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Intra Coding Strategy for Video Error Resiliency: Behavioral Analysis

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Abstract—One challenge in video transmission is to deal with packet loss. Since the compressed video streams are sensitive to data loss, the error resiliency of the encoded video becomes important. When video data is lost and retransmission is not possible, the missed data should be concealed. But loss concealment causes distortion in the lossy frame which also propagates into the next frames even if their data are received correctly. One promising solution to mitigate this error propagation is intra coding. There are three approaches for intra coding: intra coding of a number of blocks selected randomly or regularly, intra coding of some specific blocks selected by an appropriate cost function, or intra coding of a whole frame. But Intra coding reduces the compression ratio; therefore, there exists a trade-off between bitrate and error resiliency achieved by intra coding. In this paper, we study and show the best strategy for getting the best rate-distortion performance. Considering the error propagation, an objective function is formulated, and with some approximations, this objective function is simplified and solved. The solution demonstrates that periodical I-frame coding is preferred over coding only a number of blocks as intra mode in P-frames. Through examination of various test sequences, it is shown that the best intra frame period depends on the coding bitrate as well as the packet loss rate. We then propose a scheme to estimate this period from curve fitting of the experimental results, and show that our proposed scheme outperforms other methods of intra coding especially for higher loss rates and coding bitrates.

Index Terms—Error resilient video coding, video error concealment, intra coding.

I. INTRODUCTION

NOWADAYS, real-time digital video transmission over networks is very popular. Due to the tremendous volume of the raw video data, video compression is inevitable. But delivering compressed data over wired/wireless channels is challenging

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since the underlying networks are not always reliable and some data losses are usually experienced during transmission.

The erroneous and unreceived data corrupts the decompression process and the video fidelity. In this condition, using error concealment techniques alleviates the problem to some extent [1]. At high compression rates, data loss is more destructive; the higher the compression, the more the sensitivity to data loss. For this reason, High Efficiency Video Coding (HEVC), the latest standard video codec, is less error resilient than H.264/AVC [2]. Therefore, this makes HEVC video communication over error prone channels a challenging problem for researchers and practitioners in this field.

In error concealment techniques, the non-received data are estimated from the received ones. This is done by exploiting the spatio-temporal correlations among the available data at the area of missing information. However, the replaced data will not be exactly the same as the actual data; therefore, there exists a mismatch/distortion between them. If the recovered frame was used as the prediction reference at the encoder, its reconstructed erroneous part would propagate into the next frames at the decoder. In video coding, a large portion of compression comes from inter frame coding, but inter frame coding increases inter dependency and causes error propagation. In contrast, although intra coding is less efficient for compression, it mitigates the error propagation problem and could be used as a strong error resiliency tool, since it does not use prediction from the other frames [3]–[6]. Therefore, by intra coding, there is a trade-off between error resiliency and compression ratio. That is, intra mode for a block must be selected with sufficient care. For this reason, loss resiliency through intra mode is discussed in several works, as described in Section II.

In this paper we show both analytically and experimentally that the best strategy for intra coding is to code some selected frames deliberately in intra mode. For doing so, considering the transmission distortion, the decoder side distortion is formulated and an objective function is developed. Through optimization of this objective function, the optimal solution indicates that coding a whole frame as an I-frame is preferred over coding a certain number of blocks in the frames as intra mode. Our investigations show that the best approach to exploit the error resiliency of intra coding is to reduce the intra period instead of distributing the intra coded blocks among the frames. We had solved a similar problem for Multiple Description Coding (MDC) in [32], but the treatment of a single stream is different from the multi streams of MDC. MDC rarely deals with concealment distortion, since most of the time at least one description is available. Therefore,

the objective functions and approaches taken for solving the problem here are different from [32].

The rest of the paper is structured as follows. Section II presents the related work, while in Section III the objective function is formulated. Through experimental results, this function is first simplified and then solved in Sections IV and V. The performance comparison with the other approaches for error resilient intra coding is presented in Section VI and the paper is concluded in Section VII.

II. RELATED WORK

In the works presented in [7], [8], a recursive algorithm called ROPE has been developed. In this algorithm, by pixel-wise operations, the encoder estimates the receiver-side expected distortion which is then used for intra/inter mode decision. However, this algorithm is too complex due to its pixel-by-pixel computations. Its extension for bursty loss channels is presented in [9], and the extension of error resilient mode decision to motion estimation and also considering intra-frame prediction for intra modes is presented in [10]. ROPE was also used in [11] to optimally decide between Motion Vector (MV) replication or intra coding mode. Using ROPE for motion estimation and reference frame generation is presented in [12], while [13] discusses the intra/inter mode selection in video transcoding, where the lossy frame and its propagated error within the ROPE algorithm is exploited. Finally, the extension of ROPE for including constrained intra prediction as candidate modes, in addition to inter and intra modes, is presented in [14].

In another proposal described in [15], frame-level channel distortion is analyzed, where through linear models/approximations and end-to-end distortion optimization, a scheme for intra mode selection and rate control is developed. Some models for transmission distortion are presented in [16] where parameters such as intra prediction, deblocking filtering, sub-pixel motion estimation and the effect of decoder side temporal error concealment are taken into account. With the same approach, an end-to-end distortion modeling and optimization method was presented in [17] which is then used to develop a faster algorithm for intra/skip mode decision [18], [19]. In [20], motion estimation and mode decision in HEVC are performed based on error propagation. Another algorithm is presented in [21] where due to high sensitivity to error propagation, the algorithm selects the intra mode for the Prediction Units (PUs) much more than is required, especially for lower content videos. Even though the authors try to solve this issue with updating some parameters, the intra rates are still high and this degrades its performance at low Packet Loss Rates (PLRs) and low bitrates.

A fast intra mode decision for loss resiliency is developed in [22] where, through a linear model, the distortion is estimated and an optimal value for Intra Refresh Rate (IRR) is obtained. IRR or simply the intra rate is the number of blocks coded in intra mode divided by the total number of blocks in the frame. A modified model for considering the role of IRR in bitrate and distortion is introduced in [23]. Using a linear model and considering motion activity and PLR, the optimal IRR and the intra coded MBs' pattern are discussed in [24]. It is shown in [25]

that for low activity sequences, cyclic intra coding of MBs is more effective than periodic I-frames, and vice-versa for highly active videos. Combining cyclic intra-refreshing with unequal error protection is introduced in [26], [27], though intra-refresh is in conflict with multiple reference selection, as shown in [28]. Error propagation is formulated and the IRR is obtained in [29], then the selected MBs for intra coding are grouped into a common slice group where they are then protected with stronger channel codes.

The above mentioned intra coding research works can be categorized into two groups: those which discuss Selecting Intra Mode (SIM) and those which discuss Intra Refresh. In SIM methods, the cost function for inter/intra mode decision is modified to take into account the lossy channel and the transmission distortion; examples are [7]–[21]. In Intra Refresh, the intra rate is determined. Then, the intra coded blocks can be selected randomly, or selected with vertically or horizontally ordered columns/rows, provided that they do not overlap in the successive frames such that the blocks in all positions are intra refreshed after a while; examples are [22]–[29].

Our work is different from the above works since our formulation and optimization leads to a straightforward and specific solution: reduce the intra period (coding a whole frame in intra mode) to achieve the best error resiliency outcome of intra coding, instead of distributing the intra coded blocks within the frames of the GOP. Afterwards, the best intra period, which depends on the content and channel loss rate, is approximately but simply obtained from a function, without additional computational complexity. The experimental results confirm the efficient performance of the proposed scheme, for various loss rates and video contents.

Another tool which can help to prevent error propagating is Reference Picture Selection (RPS) which allows the encoder to select one or two frames from a list as inter-prediction references for each prediction block. Several reference frames are examined for the best rate-distortion coding. For error resiliency, this feature is usually in conjunction with decoder feedback which informs the encoder not to select the erroneously received frames as the prediction reference [42], [43]. However, this feedback information is not available in many applications; e.g., multicast and broadcast applications, or pre-recorded video on demand applications. Moreover, responding to various receivers concurrently is not practical, or the feedback messages might be received too late. RPS without a back channel and for error resiliency has been presented in [44]. In this work, the authors propose not to use a single frame as prediction reference of the PUs, but to select from a list of reference frames such that all frames in the list are selected uniformly. However, this method needs to consider a list of frames as candidate reference frames, so it has the complexity of the multi-reference prediction. For example, for five candidate reference frames, the computational complexity of Motion Estimation and Mode Decision becomes five times more. The required encoder/decoder buffer size becomes larger with the number of reference frames as well. In the error resiliency of the intra coding method proposed in our paper, the only required information is channel loss rate, without any additional complexity in the encoder/decoder. It is worth

noting that full frame intra prediction provides random access to video stream, but it also generates large peaks of bitrates. However, such large spikes in the bitrate can be eased with either a few frames delay, which is acceptable in many applications, or compensated by statistical multiplexing with lower bitrates of P- and B-frames of other video streams. Therefore, there are many circumstances that intra coding is a feasible solution while RPS cannot be employed.

Our application scenario is distribution/broadcast of video without assuming any specific limits on delay or bandwidth, and assuming the PLR is known by the encoder. PLR can be estimated with or without back channel. The application scenario without back channel compromises the great majority of current video distribution/broadcast systems today. In such a scenario, we assume PLR is estimated by the service/network operator from the history of the channel for the specific weekday and time of the day, or is calculated offline, or is tested by small ping packets periodically, or by traffic modeling [30], or by one-way estimation methods that use message segment size, goodput, and delay [31] all estimated at the sender side, or by any other estimation means. Of course PLR can also be estimated with back channel, and this would be more accurate. In the latter scenario, our proposed method is applicable if this back channel cannot inform us of the lost packets immediately due to the delay in feedbacks or a long Round-Trip Time; therefore, retransmission of the lost data or Reference Picture Selection is not possible. This scenario is also assumed by other credible works [8], [13], [15], [17], [21]. Finally, since our method introduces a small delay of about 92 msec, as will be shown later in the paper, we assume that such small delay is acceptable for the target application.

III. THE OBJECTIVE FUNCTION FOR ERROR RESILIENT INTRA CODING

For error resilient coding, the following two aspects of intra coding must be considered:

First aspect - intra coding prevents temporal error propagation, since it has no reference to the other frames. In intra coding of advanced video codecs, such as H.264/AVC and H.265/HEVC, pixels of the adjacent blocks are used as intra prediction references, and these references (in encoded form) together with the residual data are encapsulated and transmitted in a single packet. However, if the reference pixels had been encoded in inter mode, they themselves might be erroneous, even if the residual data is received correctly. In this case, temporally propagated errors can propagate spatially into the intra-coded blocks. To avoid this condition and exploit the error propagation prevention provided by intra coding, the option of ‘‘Constrained-IntraPred’’ can be enabled, which restricts the intra mode to use only the pixels of adjacent intra coded blocks as prediction references. This way, the received intra coded PUs are correctly decodable.

Second aspect - in no loss conditions, inter mode is obviously used more often than intra mode, because inter-coded blocks have lower bitrates than intra coded ones. By enabling the ‘‘ConstrainedIntraPred’’ option, the compression efficiency

of intra mode is reduced even more, but it is beneficial for error resiliency [16] when we do have losses.

Therefore, in deciding to code a block in intra mode, there is a trade-off between bitrate and error resiliency. In this section, an objective function is developed which, rather than optimizing the encoder side rate-distortion, the decoder side rate-distortion is optimized. In other words, taking into account the channel distortion, the receiver side distortion is estimated at the encoder which is then used as the objective function.

Intra/inter mode selection is conventionally carried out based on the following Lagrangian cost function [33], [34]:

$$cost = D_q + \lambda R \quad (1)$$

where D_q is the quantization distortion in Mean Squared Error (MSE), λ is the Lagrangian coefficient and R is the number of required bits. This cost function is computed for the candidate modes and the mode with the lowest cost is selected as the final mode. However, this cost function does not take the transmission distortion into account. To consider it, with the same approach as presented in [15]–[17], the rate overall-distortion in a frame is represented in (2). The assumption behind this equation is that PLR is known at the transmitter side.

$$D^{(1)} = (1 - PLR) D_q^{(1)} + PLR D_{conceal}^{(1)} \quad (2)$$

where $D^{(1)}$, $D_q^{(1)}$ and $D_{conceal}^{(1)}$ are the expected total distortion, the quantization distortion, and the error concealment distortion for frame 1, respectively. The *expected* distortion means the average distortion seen over a long enough duration, or equivalently over a variant enough packet loss pattern, the latter used in our simulation. Note that the concealment distortion, $D_{conceal}$ in (2), is the distortion when all packets of the frame are lost and the frame is error concealed. It is evident that the frame is transmitted by a single packet; however, as shown in the Appendix, this is also valid when the frame is encoded into n packets and the packets convey the same amount of information.

Frame 0 is the initial I-frame of the sequence which is assumed to be received correctly. For frame 1, depending on whether its packets are received or not, the distortion will be $D_q^{(1)}$ or $D_{conceal}^{(1)}$, respectively. For frame 2, it becomes:

$$D^{(2)} = (1 - PLR) D_q^{(2)} + PLR D_{conceal}^{(2)} + PLR [1 - \beta^{(2)}] \Delta^{(1)} \quad (3)$$

where $\beta^{(2)}$ is the intra rate of frame 2 and

$$\Delta^{(1)} = E \left[\left(F_q^{(1)} - F_{conceal}^{(1)} \right)^2 \right] \quad (4)$$

is the mean squared difference between frame 1 decoded correctly ($F_q^{(1)}$) and loss concealed ($F_{conceal}^{(1)}$); i.e., $\Delta^{(1)}$ denotes the *Mismatched Distortion* for frame 1 caused by error concealment. We assume that only the previous frame is used as prediction reference, as happens most of the times in encoders. Enabling multi-frame prediction results in a slight improvement in quality but at the cost of significant computational cost.

Equations (3) and (4) show that the quality of frame 1 directly affects the quality of frame 2, and its effect is controlled by

parameter $\beta^{(2)}$ in (3). At larger β , the impact of mismatched distortion is clearly reduced, since intra coded PUs do not refer to the previous frame. As shown in [15], the quantization and mismatched distortions are independent of each other and one can simply write:

$$D_{conceal}^{(2)} = D_q^{(2)} + \Delta^{(2)} \quad (5)$$

Substituting (5) into (3) gives:

$$\begin{aligned} D^{(2)} &= D_q^{(2)} + PLR \left[\Delta^{(2)} + (1 - \beta^{(2)}) \Delta^{(1)} \right] \\ &= D_q^{(2)} + PLR \Delta_{accum}^{(2)} \end{aligned} \quad (6)$$

in which

$$\Delta_{accum}^{(2)} = \Delta^{(2)} + (1 - \beta^{(2)}) \Delta^{(1)} \quad (7)$$

is the *Accumulated Mismatched Distortion* seen in frame 2. It is evident that for frame 1, $\Delta_{accum}^{(1)} = \Delta^{(1)}$ and then (7) can be rewritten as:

$$\Delta_{accum}^{(2)} = \Delta^{(2)} + (1 - \beta^{(2)}) \Delta_{accum}^{(1)} \quad (8)$$

Following the above concept, the distortion for the n th frame is:

$$D^{(n)} = D_q^{(n)} + PLR \Delta_{accum}^{(n)} \quad (9)$$

where

$$\begin{aligned} \Delta_{accum}^{(n)} &= \Delta^{(n)} + (1 - \beta^{(n)}) \Delta_{accum}^{(n-1)} \\ \Delta_{accum}^{(0)} &= 0 \end{aligned} \quad (10)$$

and

$$\Delta^{(n)} = E \left[\left(F_q^{(n)} - F_{conceal}^{(n)} \right)^2 \right] \quad (11)$$

Therefore, the distortion over a GoP of N frames is as given in (12) (as already mentioned, the 0th frame of the GoP is excluded from the summation):

$$D_{GoP} = \sum_{i=1}^N D^{(i)} = \sum_{i=1}^N \left(D_q^{(i)}(\beta) + PLR \Delta_{accum}^{(i)}(\beta) \right) \quad (12)$$

where $\beta = [\beta^{(1)}, \beta^{(2)}, \beta^{(3)}, \dots, \beta^{(N)}]$ is the vector intra rates for the N frames of the GoP. Quantization Parameter (QP) is excluded from this formulation, since its variation is usually ± 1 units at the given bitrate, except for sudden changes; e.g., scene-cut or fast/non-translational motions which is difficult for compensation with inter prediction. Therefore, we can assume that QP does not have significant changes for the N frames under consideration.

