.33
(5,7,9)	(7,9,9)	(5,7,9)	(175,441, 729)	EXH2	448.33
(5,7,9)	(5,7,9)	(7,9,9)	(175,441, 729)	EXH2	448.33
(5,7,9)	(5,7,9)	(5,7,9)	(45,343, 729)	EXH3	372.33
(5,7,9)	(3,5,7)	(3,5,7)	(125,175, 441)	VH1	247
(3,5,7)	(5,7,9)	(3,5,7)	(45,175, 441)	VH2	220.33
(3,5,7)	(3,5,7)	(5,7,9)	(45,175, 441)	VH2	220.33
(3,5,7)	(3,5,7)	(3,5,7)	(27,45,343)	H1	138.33
(1,3,5)	(1,3,5)	(3,5,7)	(1,45,175)	H2	74.33
(3,5,7)	(1,3,5)	(1,3,5)	(1,45,175)	H3	73.00
(1,3,5)	(3,5,7)	(1,3,5)	(3,45,175)	H3	73.00
(1,3,5)	(1,3,5)	(1,3,5)	(1,27,125)	M1	51
(7,9,9)	(1,1,3)	(1,1,3)	(7,9,81)	M2	32.33
(1,1,3)	(7,9,9)	(1,1,3)	(7,9,81)	M2	32.33
(1,1,3)	(1,1,3)	(7,9,9)	(7,9,81)	M2	32.33
(3,5,7)	(1,1,3)	(1,1,3)	(3,5,63)	L	23.67
(1,1,3)	(3,5,7)	(1,1,3)	(3,5,63)	L	23.67
(1,1,3)	(1,1,3)	(3,5,7)	(3,5,63)	L	23.67
(1,3,5)	(1,1,3)	(1,1,3)	(1,3,45)	VL1	16.33
(1,1,3)	(1,3,5)	(1,1,3)	(1,3,45)	VL1	16.33
(1,1,3)	(1,1,3)	(1,3,5)	(1,3,45)	VL1	16.33
(1,1,3)	(1,1,3)	(1,1,3)	(1,1,9)	VL2	3.67

763



764  
765

**Appendix 2:** Decision makers rating over risk factors of projects using FMEA codes

<b>DM<sub>1</sub></b>	<b>C<sub>1</sub></b>	<b>C<sub>2</sub></b>	<b>C<sub>3</sub></b>	<b>C<sub>4</sub></b>	<b>C<sub>5</sub></b>	<b>C<sub>6</sub></b>	<b>C<sub>7</sub></b>	<b>C<sub>8</sub></b>	<b>C<sub>9</sub></b>	<b>C<sub>10</sub></b>	<b>C<sub>11</sub></b>	<b>C<sub>12</sub></b>
Project 1	EXH2	L	H3	M2	VL2	L	VH2	M1	L	M1	M2	M2
Project 2	VL1	L	M1	M1	VH1	M1	M2	VL2	VL2	VH2	M1	H2
Project 3	M1	M1	EXH2	L	M2	L	M1	M2	H1	H2	L	L
Project 4	H2	L	M2	H3	L	EXH3	M1	H2	H2	M1	L	M2
Project 5	M2	VH1	M2	L	M2	M1	M2	M1	M1	M1	M1	L
Project 6	L	M2	H1	M1	L	VH2	VL1	H3	L	H3	EXH3	VL2
<b>DM<sub>2</sub></b>												
Project 1	EXH3	L	H2	M1	VL1	VL2	VH1	M2	VL1	M2	M1	M1
Project 2	VL2	VL1	M2	M2	VH1	M1	M1	VL1	VL2	VH1	M1	H1
Project 3	M1	M2	EXH2	L	M1	VL1	M2	M1	H2	H2	VL2	VL1
Project 4	H3	L	M1	H3	VL1	EXH2	M2	H2	H1	M2	VL1	M2
Project 5	M1	VH2	M2	VL2	M1	M2	M1	M2	M1	M2	M2	VL2
Project 6	VL1	M2	H2	M1	L	VH1	VL2	H2	VL1	H2	EXH2	L
<b>DM<sub>3</sub></b>												
Project 1	VH1	VL2	H1	M1	VL1	VL1	VH2	M1	VL2	M1	M1	M2
Project 2	VL1	VL1	M2	M1	VH2	M2	M1	VL1	VL2	VH1	M2	H1
Project 3	M1	M1	EXH3	VL2	M1	VL1	M1	M2	H3	H3	VL2	VL2
Project 4	H2	L	M1	H1	VL2	EXH3	M2	H3	H1	M2	VL2	M2
Project 5	M2	VH1	M1	VL1	M1	M2	M2	M2	M2	M1	M1	VL1
Project 6	VL2	M1	H3	M2	VL1	VH2	VL1	H1	VL2	H2	EXH1	VL1

766  
767

768 **Appendix 3:** Defuzzified aggregated decision makers judgment table (Initial decision matrix)

769

	C <sub>1</sub>	C <sub>2</sub>	C <sub>3</sub>	C <sub>4</sub>	C <sub>5</sub>	C <sub>6</sub>	C <sub>7</sub>	C <sub>8</sub>	C <sub>9</sub>	C <sub>10</sub>	C <sub>11</sub>	C <sub>12</sub>
Project 1	355.89	17	95.22	44.78	12.11	14.56	229.22	44.78	14.56	44.78	44.78	38.55
Project 2	12.11	18.78	38.55	44.78	238.11	44.78	44.78	12.11	3.67	238.11	44.78	117
Project 3	51	44.78	423	17	44.78	18.78	44.78	38.55	95.22	73.89	10.34	14.56
Project 4	73.89	23.67	44.78	94.78	14.56	397.66	38.55	73.89	117	38.55	14.56	32.33
Project 5	38.55	238.11	38.55	14.56	44.78	38.55	38.55	38.55	44.78	44.78	44.78	14.56
Project 6	14.56	38.55	95.22	44.78	21.22	229.22	12.11	95.22	14.56	73.89	473.66	14.56

770

771

772

773

774 **Appendix 4:** Matrices of the positive distance from average (PDA) and the negative distance from  
 775 average (NDA)

776

PDA	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12
Project 1	2.9109	0	0	0.0307	0.8065	0	2.371	0	0	0	0	0
Project 2	0	0	0	0.0307	0	0	0	0	0	1.7795	0	2.0317
Project 3	0	0	2.4515	0	0.2846	0	0	0	0.9716	0	0	0
Project 4	0	0	0	1.1816	0.7674	2.2089	0	0.4626	1.4225	0	0	0
Project 5	0	2.7508	0	0	0.2846	0	0	0	0	0	0	0
Project 6	0	0	0	0.0307	0.6609	0.8497	0	0.8849	0	0	3.4905	0

777

NDA	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12
Project 1	0	0.7322	0.223	0	0	0.8825	0	0.1136	0.6986	0.4773	0.5755	0.001
Project 2	0.8669	0.7042	0.6854	0	2.8041	0.6387	0.3415	0.7603	0.924	0	0.5755	0
Project 3	0.4396	0.2947	0	0.6086	0	0.8485	0.3415	0.2368	0	0.1375	0.902	0.6228
Project 4	0.188	0.6271	0.6346	0	0	0	0.433	0	0	0.55	0.862	0.1623
Project 5	0.5763	0	0.6854	0.6649	0	0.6889	0.433	0.2368	0.0729	0.4773	0.5755	0.6228
Project 6	0.84	0.3927	0.223	0	0	0	0.8219	0	0.6986	0.1375	0	0.6228

778

779

780