With the aim of maximizing the received video quality, the objective function with a constraint on the overhead bitrate of intra coding is:

$$\begin{aligned} \min_{\beta} & \left\{ \sum_{i=1}^N \left(D_q^{(i)}(\beta) + PLR \Delta_{accum}^{(i)}(\beta) \right) \right\} \\ \text{s.t.} & \sum_{i=1}^N R_{intra}^{(i)}(\beta) \leq R_{red} \end{aligned} \quad (13)$$

where $R_{intra}^{(i)}$ is the number of additional bits needed for intra encoding of the i th frame according to the intra rate of $\beta^{(i)}$; that is, if $\beta^{(i)} = 0$, then $R_{intra}^{(i)} = 0$ and no block is coded in intra mode for error resiliency. The term R_{red} in (13) is the total redundancy budget allowed for these N frames for intra coding, which in turn is related to the PLR and the required degree of error resiliency. Increasing the intra rates of frame i ; i.e., $\beta^{(i)}$, reduces $\Delta_{accum}^{(i)}$ (see equation (10)) but in turn increases bitrate usage.

IV. SOLVING THE OBJECTIVE FUNCTION

In this section, a solution to the constrained problem of (13) is driven through approximation. The behaviors of terms in this equation are observed and approximated through matching them to the experimental results. The experiments settings, the simplifying approximations, and the solution to the problem are provided in subsections A, B and C, respectively.

A. The Error Concealment Strategy

An important part of distortion in (13) belongs to the distortions caused by error/loss concealment. Error concealment techniques can be categorized into spatial and temporal domain processing techniques. In the spatial domain, the lost area of the frame is concealed using the spatially neighboring pixels. These methods exploit the correlations that usually exist among the neighboring pixels. In the temporal processing techniques, the contents from the previous and/or the future frames are addressed by MVs and used for temporal replacement. The actual MVs are not available and must be estimated or recovered first by the temporal loss concealment methods.

If the lost area is large, spatial domain is not effective, as pixels are very far apart from each other to be useful. The reason for dealing with large lost areas in HEVC is the size of its Coding Tree Unit (CTU), which can be as large as 64×64 pixels. An integer number of CTUs are regarded as one slice and an integer number of slices are encapsulated into a single transmission packet. Therefore, packet losses in HEVC streams affect a significant portion of the picture area especially for smaller picture sizes. As a result, temporal error concealment in HEVC streams is more applicable than spatial concealment.

Actually, exploiting the temporal frames' MVs will provide higher quality error concealment. One simple yet efficient technique is the Motion Copy algorithm where the MV of the collocated block is simply used for motion compensated temporal replacement. If the collocated block is coded in intra mode, Zero MV is used. However, in the case of having a high percentage of intra coded blocks, this approach is not efficient due to lack of MVs for intra blocks. For intra coded blocks, one solution is to recover the MVs by Boundary Matching Algorithm (BMA). A suggestion is to combine Motion Copy for inter coded and reliable collocated blocks, and BMA for intra coded or unreliable collocated blocks, as presented in [35]. The blocks with high residual signals are labeled as unreliable blocks and their MVs are not used for MV recovery. In [35], loss concealment is performed in two stages: firstly, the lost area is replaced using the Motion Copy algorithm. Then, for the unreliable MVs,

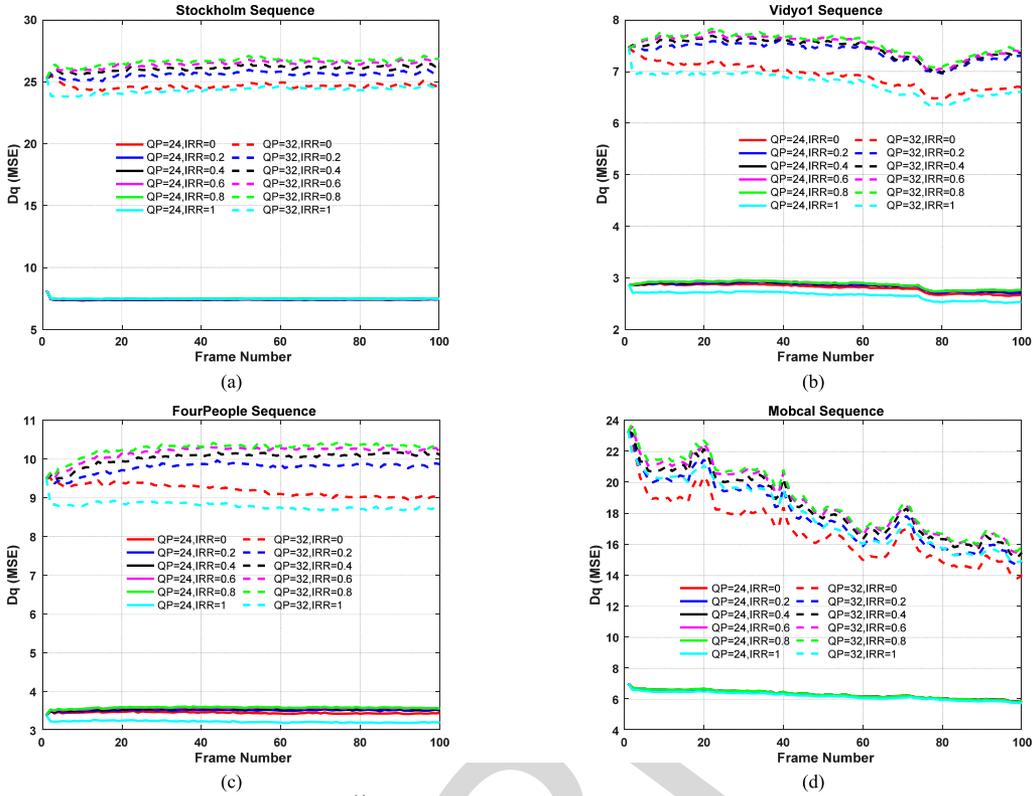


Fig. 1. The variation of $D_q^{(i)}(\beta^{(i)})$ with respect to IRR for test sequences and two values of QP .

376 MVs are obtained using BMA. Some other methods such as
 377 [36]–[37] are proposed for HEVC error concealment, but they
 378 work again based on the spatially close boundary pixels, which
 379 are not always available in the actual scenarios. The algorithm
 380 presented in [38] works based on MV extrapolation but with
 381 applying higher weights to the MVs belonging to the larger parti-
 382 tions. However, the problem is that this algorithm is based on
 383 the MVs of the blocks of the previous frame and therefore it is
 384 efficient when there are a few intra coded blocks. The method of
 385 [39] is proposed for error concealment of a sequence of succes-
 386 sive MBs in H.264/AVC. This error concealment method does
 387 not need to know the MVs’ neighboring spatially or tempo-
 388 rally missed blocks, and instead estimates them by BMA. This
 389 method is also useful for large area losses of HEVC. The chal-
 390 lenge in using BMA is the fact that the error concealment of one
 391 block will affect the error concealment of the following blocks
 392 as well. One solution, proposed in [39], is rank ordering the MBs
 393 for error concealment based on the texture of the available MBs
 394 in the surrounding of the lost area. A missed MB with a higher
 395 texture around it will be error concealed with higher priority.
 396 The criterion for the higher texture is the standard deviation of
 397 the luminance pixel values. Another solution for considering the
 398 interaction of loss concealed blocks is presented in [40], but it
 399 imposes significant computational complexity without consid-
 400 erable improvement.

401 In this paper, three techniques are used for error concealment:
 402 Motion Copy, the method presented in [35], and the method
 403 presented in [39]. The first two methods are appropriate when

404 the blocks in the earlier frame are encoded mostly in inter mode,
 405 and the third method is suitable when the blocks in the earlier
 406 frame are encoded mostly or completely in intra mode. Then, the
 407 highest quality output is selected and used for the measurements.

408 It is worth noting that throughout the paper error concealment
 409 and loss concealment are used interchangeably, but in fact loss
 410 concealment is carried out. The reason is that in highly error
 411 prone networks, such as wireless networks, severely erroneous
 412 packets cannot be corrected and they are regarded as lost packets
 413 by the decoder. However, if the used entropy coder is symmetric,
 414 such as that of the H.263 codec, then parts of the data can be
 415 retrieved and the lossy area can be less than that of whole packet
 416 loss [45]. Since H.265/HEVC does not use symmetric entropy
 417 coder, then there would not be any retrieval of erroneous parts
 418 and the whole packet can be regarded as lost. Hence, loss con-
 419 cealment is a proper choice.

B. Simplifying the Objective Function

420
 421 First, the quantization distortion does not significantly change
 422 with parameter $\beta^{(i)}$. That is, $D_q^{(i)}(\beta^{(i)})$ is approximately con-
 423 stant when $\beta^{(i)}$ varies from minimum ($\beta = 0$) to maximum
 424 ($\beta = 1$). This can be verified from the simulation results shown
 425 in Fig. 1. In this figure, four HD test video sequences are coded
 426 with HM16.0, the reference software of HEVC, at two values
 427 of QP and six values of IRR. The tested video sequences are
 428 *Stockholm*, *Vidyo1*, *FourPeople* and *Mobcal*. For the given intra
 429 rates, a sufficient number of PUs with sizes of 16×16 pixels

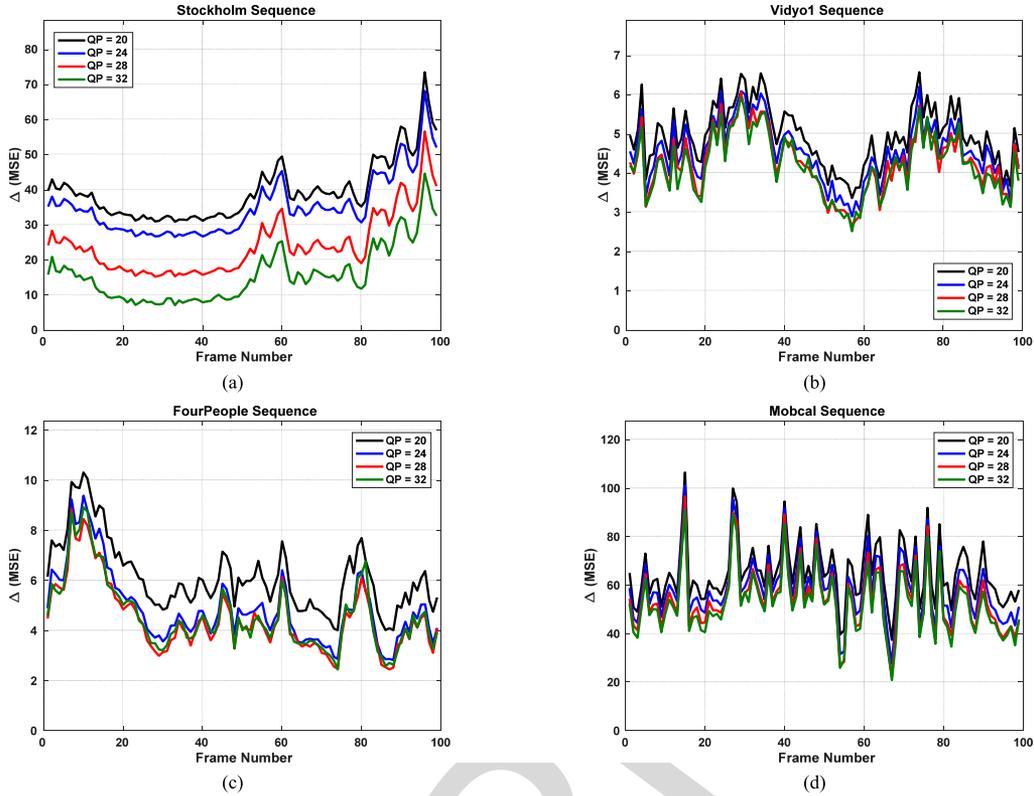


Fig. 2. The variation of mismatched distortion ($\Delta^{(i)}$) for the frames of test sequences for four values of QP .

430 are selected randomly and are forced to intra coding mode. As
 431 already mentioned, the randomly selected PUs do not overlap in
 432 the frames.

433 Fig. 1 shows the ignorable changes of $D_q^{(i)}$ with $\beta^{(i)}$. It can
 434 also be seen that the variation in $D_q^{(i)}$ for $QP = 24$ is less than
 435 that of $QP = 32$. The mathematical reason is that for smaller
 436 QPs , or smaller quantization step sizes (Q_{SS}), the high bitrate
 437 approximation is more accurate and the quantization distortion
 438 is nearly equal to $\frac{Q_{SS}^2}{12}$ [17]. This is fixed for various signals,
 439 independent of inter or intra coding. However, the difference
 440 in $D_q^{(i)}$ s for various β s is still ignorable, even for $QP = 32$.
 441 Therefore, $D_q^{(i)}$ is fixed with the optimization arguments and
 442 equation (13) can be simplified as:

$$\begin{aligned} \min_{\beta} & \left\{ \sum_{i=1}^N \left(PLR \Delta_{accum}^{(i)}(\beta) \right) \right\} \\ \text{s.t.} & \sum_{i=1}^N R_{intra}^{(i)}(\beta) \leq R_{red} \end{aligned} \quad (14)$$

443 An important term in (14) is $\Delta_{accum}^{(i)}$ which is the multiply-
 444 accumulated of mismatched distortions $\Delta^{(i)}$ s, with the multipli-
 445 cation coefficient of $(1 - \beta^{(i)})$, as given in (10). Therefore, the
 446 variation of $\Delta^{(i)}$ per frames is important in the behavior of the
 447 objective function of (13). To measure $\Delta^{(i)}$ s, the frames are first
 448 error concealed with the strategy given in IV.A, and then $\Delta^{(i)}$ is
 449 calculated by (11). The results are shown in Fig. 2 where it can be
 450 seen that, most of the times and with a good approximation, the
 451 frames of a sequence have close mismatched distortions, that is:

$$\Delta^{(1)} \cong \Delta^{(2)} \cong \dots \cong \Delta \quad (15)$$

452
 453 Even though it might not be valid for all frames, the variations
 454 are smooth in the windows of N frames, as large as the usually
 455 used GoP sizes (30–60 frames). This assumption may not be
 456 much accurate; however, this assumption, by nature, is similar
 457 to the assumption made in Rate-Control (RC) algorithms. In
 458 RC algorithms, the goal is to control the total bitrate to be less
 459 than the given bound with minimum fluctuation in the quality.
 460 Therefore, for a real-time RC, the encoder must assume that the
 461 future frames have almost the same behavior in the view of com-
 462 pression properties. Even though this assumption is not always
 463 valid, it is very efficient and helpful in practice. Similar to RC
 464 algorithms, we can assume that the frames behave similarly in
 465 the view of mismatched distortion. Therefore, with the assump-
 466 tion of (15), $\Delta^{(i)}$ is fixed for the frames, and since the employed
 467 loss concealment strategy is not much sensitive to the intra/inter
 468 coding, it is also fixed with β . Therefore, by substituting the
 469 recursive formula given in (8), the objective function of (14) can
 470 be expanded as follows:

$$\begin{aligned} \min_{\beta} & \left\{ PLR \cdot \Delta \left[N + \sum_{i=1}^N \left(\sum_{j=1}^{N-(i-1)} \left(\prod_{k=0}^{i-1} (1 - \beta^{(j+k)}) \right) \right) \right] \right\} \\ \text{s.t.} & \sum_{i=1}^N R_{intra}^{(i)}(\beta) \leq R_{red} \end{aligned} \quad (16)$$

where PLR and Δ are assumed constant during optimization. 471

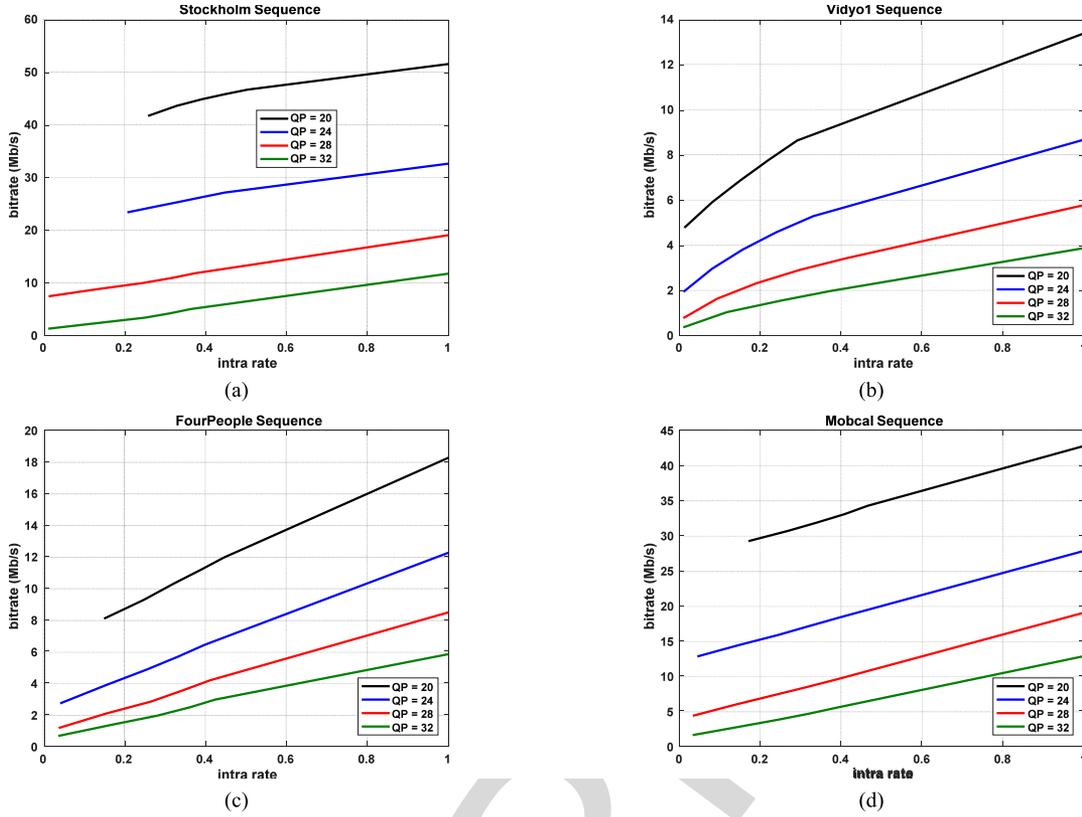


Fig. 3. The variation of bitrate with intra rate for various QPs and test sequences.

472 Now, for the constraint of (16), we do another simulation: the
 473 variation of frame bits when β varies from 0 to 1, as depicted in
 474 Fig. 3. In this figure, the average bitrates needed for sending the
 475 encoded video frames are measured and shown against the intra
 476 rate.

477 From Fig. 3, we can generally assume that the bitrates are
 478 increased almost linearly with β . That is:

$$\begin{aligned} R^{(i)} &= R_0^{(i)} + R_{intra}^{(i)} = R_0^{(i)} + \alpha^{(i)} \beta^{(i)} \\ \Rightarrow R_{intra}^{(i)} &= \alpha^{(i)} \beta^{(i)} \end{aligned} \quad (17)$$

479 where $R_0^{(i)}$ is the bitrate of the i^{th} frame for $\beta = 0$. The figure
 480 shows that the curves almost have the same slope; that is, they
 481 have the same α defined in (17). For this reason, the constraint
 482 term in (16) can be stated as:

$$\sum_{i=1}^N (\alpha \beta^{(i)}) \leq R_{red} \quad (18)$$

483 or equivalently

$$\sum_{i=1}^N \beta^{(i)} \leq \beta_{red} \quad (19)$$

484 where β_{red} is the intra rate budget; i.e., the sum of total intra
 485 rates allowed to be assigned to these N frames. Therefore, the

objective function of (16) is simplified as

486

$$\begin{aligned} \min_{\beta} & \left\{ PLR \cdot \Delta \left[N + \sum_{i=1}^N \left(\sum_{j=1}^{N-(i-1)} \left(\prod_{k=0}^{i-1} (1 - \beta^{(j+k)}) \right) \right) \right] \right\} \\ \text{s.t.} & \sum_{i=1}^N \beta^{(i)} \leq \beta_{red} \end{aligned} \quad (20)$$

487 Since we can assume that PLR and Δ are fixed during opti-
 488 mization, the problem in (20) can be rewritten as:

487
488

$$\begin{aligned} ErrorPro_{min} &= \min_{\beta} \left\{ \sum_{i=1}^N \left(\sum_{j=1}^{N-(i-1)} \left(\prod_{k=0}^{i-1} (1 - \beta^{(j+k)}) \right) \right) \right\} \\ \text{s.t.} & \sum_{i=1}^N \beta^{(i)} \leq \beta_{red} \end{aligned} \quad (21)$$

489 It is worth mentioning that for simplicity of deriving the objec-
 490 tive function, without loss of generality, there are no B-frames.
 491 This is because, in general, some B-frames maybe used as pre-
 492 diction reference like P-frames causing error propagation, while
 493 others are not used as the reference and hence do not propagate
 494 the errors but they become erroneous. Modifying our formula-
 495 tions to highlight this matter makes the equations more compli-
 496 cated without giving the required information to the reader.

TABLE I
THE OUTPUT OF THE OBJECTIVE FUNCTION OF (21) FOR SOME VALUES OF β_{red}

Range of β_{red}	Intra rate of the frames															Constraint
	$\beta^{(1)}$	$\beta^{(2)}$	$\beta^{(3)}$	$\beta^{(4)}$	$\beta^{(5)}$	$\beta^{(6)}$	$\beta^{(7)}$	$\beta^{(8)}$	$\beta^{(9)}$	$\beta^{(10)}$	$\beta^{(11)}$	$\beta^{(12)}$	$\beta^{(13)}$	$\beta^{(14)}$	$\beta^{(15)}$	
$\beta_{red} \leq 1$	0	0	0	0	0	0	0	a_1	0	0	0	0	0	0	0	$a_1 = \beta_{red}$
$1 < \beta_{red} \leq 1.45$	0	0	0	a_1	0	0	0	1	0	0	0	a_2	0	0	0	$a_1 + a_2 = \beta_{red} - 1$
$1.45 < \beta_{red} \leq 2$	0	0	0	0	a_1	0	0	0	0	1	0	0	0	0	0	$a_1 = \beta_{red} - 1$
	0	0	0	0	0	1	0	0	0	0	0	a_1	0	0	0	
$2 < \beta_{red} \leq 2.71$	0	0	0	0	1	0	0	0	0	1	0	0	a_1	0	0	$a_1 = \beta_{red} - 2$
	0	0	0	0	1	0	0	a_1	0	0	1	0	0	0	0	
	0	0	a_1	0	0	1	0	0	0	0	1	0	0	0	0	
$2.71 < \beta_{red} \leq 3$	0	0	0	a_1	0	0	0	1	0	0	0	1	0	0	0	$a_1 = \beta_{red} - 2$
	0	0	0	1	0	0	0	a_1	0	0	0	1	0	0	0	
	0	0	0	1	0	0	0	1	0	0	0	a_1	0	0	0	
$3 < \beta_{red} \leq 3.6$	0	a_1	0	1	0	a_2	0	1	0	a_3	0	1	0	a_4	0	$a_1 + a_2 + a_3 + a_4 = \beta_{red} - 3$

497 C. Solving the Simplified Objective Function

498 In this subsection, the solution for the objective function given
499 in (21) is discussed. The problem is actually minimizing the
500 error propagation at a given intra rate budget. As an example,
501 this problem is solved for $N = 15$ and various values of β_{red} ;
502 the results are tabulated in Table I.

503 As can be seen from this table, when $\beta_{red} \leq 1$, the best frame
504 for intra coding is the middle frame. If there was more intra
505 budget; i.e., $1 < \beta_{red} \leq 1.45$, $\beta^{(4)}$ and $\beta^{(12)}$ begin to grow
506 irrespective of whether the intra rate is allocated to the 4th frame
507 or the 12th frame. However, when intra rate budget exceeds
508 1.45, the optimization function given in (21) recommends other
509 frames for intra coding to be chosen; e.g., frames 5 and 10, where
510 frame 10 is coded wholly as I-frame, and frame 5 has partially
511 intra coded blocks. Equivalently, another package is frames 6 and
512 11, where frame 6 is now selected for I-frame coding. One can
513 see that these two packages produce the same obstacle against
514 the error propagation.

515 For some other regions of β_{red} , the selected frames are given
516 in Table I. One important point is changing the intra coded frame
517 candidates imposed by the objective function of (21). The reason
518 is that, if β_{red} is between two integers K_1 and K_2 ; that is $K_1 <$
519 $\beta_{red} < K_2$, the optimizers may decide to add another frame for
520 intra coding in addition to K_1 frames (e.g., one frame between
521 them), or decide to select K_2 frames for intra coding and reduce
522 the intra rate of one of them to comply with the bound of β_{red} .
523 Clearly, if β_{red} is close to K_1 , the former case happens, and the
524 latter case happens when β_{red} is close enough to K_2 . However,
525 as shown in Fig. 4, $ErrorPro_{min}$ behaves continuously at these
526 border points of β_{red} . In each interval shown by broken lines, the
527 intra coding frame candidates are the same where one or more
528 appropriate frames of these candidates consume the allocated
529 intra coding budget. As already mentioned, the slope of decay
530 in $ErrorPro_{min}$ in each interval is constant. If β_{red} becomes
531 larger than 7, the frames are alternately coded as I-frame; that
532 is the GOP structure is IPIPIP, and now all P-frames have the
533 same priority for intra rate for all β_{red} amounts; therefore; there
534 are no broken lines in Fig. 4 for $\beta_{red} > 7$.

535 This solution proves that to achieve the best error resiliency
536 for intra coding, the best strategy is to concentrate on intra

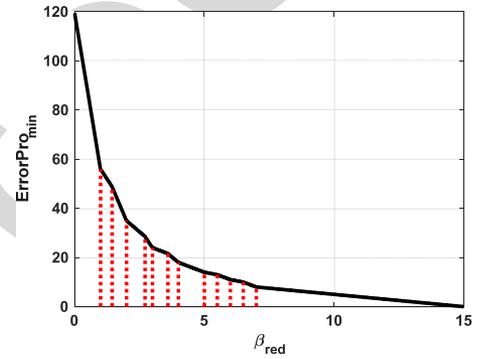


Fig. 4. Behavior of $ErrorPro_{min}$ with β_{red} .

537 coding the blocks in the middle frame of the GoP, such that
538 the entire frame is coded as an I-frame. If the intra rate budget
539 (or accordingly bitrate budget) allows, more frames can still be
540 coded in intra mode. In other words, the output of the objec-
541 tive function is to reduce the intra period; this strategy leads
542 to smaller error propagation and hence higher video quality for
543 lossy channels, compared to the case that intra coded blocks are
544 distributed among the frames.

545 V. THE OPTIMAL VALUE FOR THE INTRA PERIOD

546 As shown in Table I, at a larger β_{red} , the number of I-frames
547 in the GoP can increase. This is in favor of mitigation of error
548 propagation; however, the required bitrate for sending the video
549 is increased since the compression ratio is decreased.

550 Having more I-frames is justified in channels with higher loss
551 rates and vice versa. Therefore, PLR and the coding bitrate affect
552 the best value for β_{red}^* . As shown in Table I, β_{red}^* is directly
553 related to Intra Period (IP); therefore, the problem of finding
554 $\beta_{red-opt}$ is equivalent to finding an optimal value for IP , denoted
555 as IP^* . However, to find IP^* analytically, one must know the
556 rate-distortion behavior of the frames of the GoP under consid-
557 eration; that is, the behavior of future frames must be known
558 *a priori*, which is not possible unless it is estimated based on
559 the frames' history similar to the work presented in [41]. This
560

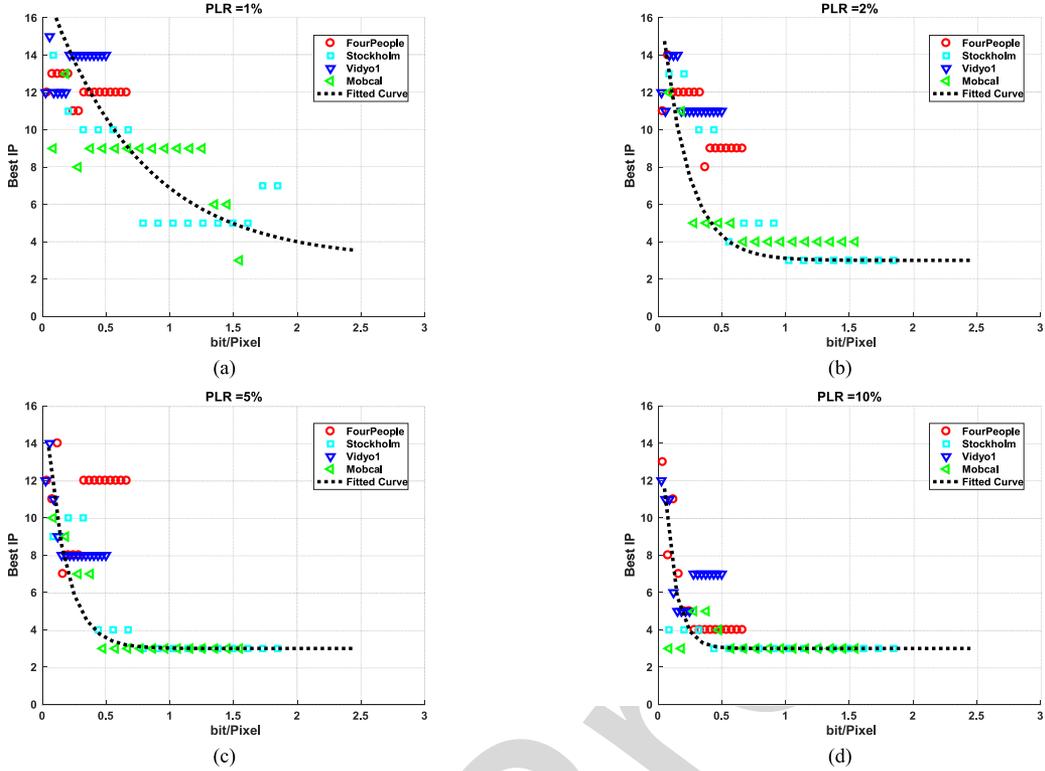


Fig. 5. The best IP versus bit/pixel for various PLRs and test sequences.

560 way, the problem can be solved using classical constraint optimization approaches. However, the complexity of the problem and non-trivial solutions have encouraged us to use an empirical approach. Therefore, IP^* has been found through experimental measurements, as follows.

565 The videos are encoded in Slice Mode, and each slice contains an integer number of CTUs in raster scan order. Each coded slice can be as large as 1500 bytes, meeting the Maximum Transmission Unit (MTU) of the network, and transmitted as a single packet. The channels experience a burst form of loss generated by Elliot-Gilbert model [46]. At each PLR , 40 packet loss patterns with an average burst length of three packets are generated and applied on the bit streams.

573 The video sequences are encoded at various values of IP ; $IP = M$ means every M th frame of the sequence is coded as an I-frame. For example, for $IP = 3$, there are two P-frames after each I-frame, and this pattern is repeated throughout the sequence. In a GoP of 30 frames, the videos are encoded with $IP = 1, 2, \dots, 15$ (for GoP of N frames, $IP > \frac{N}{2}$ is not reasonable). The compressed bit stream is subjected to a specific PLR , and the decoded video is loss concealed (as given in IV.A) and the resulting quality is measured. Video quality is measured in terms of Video Quality Model (VQM) [47] and its average index taken over the loss patterns is calculated. VQM is a video quality assessment method which considers both spatial and temporal distortions, so it is quite suitable to our case. For each test video and at the given PLR , the best IP which provides the best quality (i.e., the lowest VQM index, since higher quality is equivalent to lower VQM index) at the corresponding bitrate is selected. Fig. 5 shows the best IP s as a function of bit/pixel for four sequences.

591 It can be seen that the best IP becomes smaller at higher bitrates and higher PLRs. Even though some points are not close to the others, they can be fitted on decaying exponential functions, as shown in Fig. 5. The fitted curves can be formulated with the following equations:

$$IP^* = 3 + 15 \exp\left(-\frac{R}{R_0}\right)$$

$$R_0 = 0.15 + 1.4575 \exp\left(-\frac{PLR}{0.01}\right) \quad (22)$$

596 where R is the bit per pixel. Clearly, IP^* obtained from (22) must be rounded to the nearest integer number. Even though the decimal values are also applicable, our empirical approach and curve fitting is not accurate enough for extracting decimal values for frames' intra rates.

601 One issue is the fact that coding a frame fully in Intra mode might cause sudden changes in the bitrate and hence more congestion in the lossy channels. However, for numerous applications, like video broadcast, streaming, multicasting etc., one needs to play the video at almost any time during transmission. This facility can only be provided by Intra coded frames. On the issue of increased I-frame bitrates, one should note that in these applications, normally several video flows are multiplexed, such that higher bitrates of I-frames coincide with lower bitrates of many P- and B-frames of the other flows and are easily smoothed out. Despite this, even for a single video flow, some traffic shaping, such as coarser quantization parameter for I-frames can be applied to reduce the bits; however, this solution may lead to quality flicker due to lower qualities of the I-frames if the QPs of I-frame and P-frames are much different. For high motion

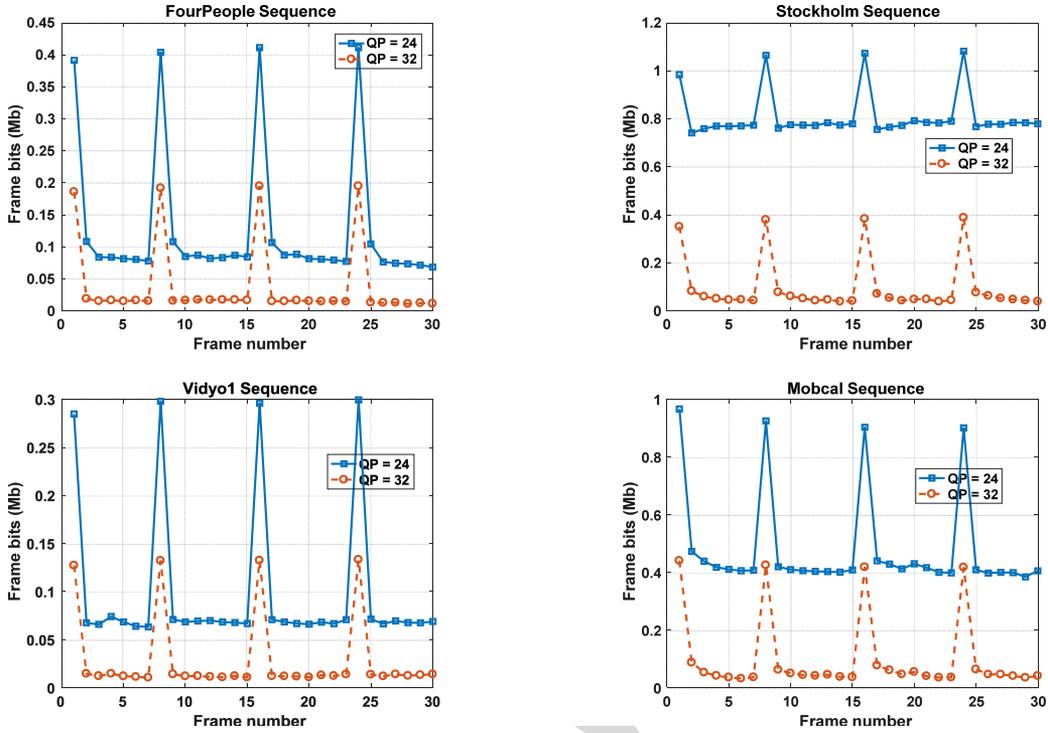


Fig. 6 The sudden changes in the frame bits when a frame is encoded as I-frame. Every 8 frames, one frame is Intra coded entirely.

616 and high texture videos, the difference between I and P frames' bits are not so large and this approach might be sufficient there. 617
 618 If this was not the case, another solution is to have the same QP for I and P frames but use an encoder smoothing buffer to regulate the bitrate (e.g., traffic shaping), of course at the cost of a few frames delay in video display. How this delay can solve the problem is explained below. Let us assume that intra period is M frames. If the frame rate of the video is FPS , the average bitrate required by the channel is:

$$R = FPS \frac{((M-1)R_P + R_I)}{M} \text{ bits/sec} \quad (23)$$

625 where R_P and R_I are number of bits needed for coding the P-frames and I-frames, respectively. Now if the I-frame has k times more bits than the P-frames, then:

$$\begin{aligned} R &= \frac{FPS (M-1+k) R_P}{M} \\ &= \frac{FPS (M-1+k) R_I}{kM} \text{ bits/sec} \quad (k > 1) \end{aligned} \quad (24)$$

628 At each $1/FPS$ second, the total sent bits are:

$$\begin{aligned} R &= \left(1 + \frac{k-1}{M}\right) R_P \\ &= \left(\frac{M+k-1}{kM}\right) R_I \text{ bits/sec} \quad (k > 1) \end{aligned} \quad (25)$$

629 Therefore, more than one P-frame or less than one I-frame is transmitted at each $1/FPS$. That is, compared to the case where all frames have the same number of bits (i.e., $k = 1$), delivering P-frames is faster and delivering I-frames is slower. 630
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 632

633 However, the issue that arise here is the transmit and receive buffers' overflow and underflow in a live streaming application. It can be shown that, with display latency as large as $M(k-1)/(M-1+k)$ frames, there is no overflow or underflow in the buffers and continuous playing of the video is preserved (see Appendix B in [32] for the proof). This latency increases with M ; therefore, a smaller M chosen for higher PLRs leads to lower latencies. 634
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641 The value of k is content dependent; Fig. 6 shows the number of bites of I and P frames, with $M = 8$ for four sequences and two QPs. One can see that k is about 1.5 for *Stockholm* at $QP = 24$; that is, k is small and the delay is not significant. For example, for PLRs of 5%, if M is around of 4 as shown in Fig. 5, this gives a latency of about 0.5 frames. However, the ratio k becomes larger at $QP = 32$. And also, M is typically larger for lower bitrates; i.e., for $QP = 32$. Therefore, the incurred delay is more challenging here; for example, for *FourPeople* at $QP = 32$, k is about 10 as shown in Fig. 6, which is relatively very high. Now for $M = 15$ (as inferred from Fig. 5), the delay becomes about 5.5 frames. For FPS of 60, it leads to a delay less than 100 ms which is acceptable for many applications. For smaller delays, we can combine the above two approaches; that is, applying coarser quantizer and forcing a delay. The coarser quantizer to I-frames leads to a smaller k which in turn leads to a smaller delay. 642
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VI. PERFORMANCE COMPARISON

657
 658 The analysis explained in the previous sections shows that using I-frames instead of applying IRR is more efficient as an error resiliency tool and gives higher quality in dealing with transmission of encoded videos over lossy channels. The 659
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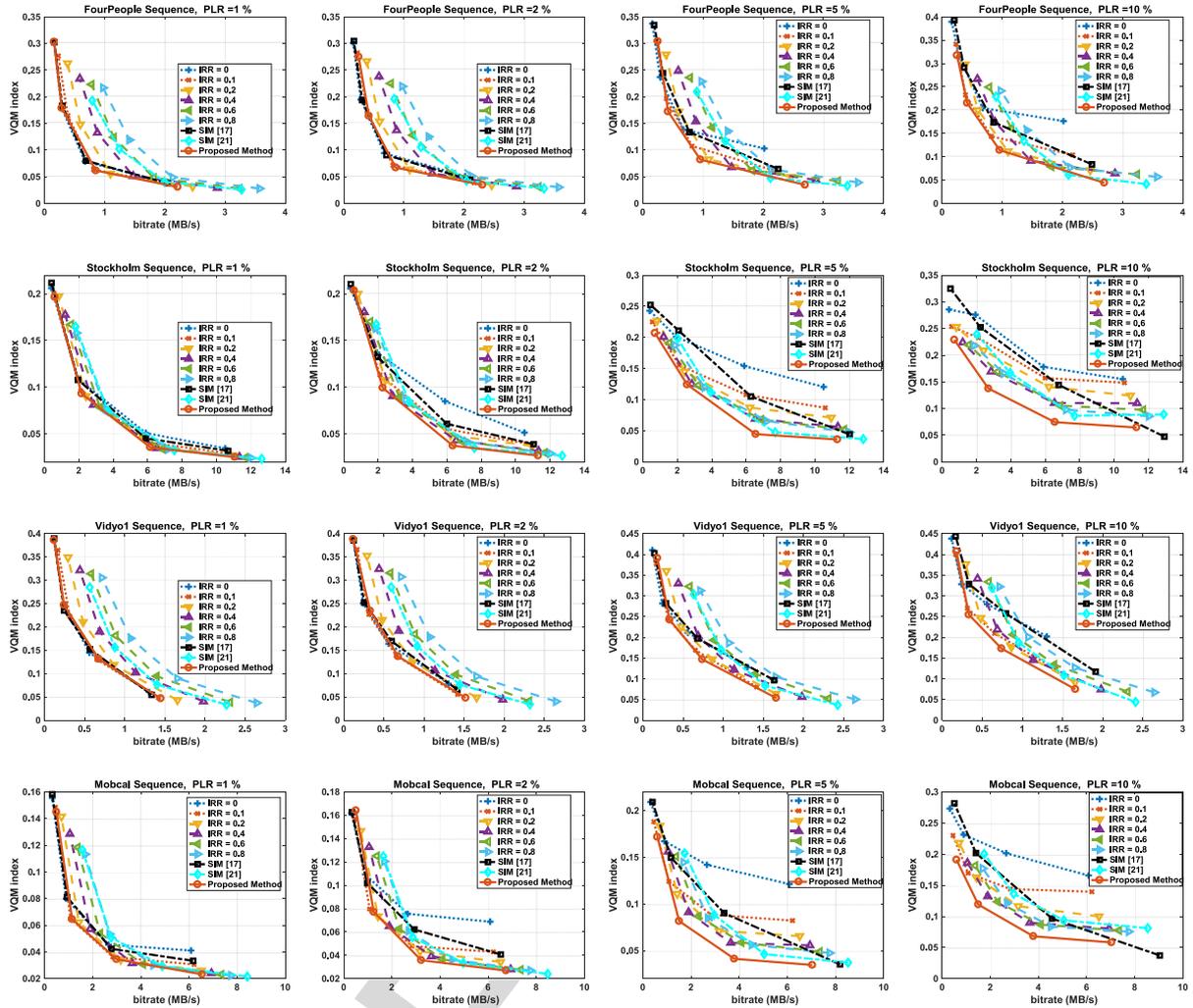


Fig. 7. Performance comparison of the proposed method for various PLRs and *FourPeople*, *Stockholm*, *Vidyo1* and *Mobcal* sequences for burst length of three packets.

suitable I-frame period is given by (22). As already mentioned in Section II, there are two other options for intra coding, SIM and Intra Refresh. For performance comparison, our proposed method is compared against two SIM methods, [17] and [21], where the PUs are selected based on an objective function for intra or inter coding. Note that as explained in Section II, there are also two options for selecting the blocks to be forced for intra coding in the Intra Refresh scheme. They can be selected randomly or in a regular manner, such as a column of intra blocks moving frame by frame from left to right. Our experiments showed that the latter option, called Periodic Intra Refresh (PIR) or cyclic intra-refresh generally gives superior performance in terms of rate-distortion. Therefore, we have included the results of PIR in Figs 7–9. Since there are no appropriate recent related works on the best value of IRR, we examine PIR with several possible values of IRR for all examined PLRs; these are {0, 0.1, 0.2, 0.4, 0.6, 0.8}. Note that $IRR = 0$ is equivalent to not paying any attention to channel loss at the encoder. With the experimental settings given in Section V, these results are shown in Figs 7–9, Fig. 9 is for the average burst length of six packets.

Despite of the simplifications and approximations made in our method through analysis and curve fitting, it can be seen from Figs 7–8 that our proposed method outperforms the others in many cases. For lower PLRs and smaller bitrates, the proposed method provides actually no gain. In these regions, since the video is less sensitive to packet loss, the curves are actually close to each other. The algorithm of [21] picks many PUs for intra coding; therefore, it applies intra rate much more than required but with a slight gain in quality in lower PLRs. For this reason, this algorithm does not work well for low PLRs. In the cases of higher PLRs and higher bitrates, one can see the VQM quality index of our proposed method is better than the others which is sometimes significant. A reminder that the smaller VQM index means higher quality. Light content video sequences, such as *FourPeople* and *KrisenAndSara*, as already mentioned are less sensitive to data loss; hence the VQM curves are again similar while ours are still marginally better.

For the PLRs of 5% and 10%, the results of applying average burst length of six packets are shown in Fig. 9. It can be seen that the performance of our proposed method is still better than the others. Actually, the loss pattern does not significantly affect our

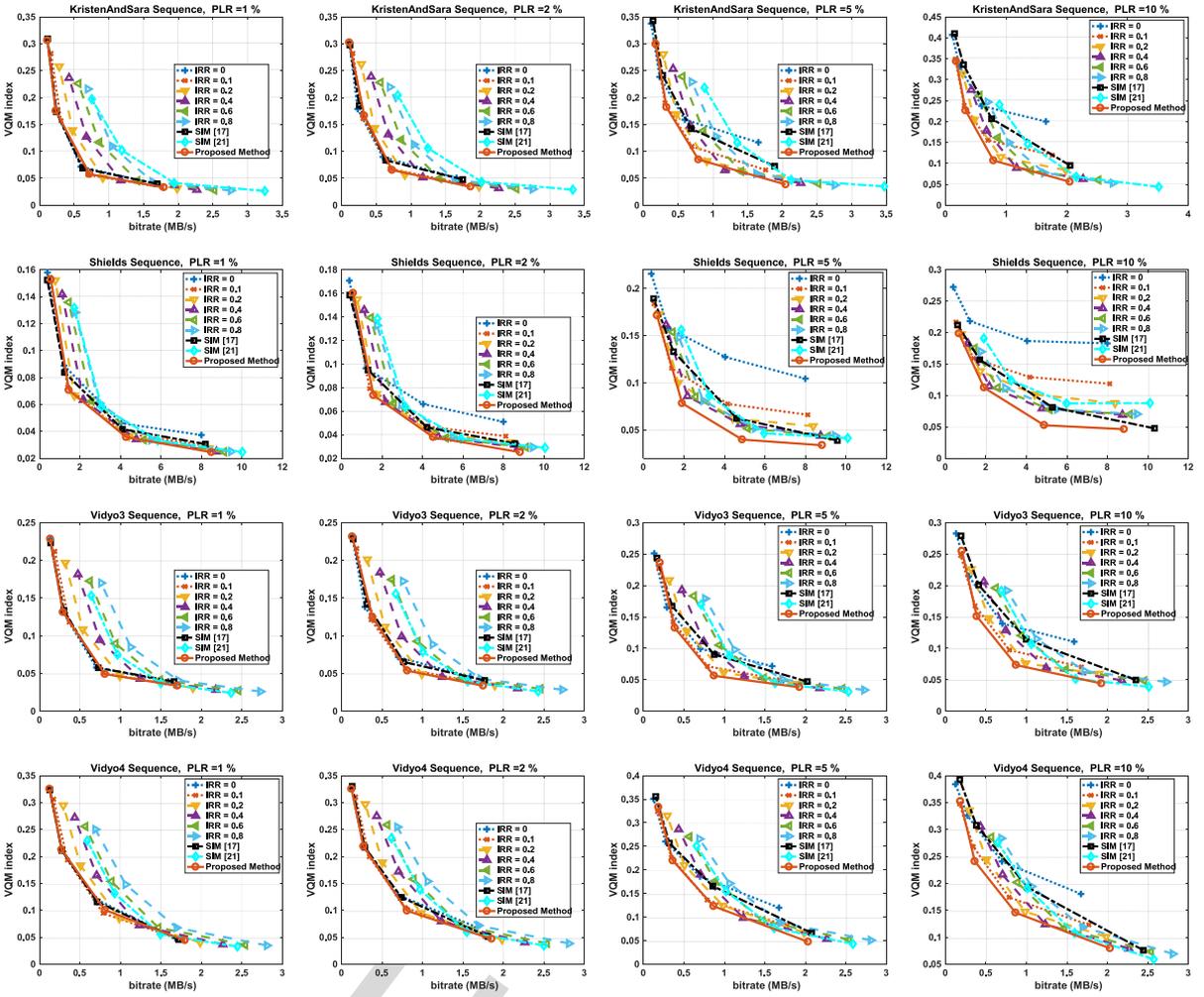


Fig. 8 Performance comparison of the proposed method for various PLRs and *Kristen and Sara*, *Shields*, *Vidyo3* and *Vidyo4* sequences for burst length of three packets.

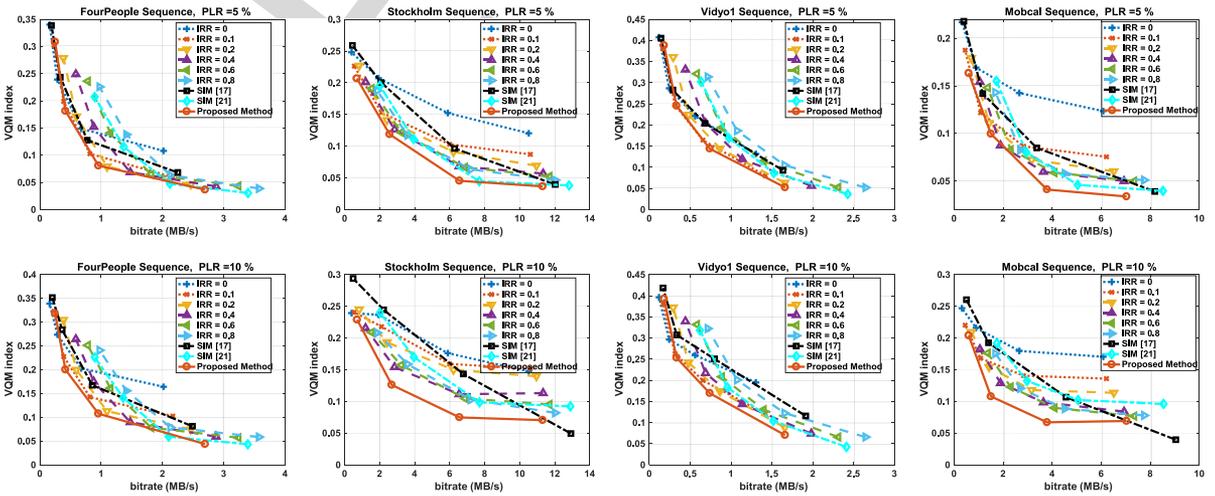


Fig. 9 Performance comparison of the proposed method for various PLRs and *FourPeople*, *Stockholm*, *Vidyo1* and *Mobcal* sequences for burst length of six packets.

704 results due to our loss concealment procedure applied to lossy
705 bitstreams generated by any of competing methods.

706 The burst loss leads to larger lossy areas in the pictures,
707 which is usually handled by the Motion Copy algorithm. Note
708 that burst loss will lead to the loss of consecutive frames in low
709 bitrate and low resolution videos, while it is not so destructive
710 for HD and beyond.

711 VII. CONCLUSION

712 In this paper, the best strategy for intra coding as an error
713 resiliency tool is presented. It was proposed to encode some
714 frames entirely in intra mode, rather than the conventional ap-
715 proach where some blocks or PUs are selected in PIR manner
716 (with a specific intra rate) or by a cost function to be coded in
717 intra mode. Considering the error propagation, the receiver side
718 distortion is formulated and it is simplified with some obser-
719 vations. The simplified objective function has a straightforward
720 solution: $\beta^{(i^*)} = 1$, where i^* is the index of the frames sym-
721 metrically positioned in the GoP, and the number of I-frames
722 depends on β_{red} or equivalently the available bitrate budget for
723 intra coding. The output of the objective function is to reduce
724 the IP as much as possible and as long as the bitrate overhead
725 of intra coding is justified at the given channel loss rate.

726 The optimal IP varies with the coding bitrate as well as the
727 PLR as shown in Fig. 5. We have fitted a curve to the experi-
728 mental points obtained from examining various test sequences,
729 as given in (22). With the IP^* selected by (22), experimental re-
730 sults show that the proposed method achieves lower VQM index
731 compared to the conventional SIM and PIR methods.

732 APPENDIX

733 Assume that frame 1 is transmitted through n packets. If m
734 packets are lost, the average distortion after error concealment
735 is:

$$D_m^{(1)} = \frac{(n-m)}{n} D_q^{(1)} + \frac{m}{n} D_{conceal}^{(1)} \quad (26)$$

736 If each packet is lost with a probability of PLR , the proba-
737 bility of losing m packets is

$$\begin{aligned} PLR_m &= C(n, m) PLR^m (1 - PLR)^{n-m} \\ &= \binom{n}{m} PLR^m (1 - PLR)^{n-m} \end{aligned} \quad (27)$$

738 where $C(n, m)$ is the number of m -combinations from n packets.
739 Therefore, the expected distortion of frame 1 is as given by (28):

$$\begin{aligned} D^{(1)} &= \sum_{m=0}^n \left(PLR_m D_m^{(1)} \right) \\ &= \frac{D_q^{(1)}}{n} \sum_{m=0}^n \left[(n-m) \binom{n}{m} PLR^m (1 - PLR)^{n-m} \right] \\ &\quad + \frac{D_{conceal}^{(1)}}{n} \sum_{m=0}^n \left[m \binom{n}{m} PLR^m (1 - PLR)^{n-m} \right] \end{aligned} \quad (28)$$

740 Both summations in (28) are the expected values of a *Bino-*
741 *mial* distribution with probabilities of $(1 - PLR)$ and PLR ,
742 respectively. That is $D^{(1)}$ becomes

$$\begin{aligned} D^{(1)} &= \frac{D_q^{(1)}}{n} [n(1 - PLR)] + \frac{D_{conceal}^{(1)}}{n} [n PLR] \\ &= (1 - PLR) D_q^{(1)} + PLR D_{conceal}^{(1)} \end{aligned} \quad (29)$$

743 which is the same as equation (2).

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Intra Coding Strategy for Video Error Resiliency: Behavioral Analysis

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Abstract—One challenge in video transmission is to deal with packet loss. Since the compressed video streams are sensitive to data loss, the error resiliency of the encoded video becomes important. When video data is lost and retransmission is not possible, the missed data should be concealed. But loss concealment causes distortion in the lossy frame which also propagates into the next frames even if their data are received correctly. One promising solution to mitigate this error propagation is intra coding. There are three approaches for intra coding: intra coding of a number of blocks selected randomly or regularly, intra coding of some specific blocks selected by an appropriate cost function, or intra coding of a whole frame. But Intra coding reduces the compression ratio; therefore, there exists a trade-off between bitrate and error resiliency achieved by intra coding. In this paper, we study and show the best strategy for getting the best rate-distortion performance. Considering the error propagation, an objective function is formulated, and with some approximations, this objective function is simplified and solved. The solution demonstrates that periodical I-frame coding is preferred over coding only a number of blocks as intra mode in P-frames. Through examination of various test sequences, it is shown that the best intra frame period depends on the coding bitrate as well as the packet loss rate. We then propose a scheme to estimate this period from curve fitting of the experimental results, and show that our proposed scheme outperforms other methods of intra coding especially for higher loss rates and coding bitrates.

Index Terms—Error resilient video coding, video error concealment, intra coding.

I. INTRODUCTION

NOWADAYS, real-time digital video transmission over networks is very popular. Due to the tremendous volume of the raw video data, video compression is inevitable. But delivering compressed data over wired/wireless channels is challenging

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since the underlying networks are not always reliable and some data losses are usually experienced during transmission.

The erroneous and unreceived data corrupts the decompression process and the video fidelity. In this condition, using error concealment techniques alleviates the problem to some extent [1]. At high compression rates, data loss is more destructive; the higher the compression, the more the sensitivity to data loss. For this reason, High Efficiency Video Coding (HEVC), the latest standard video codec, is less error resilient than H.264/AVC [2]. Therefore, this makes HEVC video communication over error prone channels a challenging problem for researchers and practitioners in this field.

In error concealment techniques, the non-received data are estimated from the received ones. This is done by exploiting the spatio-temporal correlations among the available data at the area of missing information. However, the replaced data will not be exactly the same as the actual data; therefore, there exists a mismatch/distortion between them. If the recovered frame was used as the prediction reference at the encoder, its reconstructed erroneous part would propagate into the next frames at the decoder. In video coding, a large portion of compression comes from inter frame coding, but inter frame coding increases inter dependency and causes error propagation. In contrast, although intra coding is less efficient for compression, it mitigates the error propagation problem and could be used as a strong error resiliency tool, since it does not use prediction from the other frames [3]–[6]. Therefore, by intra coding, there is a trade-off between error resiliency and compression ratio. That is, intra mode for a block must be selected with sufficient care. For this reason, loss resiliency through intra mode is discussed in several works, as described in Section II.

In this paper we show both analytically and experimentally that the best strategy for intra coding is to code some selected frames deliberately in intra mode. For doing so, considering the transmission distortion, the decoder side distortion is formulated and an objective function is developed. Through optimization of this objective function, the optimal solution indicates that coding a whole frame as an I-frame is preferred over coding a certain number of blocks in the frames as intra mode. Our investigations show that the best approach to exploit the error resiliency of intra coding is to reduce the intra period instead of distributing the intra coded blocks among the frames. We had solved a similar problem for Multiple Description Coding (MDC) in [32], but the treatment of a single stream is different from the multi streams of MDC. MDC rarely deals with concealment distortion, since most of the time at least one description is available. Therefore,

the objective functions and approaches taken for solving the problem here are different from [32].

The rest of the paper is structured as follows. Section II presents the related work, while in Section III the objective function is formulated. Through experimental results, this function is first simplified and then solved in Sections IV and V. The performance comparison with the other approaches for error resilient intra coding is presented in Section VI and the paper is concluded in Section VII.

II. RELATED WORK

In the works presented in [7], [8], a recursive algorithm called ROPE has been developed. In this algorithm, by pixel-wise operations, the encoder estimates the receiver-side expected distortion which is then used for intra/inter mode decision. However, this algorithm is too complex due to its pixel-by-pixel computations. Its extension for bursty loss channels is presented in [9], and the extension of error resilient mode decision to motion estimation and also considering intra-frame prediction for intra modes is presented in [10]. ROPE was also used in [11] to optimally decide between Motion Vector (MV) replication or intra coding mode. Using ROPE for motion estimation and reference frame generation is presented in [12], while [13] discusses the intra/inter mode selection in video transcoding, where the lossy frame and its propagated error within the ROPE algorithm is exploited. Finally, the extension of ROPE for including constrained intra prediction as candidate modes, in addition to inter and intra modes, is presented in [14].

In another proposal described in [15], frame-level channel distortion is analyzed, where through linear models/approximations and end-to-end distortion optimization, a scheme for intra mode selection and rate control is developed. Some models for transmission distortion are presented in [16] where parameters such as intra prediction, deblocking filtering, sub-pixel motion estimation and the effect of decoder side temporal error concealment are taken into account. With the same approach, an end-to-end distortion modeling and optimization method was presented in [17] which is then used to develop a faster algorithm for intra/skip mode decision [18], [19]. In [20], motion estimation and mode decision in HEVC are performed based on error propagation. Another algorithm is presented in [21] where due to high sensitivity to error propagation, the algorithm selects the intra mode for the Prediction Units (PUs) much more than is required, especially for lower content videos. Even though the authors try to solve this issue with updating some parameters, the intra rates are still high and this degrades its performance at low Packet Loss Rates (PLRs) and low bitrates.

A fast intra mode decision for loss resiliency is developed in [22] where, through a linear model, the distortion is estimated and an optimal value for Intra Refresh Rate (IRR) is obtained. IRR or simply the intra rate is the number of blocks coded in intra mode divided by the total number of blocks in the frame. A modified model for considering the role of IRR in bitrate and distortion is introduced in [23]. Using a linear model and considering motion activity and PLR, the optimal IRR and the intra coded MBs' pattern are discussed in [24]. It is shown in [25]

that for low activity sequences, cyclic intra coding of MBs is more effective than periodic I-frames, and vice-versa for highly active videos. Combining cyclic intra-refreshing with unequal error protection is introduced in [26], [27], though intra-refresh is in conflict with multiple reference selection, as shown in [28]. Error propagation is formulated and the IRR is obtained in [29], then the selected MBs for intra coding are grouped into a common slice group where they are then protected with stronger channel codes.

The above mentioned intra coding research works can be categorized into two groups: those which discuss Selecting Intra Mode (SIM) and those which discuss Intra Refresh. In SIM methods, the cost function for inter/intra mode decision is modified to take into account the lossy channel and the transmission distortion; examples are [7]–[21]. In Intra Refresh, the intra rate is determined. Then, the intra coded blocks can be selected randomly, or selected with vertically or horizontally ordered columns/rows, provided that they do not overlap in the successive frames such that the blocks in all positions are intra refreshed after a while; examples are [22]–[29].

Our work is different from the above works since our formulation and optimization leads to a straightforward and specific solution: reduce the intra period (coding a whole frame in intra mode) to achieve the best error resiliency outcome of intra coding, instead of distributing the intra coded blocks within the frames of the GOP. Afterwards, the best intra period, which depends on the content and channel loss rate, is approximately but simply obtained from a function, without additional computational complexity. The experimental results confirm the efficient performance of the proposed scheme, for various loss rates and video contents.

Another tool which can help to prevent error propagating is Reference Picture Selection (RPS) which allows the encoder to select one or two frames from a list as inter-prediction references for each prediction block. Several reference frames are examined for the best rate-distortion coding. For error resiliency, this feature is usually in conjunction with decoder feedback which informs the encoder not to select the erroneously received frames as the prediction reference [42], [43]. However, this feedback information is not available in many applications; e.g., multicast and broadcast applications, or pre-recorded video on demand applications. Moreover, responding to various receivers concurrently is not practical, or the feedback messages might be received too late. RPS without a back channel and for error resiliency has been presented in [44]. In this work, the authors propose not to use a single frame as prediction reference of the PUs, but to select from a list of reference frames such that all frames in the list are selected uniformly. However, this method needs to consider a list of frames as candidate reference frames, so it has the complexity of the multi-reference prediction. For example, for five candidate reference frames, the computational complexity of Motion Estimation and Mode Decision becomes five times more. The required encoder/decoder buffer size becomes larger with the number of reference frames as well. In the error resiliency of the intra coding method proposed in our paper, the only required information is channel loss rate, without any additional complexity in the encoder/decoder. It is worth

noting that full frame intra prediction provides random access to video stream, but it also generates large peaks of bitrates. However, such large spikes in the bitrate can be eased with either a few frames delay, which is acceptable in many applications, or compensated by statistical multiplexing with lower bitrates of P- and B-frames of other video streams. Therefore, there are many circumstances that intra coding is a feasible solution while RPS cannot be employed.

Our application scenario is distribution/broadcast of video without assuming any specific limits on delay or bandwidth, and assuming the PLR is known by the encoder. PLR can be estimated with or without back channel. The application scenario without back channel compromises the great majority of current video distribution/broadcast systems today. In such a scenario, we assume PLR is estimated by the service/network operator from the history of the channel for the specific weekday and time of the day, or is calculated offline, or is tested by small ping packets periodically, or by traffic modeling [30], or by one-way estimation methods that use message segment size, goodput, and delay [31] all estimated at the sender side, or by any other estimation means. Of course PLR can also be estimated with back channel, and this would be more accurate. In the latter scenario, our proposed method is applicable if this back channel cannot inform us of the lost packets immediately due to the delay in feedbacks or a long Round-Trip Time; therefore, retransmission of the lost data or Reference Picture Selection is not possible. This scenario is also assumed by other credible works [8], [13], [15], [17], [21]. Finally, since our method introduces a small delay of about 92 msec, as will be shown later in the paper, we assume that such small delay is acceptable for the target application.

III. THE OBJECTIVE FUNCTION FOR ERROR RESILIENT INTRA CODING

For error resilient coding, the following two aspects of intra coding must be considered:

First aspect - intra coding prevents temporal error propagation, since it has no reference to the other frames. In intra coding of advanced video codecs, such as H.264/AVC and H.265/HEVC, pixels of the adjacent blocks are used as intra prediction references, and these references (in encoded form) together with the residual data are encapsulated and transmitted in a single packet. However, if the reference pixels had been encoded in inter mode, they themselves might be erroneous, even if the residual data is received correctly. In this case, temporally propagated errors can propagate spatially into the intra-coded blocks. To avoid this condition and exploit the error propagation prevention provided by intra coding, the option of ‘‘Constrained-IntraPred’’ can be enabled, which restricts the intra mode to use only the pixels of adjacent intra coded blocks as prediction references. This way, the received intra coded PUs are correctly decodable.

Second aspect - in no loss conditions, inter mode is obviously used more often than intra mode, because inter-coded blocks have lower bitrates than intra coded ones. By enabling the ‘‘ConstrainedIntraPred’’ option, the compression efficiency

of intra mode is reduced even more, but it is beneficial for error resiliency [16] when we do have losses.

Therefore, in deciding to code a block in intra mode, there is a trade-off between bitrate and error resiliency. In this section, an objective function is developed which, rather than optimizing the encoder side rate-distortion, the decoder side rate-distortion is optimized. In other words, taking into account the channel distortion, the receiver side distortion is estimated at the encoder which is then used as the objective function.

Intra/inter mode selection is conventionally carried out based on the following Lagrangian cost function [33], [34]:

$$cost = D_q + \lambda R \quad (1)$$

where D_q is the quantization distortion in Mean Squared Error (MSE), λ is the Lagrangian coefficient and R is the number of required bits. This cost function is computed for the candidate modes and the mode with the lowest cost is selected as the final mode. However, this cost function does not take the transmission distortion into account. To consider it, with the same approach as presented in [15]–[17], the rate overall-distortion in a frame is represented in (2). The assumption behind this equation is that PLR is known at the transmitter side.

$$D^{(1)} = (1 - PLR) D_q^{(1)} + PLR D_{conceal}^{(1)} \quad (2)$$

where $D^{(1)}$, $D_q^{(1)}$ and $D_{conceal}^{(1)}$ are the expected total distortion, the quantization distortion, and the error concealment distortion for frame 1, respectively. The *expected* distortion means the average distortion seen over a long enough duration, or equivalently over a variant enough packet loss pattern, the latter used in our simulation. Note that the concealment distortion, $D_{conceal}$ in (2), is the distortion when all packets of the frame are lost and the frame is error concealed. It is evident that the frame is transmitted by a single packet; however, as shown in the Appendix, this is also valid when the frame is encoded into n packets and the packets convey the same amount of information.

Frame 0 is the initial I-frame of the sequence which is assumed to be received correctly. For frame 1, depending on whether its packets are received or not, the distortion will be $D_q^{(1)}$ or $D_{conceal}^{(1)}$, respectively. For frame 2, it becomes:

$$D^{(2)} = (1 - PLR) D_q^{(2)} + PLR D_{conceal}^{(2)} + PLR [1 - \beta^{(2)}] \Delta^{(1)} \quad (3)$$

where $\beta^{(2)}$ is the intra rate of frame 2 and

$$\Delta^{(1)} = E \left[\left(F_q^{(1)} - F_{conceal}^{(1)} \right)^2 \right] \quad (4)$$

is the mean squared difference between frame 1 decoded correctly ($F_q^{(1)}$) and loss concealed ($F_{conceal}^{(1)}$); i.e., $\Delta^{(1)}$ denotes the *Mismatched Distortion* for frame 1 caused by error concealment. We assume that only the previous frame is used as prediction reference, as happens most of the times in encoders. Enabling multi-frame prediction results in a slight improvement in quality but at the cost of significant computational cost.

Equations (3) and (4) show that the quality of frame 1 directly affects the quality of frame 2, and its effect is controlled by

parameter $\beta^{(2)}$ in (3). At larger β , the impact of mismatched distortion is clearly reduced, since intra coded PUs do not refer to the previous frame. As shown in [15], the quantization and mismatched distortions are independent of each other and one can simply write:

$$D_{conceal}^{(2)} = D_q^{(2)} + \Delta^{(2)} \quad (5)$$

Substituting (5) into (3) gives:

$$\begin{aligned} D^{(2)} &= D_q^{(2)} + PLR \left[\Delta^{(2)} + (1 - \beta^{(2)}) \Delta^{(1)} \right] \\ &= D_q^{(2)} + PLR \Delta_{accum}^{(2)} \end{aligned} \quad (6)$$

in which

$$\Delta_{accum}^{(2)} = \Delta^{(2)} + (1 - \beta^{(2)}) \Delta^{(1)} \quad (7)$$

is the *Accumulated Mismatched Distortion* seen in frame 2. It is evident that for frame 1, $\Delta_{accum}^{(1)} = \Delta^{(1)}$ and then (7) can be rewritten as:

$$\Delta_{accum}^{(2)} = \Delta^{(2)} + (1 - \beta^{(2)}) \Delta_{accum}^{(1)} \quad (8)$$

Following the above concept, the distortion for the n th frame is:

$$D^{(n)} = D_q^{(n)} + PLR \Delta_{accum}^{(n)} \quad (9)$$

where

$$\begin{aligned} \Delta_{accum}^{(n)} &= \Delta^{(n)} + (1 - \beta^{(n)}) \Delta_{accum}^{(n-1)} \\ \Delta_{accum}^{(0)} &= 0 \end{aligned} \quad (10)$$

and

$$\Delta^{(n)} = E \left[\left(F_q^{(n)} - F_{conceal}^{(n)} \right)^2 \right] \quad (11)$$

Therefore, the distortion over a GoP of N frames is as given in (12) (as already mentioned, the 0th frame of the GoP is excluded from the summation):

$$D_{GoP} = \sum_{i=1}^N D^{(i)} = \sum_{i=1}^N \left(D_q^{(i)}(\beta) + PLR \Delta_{accum}^{(i)}(\beta) \right) \quad (12)$$

where $\beta = [\beta^{(1)}, \beta^{(2)}, \beta^{(3)}, \dots, \beta^{(N)}]$ is the vector intra rates for the N frames of the GoP. Quantization Parameter (QP) is excluded from this formulation, since its variation is usually ± 1 units at the given bitrate, except for sudden changes; e.g., scene-cut or fast/non-translational motions which is difficult for compensation with inter prediction. Therefore, we can assume that QP does not have significant changes for the N frames under consideration.

With the aim of maximizing the received video quality, the objective function with a constraint on the overhead bitrate of intra coding is:

$$\begin{aligned} \min_{\beta} & \left\{ \sum_{i=1}^N \left(D_q^{(i)}(\beta) + PLR \Delta_{accum}^{(i)}(\beta) \right) \right\} \\ \text{s.t.} & \sum_{i=1}^N R_{intra}^{(i)}(\beta) \leq R_{red} \end{aligned} \quad (13)$$

where $R_{intra}^{(i)}$ is the number of additional bits needed for intra encoding of the i th frame according to the intra rate of $\beta^{(i)}$; that is, if $\beta^{(i)} = 0$, then $R_{intra}^{(i)} = 0$ and no block is coded in intra mode for error resiliency. The term R_{red} in (13) is the total redundancy budget allowed for these N frames for intra coding, which in turn is related to the PLR and the required degree of error resiliency. Increasing the intra rates of frame i ; i.e., $\beta^{(i)}$, reduces $\Delta_{accum}^{(i)}$ (see equation (10)) but in turn increases bitrate usage.

IV. SOLVING THE OBJECTIVE FUNCTION

In this section, a solution to the constrained problem of (13) is driven through approximation. The behaviors of terms in this equation are observed and approximated through matching them to the experimental results. The experiments settings, the simplifying approximations, and the solution to the problem are provided in subsections A, B and C, respectively.

A. The Error Concealment Strategy

An important part of distortion in (13) belongs to the distortions caused by error/loss concealment. Error concealment techniques can be categorized into spatial and temporal domain processing techniques. In the spatial domain, the lost area of the frame is concealed using the spatially neighboring pixels. These methods exploit the correlations that usually exist among the neighboring pixels. In the temporal processing techniques, the contents from the previous and/or the future frames are addressed by MVs and used for temporal replacement. The actual MVs are not available and must be estimated or recovered first by the temporal loss concealment methods.

If the lost area is large, spatial domain is not effective, as pixels are very far apart from each other to be useful. The reason for dealing with large lost areas in HEVC is the size of its Coding Tree Unit (CTU), which can be as large as 64×64 pixels. An integer number of CTUs are regarded as one slice and an integer number of slices are encapsulated into a single transmission packet. Therefore, packet losses in HEVC streams affect a significant portion of the picture area especially for smaller picture sizes. As a result, temporal error concealment in HEVC streams is more applicable than spatial concealment.

Actually, exploiting the temporal frames' MVs will provide higher quality error concealment. One simple yet efficient technique is the Motion Copy algorithm where the MV of the collocated block is simply used for motion compensated temporal replacement. If the collocated block is coded in intra mode, Zero MV is used. However, in the case of having a high percentage of intra coded blocks, this approach is not efficient due to lack of MVs for intra blocks. For intra coded blocks, one solution is to recover the MVs by Boundary Matching Algorithm (BMA). A suggestion is to combine Motion Copy for inter coded and reliable collocated blocks, and BMA for intra coded or unreliable collocated blocks, as presented in [35]. The blocks with high residual signals are labeled as unreliable blocks and their MVs are not used for MV recovery. In [35], loss concealment is performed in two stages: firstly, the lost area is replaced using the Motion Copy algorithm. Then, for the unreliable MVs,

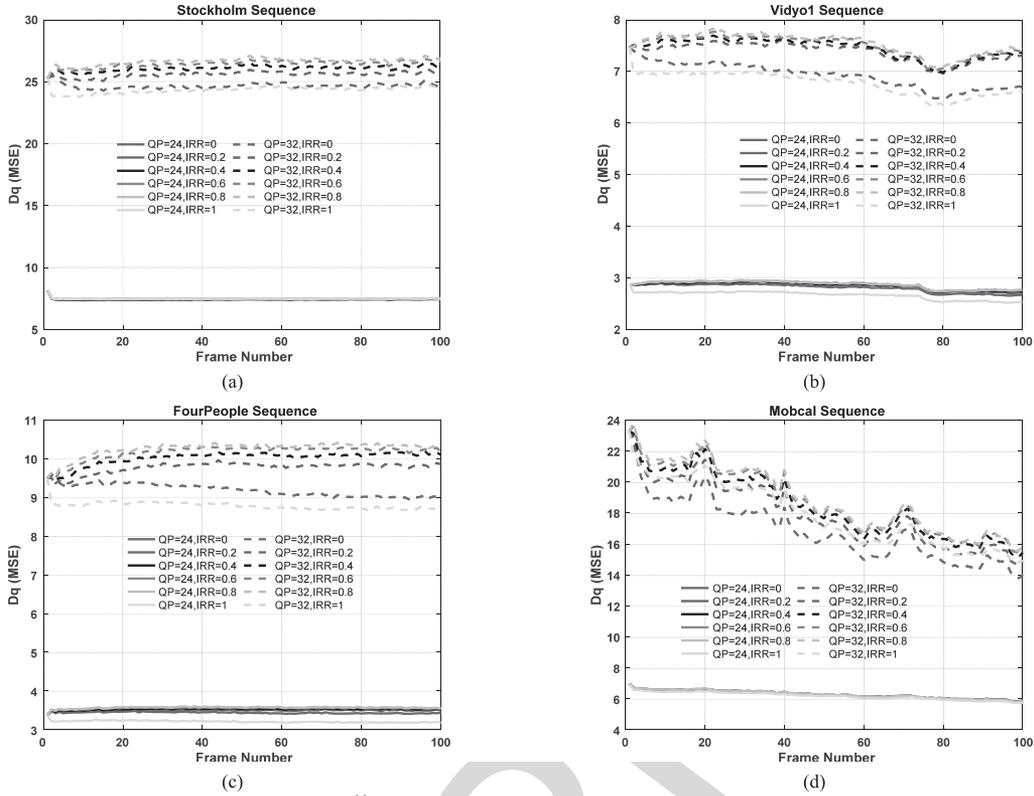


Fig. 1. The variation of $D_q^{(i)}(\beta^{(i)})$ with respect to IRR for test sequences and two values of QP .

376 MVs are obtained using BMA. Some other methods such as
 377 [36]–[37] are proposed for HEVC error concealment, but they
 378 work again based on the spatially close boundary pixels, which
 379 are not always available in the actual scenarios. The algorithm
 380 presented in [38] works based on MV extrapolation but with
 381 applying higher weights to the MVs belonging to the larger parti-
 382 tions. However, the problem is that this algorithm is based on
 383 the MVs of the blocks of the previous frame and therefore it is
 384 efficient when there are a few intra coded blocks. The method of
 385 [39] is proposed for error concealment of a sequence of succes-
 386 sive MBs in H.264/AVC. This error concealment method does
 387 not need to know the MVs’ neighboring spatially or tempo-
 388 rally missed blocks, and instead estimates them by BMA. This
 389 method is also useful for large area losses of HEVC. The chal-
 390 lenge in using BMA is the fact that the error concealment of one
 391 block will affect the error concealment of the following blocks
 392 as well. One solution, proposed in [39], is rank ordering the MBs
 393 for error concealment based on the texture of the available MBs
 394 in the surrounding of the lost area. A missed MB with a higher
 395 texture around it will be error concealed with higher priority.
 396 The criterion for the higher texture is the standard deviation of
 397 the luminance pixel values. Another solution for considering the
 398 interaction of loss concealed blocks is presented in [40], but it
 399 imposes significant computational complexity without consid-
 400 erable improvement.

401 In this paper, three techniques are used for error concealment:
 402 Motion Copy, the method presented in [35], and the method
 403 presented in [39]. The first two methods are appropriate when

404 the blocks in the earlier frame are encoded mostly in inter mode,
 405 and the third method is suitable when the blocks in the earlier
 406 frame are encoded mostly or completely in intra mode. Then, the
 407 highest quality output is selected and used for the measurements.

408 It is worth noting that throughout the paper error concealment
 409 and loss concealment are used interchangeably, but in fact loss
 410 concealment is carried out. The reason is that in highly error
 411 prone networks, such as wireless networks, severely erroneous
 412 packets cannot be corrected and they are regarded as lost packets
 413 by the decoder. However, if the used entropy coder is symmetric,
 414 such as that of the H.263 codec, then parts of the data can be
 415 retrieved and the lossy area can be less than that of whole packet
 416 loss [45]. Since H.265/HEVC does not use symmetric entropy
 417 coder, then there would not be any retrieval of erroneous parts
 418 and the whole packet can be regarded as lost. Hence, loss con-
 419 cealment is a proper choice.

B. Simplifying the Objective Function

420
 421 First, the quantization distortion does not significantly change
 422 with parameter $\beta^{(i)}$. That is, $D_q^{(i)}(\beta^{(i)})$ is approximately
 423 constant when $\beta^{(i)}$ varies from minimum ($\beta = 0$) to maximum
 424 ($\beta = 1$). This can be verified from the simulation results shown
 425 in Fig. 1. In this figure, four HD test video sequences are coded
 426 with HM16.0, the reference software of HEVC, at two values
 427 of QP and six values of IRR. The tested video sequences are
 428 *Stockholm*, *Vidyo1*, *FourPeople* and *Mobcal*. For the given intra
 429 rates, a sufficient number of PUs with sizes of 16×16 pixels

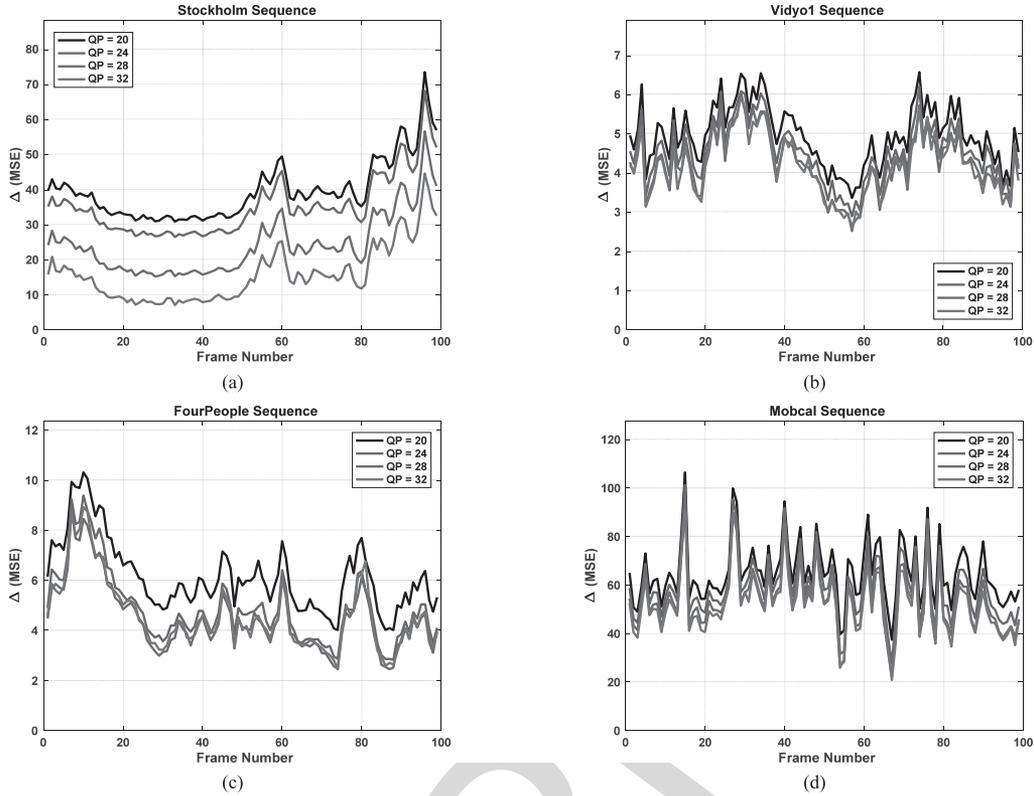


Fig. 2. The variation of mismatched distortion ($\Delta^{(i)}$) for the frames of test sequences for four values of QP .

430 are selected randomly and are forced to intra coding mode. As
 431 already mentioned, the randomly selected PUs do not overlap in
 432 the frames.

433 Fig. 1 shows the ignorable changes of $D_q^{(i)}$ with $\beta^{(i)}$. It can
 434 also be seen that the variation in $D_q^{(i)}$ for $QP = 24$ is less than
 435 that of $QP = 32$. The mathematical reason is that for smaller
 436 QPs , or smaller quantization step sizes (Q_{SS}), the high bitrate
 437 approximation is more accurate and the quantization distortion
 438 is nearly equal to $\frac{Q_{SS}^2}{12}$ [17]. This is fixed for various signals,
 439 independent of inter or intra coding. However, the difference
 440 in $D_q^{(i)}$ s for various β s is still ignorable, even for $QP = 32$.
 441 Therefore, $D_q^{(i)}$ is fixed with the optimization arguments and
 442 equation (13) can be simplified as:

$$\begin{aligned} \min_{\beta} & \left\{ \sum_{i=1}^N \left(PLR \Delta_{accum}^{(i)}(\beta) \right) \right\} \\ \text{s.t.} & \sum_{i=1}^N R_{intra}^{(i)}(\beta) \leq R_{red} \end{aligned} \quad (14)$$

443 An important term in (14) is $\Delta_{accum}^{(i)}$ which is the multiply-
 444 accumulated of mismatched distortions $\Delta^{(i)}$ s, with the multipli-
 445 cation coefficient of $(1 - \beta^{(i)})$, as given in (10). Therefore, the
 446 variation of $\Delta^{(i)}$ per frames is important in the behavior of the
 447 objective function of (13). To measure $\Delta^{(i)}$ s, the frames are first
 448 error concealed with the strategy given in IV.A, and then $\Delta^{(i)}$ is
 449 calculated by (11). The results are shown in Fig. 2 where it can be
 450 seen that, most of the times and with a good approximation, the
 451 frames of a sequence have close mismatched distortions, that is:

$$\Delta^{(1)} \cong \Delta^{(2)} \cong \dots \cong \Delta \quad (15)$$

452
 453 Even though it might not be valid for all frames, the variations
 454 are smooth in the windows of N frames, as large as the usually
 455 used GoP sizes (30–60 frames). This assumption may not be
 456 much accurate; however, this assumption, by nature, is similar
 457 to the assumption made in Rate-Control (RC) algorithms. In
 458 RC algorithms, the goal is to control the total bitrate to be less
 459 than the given bound with minimum fluctuation in the quality.
 460 Therefore, for a real-time RC, the encoder must assume that the
 461 future frames have almost the same behavior in the view of com-
 462 pression properties. Even though this assumption is not always
 463 valid, it is very efficient and helpful in practice. Similar to RC
 464 algorithms, we can assume that the frames behave similarly in
 465 the view of mismatched distortion. Therefore, with the assump-
 466 tion of (15), $\Delta^{(i)}$ is fixed for the frames, and since the employed
 467 loss concealment strategy is not much sensitive to the intra/inter
 468 coding, it is also fixed with β . Therefore, by substituting the
 469 recursive formula given in (8), the objective function of (14) can
 470 be expanded as follows:

$$\begin{aligned} \min_{\beta} & \left\{ PLR \cdot \Delta \left[N + \sum_{i=1}^N \left(\sum_{j=1}^{N-(i-1)} \left(\prod_{k=0}^{i-1} (1 - \beta^{(j+k)}) \right) \right) \right] \right\} \\ \text{s.t.} & \sum_{i=1}^N R_{intra}^{(i)}(\beta) \leq R_{red} \end{aligned} \quad (16)$$

where PLR and Δ are assumed constant during optimization.

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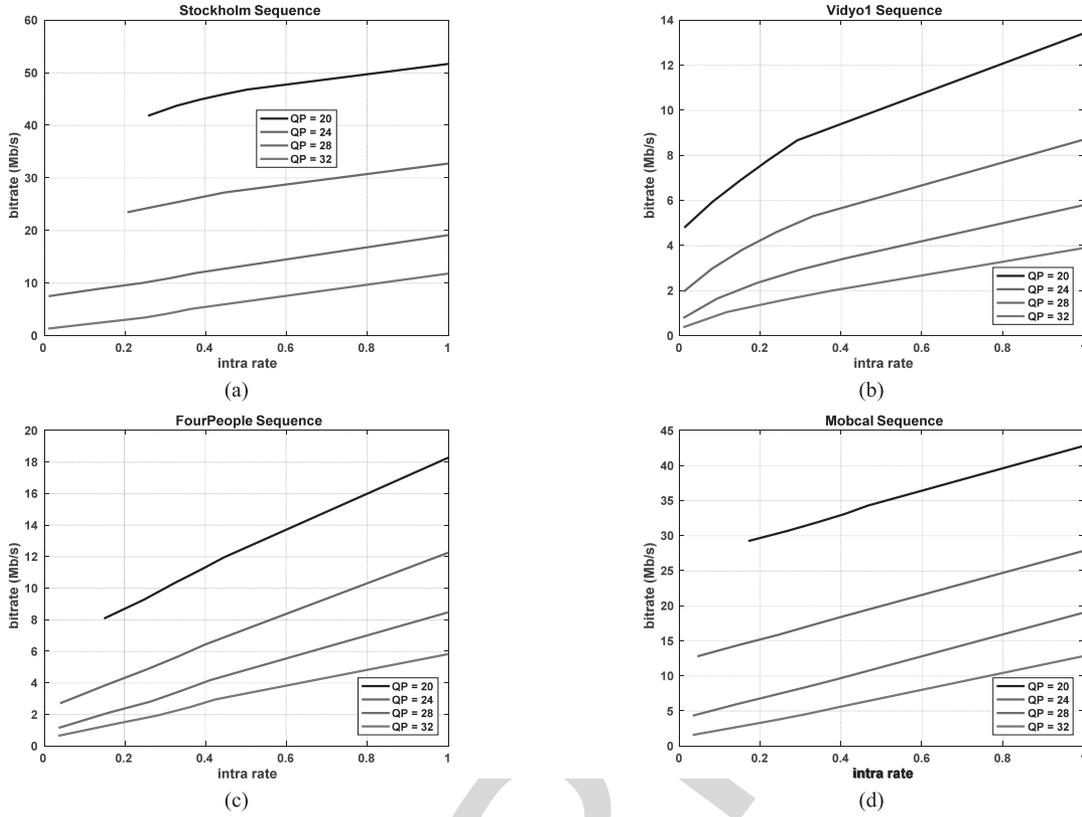


Fig. 3. The variation of bitrate with intra rate for various QPs and test sequences.

472 Now, for the constraint of (16), we do another simulation: the
 473 variation of frame bits when β varies from 0 to 1, as depicted in
 474 Fig. 3. In this figure, the average bitrates needed for sending the
 475 encoded video frames are measured and shown against the intra
 476 rate.

477 From Fig. 3, we can generally assume that the bitrates are
 478 increased almost linearly with β . That is:

$$\begin{aligned} R^{(i)} &= R_0^{(i)} + R_{intra}^{(i)} = R_0^{(i)} + \alpha^{(i)} \beta^{(i)} \\ \Rightarrow R_{intra}^{(i)} &= \alpha^{(i)} \beta^{(i)} \end{aligned} \quad (17)$$

479 where $R_0^{(i)}$ is the bitrate of the i^{th} frame for $\beta = 0$. The figure
 480 shows that the curves almost have the same slope; that is, they
 481 have the same α defined in (17). For this reason, the constraint
 482 term in (16) can be stated as:

$$\sum_{i=1}^N \left(\alpha \beta^{(i)} \right) \leq R_{red} \quad (18)$$

483 or equivalently

$$\sum_{i=1}^N \beta^{(i)} \leq \beta_{red} \quad (19)$$

484 where β_{red} is the intra rate budget; i.e., the sum of total intra
 485 rates allowed to be assigned to these N frames. Therefore, the

objective function of (16) is simplified as

486

$$\begin{aligned} \min_{\beta} & \left\{ PLR \cdot \Delta \left[N + \sum_{i=1}^N \left(\sum_{j=1}^{N-(i-1)} \left(\prod_{k=0}^{i-1} (1 - \beta^{(j+k)}) \right) \right) \right] \right\} \\ \text{s.t.} & \sum_{i=1}^N \beta^{(i)} \leq \beta_{red} \end{aligned} \quad (20)$$

487 Since we can assume that PLR and Δ are fixed during opti-
 488 mization, the problem in (20) can be rewritten as:

487

488

$$\begin{aligned} ErrorPro_{min} &= \min_{\beta} \left\{ \sum_{i=1}^N \left(\sum_{j=1}^{N-(i-1)} \left(\prod_{k=0}^{i-1} (1 - \beta^{(j+k)}) \right) \right) \right\} \\ \text{s.t.} & \sum_{i=1}^N \beta^{(i)} \leq \beta_{red} \end{aligned} \quad (21)$$

489 It is worth mentioning that for simplicity of deriving the objec-
 490 tive function, without loss of generality, there are no B-frames.
 491 This is because, in general, some B-frames maybe used as pre-
 492 diction reference like P-frames causing error propagation, while
 493 others are not used as the reference and hence do not propagate
 494 the errors but they become erroneous. Modifying our formulati-
 495 ons to highlight this matter makes the equations more compli-
 496 cated without giving the required information to the reader.

TABLE I
THE OUTPUT OF THE OBJECTIVE FUNCTION OF (21) FOR SOME VALUES OF β_{red}

Range of β_{red}	Intra rate of the frames															Constraint
	$\beta^{(1)}$	$\beta^{(2)}$	$\beta^{(3)}$	$\beta^{(4)}$	$\beta^{(5)}$	$\beta^{(6)}$	$\beta^{(7)}$	$\beta^{(8)}$	$\beta^{(9)}$	$\beta^{(10)}$	$\beta^{(11)}$	$\beta^{(12)}$	$\beta^{(13)}$	$\beta^{(14)}$	$\beta^{(15)}$	
$\beta_{red} \leq 1$	0	0	0	0	0	0	0	a_1	0	0	0	0	0	0	0	$a_1 = \beta_{red}$
$1 < \beta_{red} \leq 1.45$	0	0	0	a_1	0	0	0	1	0	0	0	a_2	0	0	0	$a_1 + a_2 = \beta_{red} - 1$
$1.45 < \beta_{red} \leq 2$	0	0	0	0	a_1	0	0	0	0	1	0	0	0	0	0	$a_1 = \beta_{red} - 1$
	0	0	0	0	0	1	0	0	0	0	a_1	0	0	0	0	
$2 < \beta_{red} \leq 2.71$	0	0	0	0	1	0	0	0	0	1	0	0	a_1	0	0	$a_1 = \beta_{red} - 2$
	0	0	0	0	1	0	0	a_1	0	0	1	0	0	0	0	
	0	0	a_1	0	0	1	0	0	0	0	1	0	0	0	0	
$2.71 < \beta_{red} \leq 3$	0	0	0	a_1	0	0	0	1	0	0	0	1	0	0	0	$a_1 = \beta_{red} - 2$
	0	0	0	1	0	0	0	a_1	0	0	0	1	0	0	0	
	0	0	0	1	0	0	0	1	0	0	0	a_1	0	0	0	
$3 < \beta_{red} \leq 3.6$	0	a_1	0	1	0	a_2	0	1	0	a_3	0	1	0	a_4	0	$a_1 + a_2 + a_3 + a_4 = \beta_{red} - 3$

497 C. Solving the Simplified Objective Function

498 In this subsection, the solution for the objective function given
499 in (21) is discussed. The problem is actually minimizing the
500 error propagation at a given intra rate budget. As an example,
501 this problem is solved for $N = 15$ and various values of β_{red} ;
502 the results are tabulated in Table I.

503 As can be seen from this table, when $\beta_{red} \leq 1$, the best frame
504 for intra coding is the middle frame. If there was more intra
505 budget; i.e., $1 < \beta_{red} \leq 1.45$, $\beta^{(4)}$ and $\beta^{(12)}$ begin to grow
506 irrespective of whether the intra rate is allocated to the 4th frame
507 or the 12th frame. However, when intra rate budget exceeds
508 1.45, the optimization function given in (21) recommends other
509 frames for intra coding to be chosen; e.g., frames 5 and 10, where
510 frame 10 is coded wholly as I-frame, and frame 5 has partially
511 intra coded blocks. Equivalently, another package is frames 6 and
512 11, where frame 6 is now selected for I-frame coding. One can
513 see that these two packages produce the same obstacle against
514 the error propagation.

515 For some other regions of β_{red} , the selected frames are given
516 in Table I. One important point is changing the intra coded frame
517 candidates imposed by the objective function of (21). The reason
518 is that, if β_{red} is between two integers K_1 and K_2 ; that is $K_1 <$
519 $\beta_{red} < K_2$, the optimizers may decide to add another frame for
520 intra coding in addition to K_1 frames (e.g., one frame between
521 them), or decide to select K_2 frames for intra coding and reduce
522 the intra rate of one of them to comply with the bound of β_{red} .
523 Clearly, if β_{red} is close to K_1 , the former case happens, and the
524 latter case happens when β_{red} is close enough to K_2 . However,
525 as shown in Fig. 4, $ErrorPro_{min}$ behaves continuously at these
526 border points of β_{red} . In each interval shown by broken lines,
527 the intra coding frame candidates are the same where one or more
528 appropriate frames of these candidates consume the allocated
529 intra coding budget. As already mentioned, the slope of decay
530 in $ErrorPro_{min}$ in each interval is constant. If β_{red} becomes
531 larger than 7, the frames are alternately coded as I-frame; that
532 is the GOP structure is IPIPIP, and now all P-frames have the
533 same priority for intra rate for all β_{red} amounts; therefore; there
534 are no broken lines in Fig. 4 for $\beta_{red} > 7$.

535 This solution proves that to achieve the best error resiliency
536 for intra coding, the best strategy is to concentrate on intra

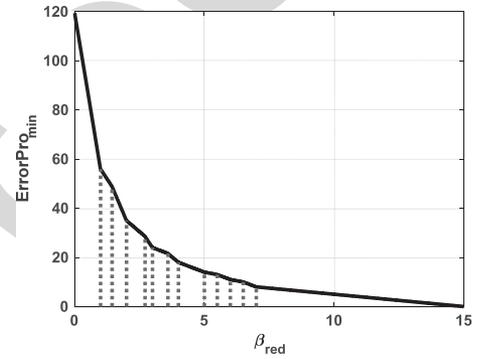


Fig. 4. Behavior of $ErrorPro_{min}$ with β_{red} .

537 coding the blocks in the middle frame of the GoP, such that
538 the entire frame is coded as an I-frame. If the intra rate budget
539 (or accordingly bitrate budget) allows, more frames can still be
540 coded in intra mode. In other words, the output of the objec-
541 tive function is to reduce the intra period; this strategy leads
542 to smaller error propagation and hence higher video quality for
543 lossy channels, compared to the case that intra coded blocks are
544 distributed among the frames.

545 V. THE OPTIMAL VALUE FOR THE INTRA PERIOD

546 As shown in Table I, at a larger β_{red} , the number of I-frames
547 in the GoP can increase. This is in favor of mitigation of error
548 propagation; however, the required bitrate for sending the video
549 is increased since the compression ratio is decreased.

550 Having more I-frames is justified in channels with higher loss
551 rates and vice versa. Therefore, PLR and the coding bitrate affect
552 the best value for β_{red}^* . As shown in Table I, β_{red}^* is directly
553 related to Intra Period (IP); therefore, the problem of finding
554 $\beta_{red-opt}$ is equivalent to finding an optimal value for IP , denoted
555 as IP^* . However, to find IP^* analytically, one must know the
556 rate-distortion behavior of the frames of the GoP under consid-
557 eration; that is, the behavior of future frames must be known
558 *a priori*, which is not possible unless it is estimated based on
559 the frames' history similar to the work presented in [41]. This
560

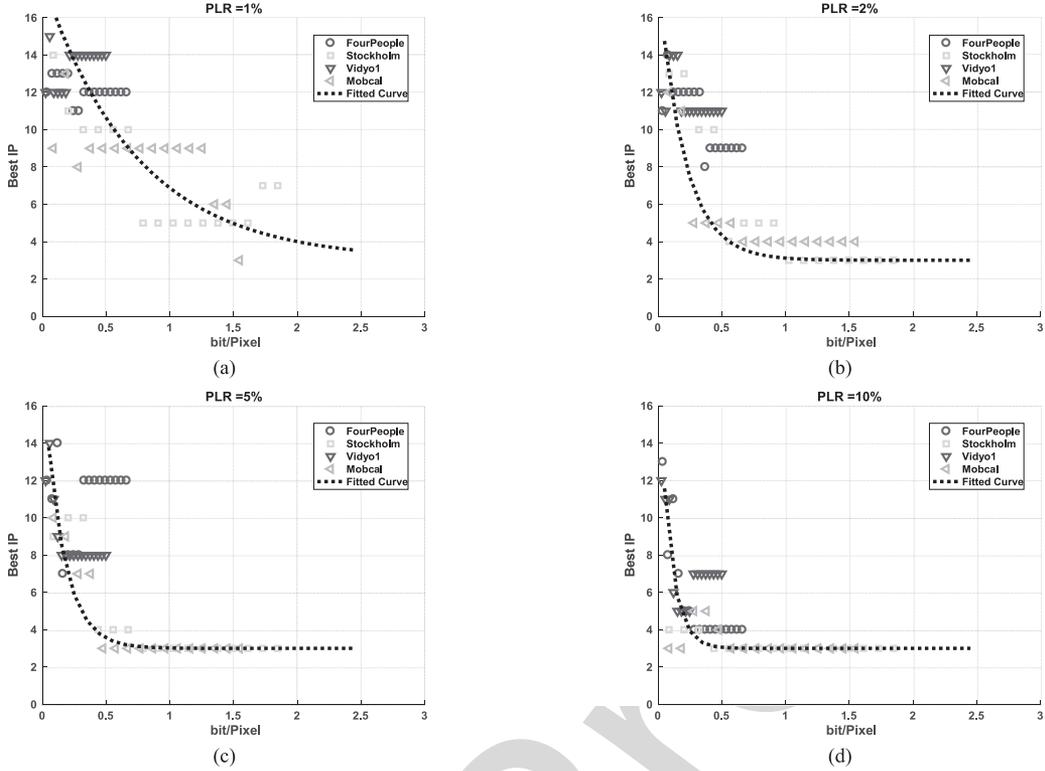


Fig. 5. The best IP versus bit/pixel for various PLRs and test sequences.

560 way, the problem can be solved using classical constraint opti-
 561 mization approaches. However, the complexity of the problem
 562 and non-trivial solutions have encouraged us to use an empirical
 563 approach. Therefore, IP^* has been found through experimental
 564 measurements, as follows.

565 The videos are encoded in Slice Mode, and each slice contains
 566 an integer number of CTUs in raster scan order. Each coded slice
 567 can be as large as 1500 bytes, meeting the Maximum Transmis-
 568 sion Unit (MTU) of the network, and transmitted as a single
 569 packet. The channels experience a burst form of loss generated
 570 by Elliot-Gilbert model [46]. At each PLR , 40 packet loss pat-
 571 terns with an average burst length of three packets are generated
 572 and applied on the bit streams.

573 The video sequences are encoded at various values of IP ;
 574 $IP = M$ means every M th frame of the sequence is coded as
 575 an I-frame. For example, for $IP = 3$, there are two P-frames
 576 after each I-frame, and this pattern is repeated throughout the
 577 sequence. In a GoP of 30 frames, the videos are encoded with
 578 $IP = 1, 2, \dots, 15$ (for GoP of N frames, $IP > \frac{N}{2}$ is not reason-
 579 able). The compressed bit stream is subjected to a specific PLR ,
 580 and the decoded video is loss concealed (as given in IV.A) and
 581 the resulting quality is measured. Video quality is measured in
 582 terms of Video Quality Model (VQM) [47] and its average index
 583 taken over the loss patterns is calculated. VQM is a video quality
 584 assessment method which considers both spatial and temporal
 585 distortions, so it is quite suitable to our case. For each test video
 586 and at the given PLR , the best IP which provides the best quality
 587 (i.e., the lowest VQM index, since higher quality is equivalent
 588 to lower VQM index) at the corresponding bitrate is selected.
 589 Fig. 5 shows the best IP s as a function of bit/pixel for four
 590 sequences.

591 It can be seen that the best IP becomes smaller at higher bi-
 592 tates and higher PLRs. Even though some points are not close to
 593 the others, they can be fitted on decaying exponential functions,
 594 as shown in Fig. 5. The fitted curves can be formulated with the
 595 following equations:

$$IP^* = 3 + 15 \exp\left(-\frac{R}{R_0}\right)$$

$$R_0 = 0.15 + 1.4575 \exp\left(-\frac{PLR}{0.01}\right) \quad (22)$$

596 where R is the bit per pixel. Clearly, IP^* obtained from (22)
 597 must be rounded to the nearest integer number. Even though the
 598 decimal values are also applicable, our empirical approach and
 599 curve fitting is not accurate enough for extracting decimal values
 600 for frames' intra rates.

601 One issue is the fact that coding a frame fully in Intra mode
 602 might cause sudden changes in the bitrate and hence more con-
 603 gestion in the lossy channels. However, for numerous applica-
 604 tions, like video broadcast, streaming, multicasting etc., one
 605 needs to play the video at almost any time during transmission.
 606 This facility can only be provided by Intra coded frames. On the
 607 issue of increased I-frame bitrates, one should note that in these
 608 applications, normally several video flows are multiplexed, such
 609 that higher bitrates of I-frames coincide with lower bitrates of
 610 many P- and B-frames of the other flows and are easily smoothed
 611 out. Despite this, even for a single video flow, some traffic shap-
 612 ing, such as coarser quantization parameter for I-frames can be
 613 applied to reduce the bits; however, this solution may lead to
 614 quality flicker due to lower qualities of the I-frames if the QPs
 615 of I-frame and P-frames are much different. For high motion

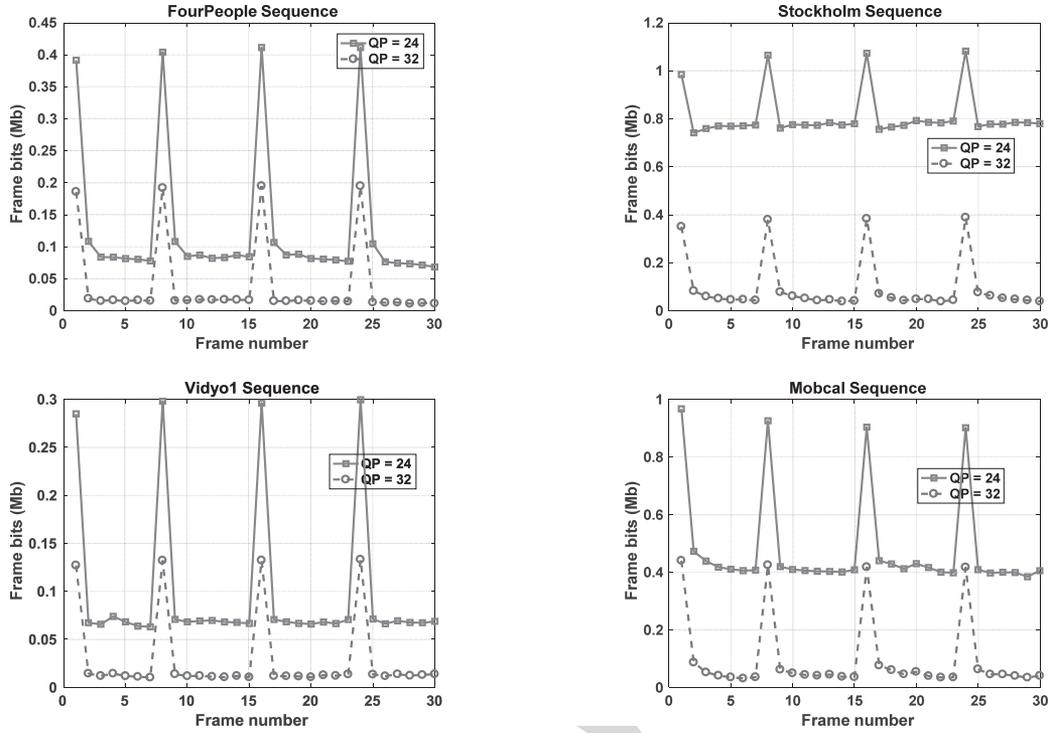


Fig. 6 The sudden changes in the frame bits when a frame is encoded as I-frame. Every 8 frames, one frame is Intra coded entirely.

616 and high texture videos, the difference between I and P frames' 617
 618 bits are not so large and this approach might be sufficient there. 619
 620 If this was not the case, another solution is to have the same 621
 622 QP for I and P frames but use an encoder smoothing buffer to 623
 624 regulate the bitrate (e.g., traffic shaping), of course at the cost of 625
 a few frames delay in video display. How this delay can solve 626
 the problem is explained below. Let us assume that intra period 627
 is M frames. If the frame rate of the video is FPS , the average 628
 bitrate required by the channel is:

$$R = FPS \frac{((M-1)R_P + R_I)}{M} \text{ bits/sec} \quad (23)$$

625 where R_P and R_I are number of bits needed for coding the 626
 627 P-frames and I-frames, respectively. Now if the I-frame has k 628
 times more bits than the P-frames, then:

$$\begin{aligned} R &= \frac{FPS (M-1+k) R_P}{M} \\ &= \frac{FPS (M-1+k) R_I}{kM} \text{ bits/sec} \quad (k > 1) \end{aligned} \quad (24)$$

628 At each $1/FPS$ second, the total sent bits are:

$$\begin{aligned} R &= \left(1 + \frac{k-1}{M}\right) R_P \\ &= \left(\frac{M+k-1}{kM}\right) R_I \text{ bits/sec} \quad (k > 1) \end{aligned} \quad (25)$$

629 Therefore, more than one P-frame or less than one I-frame 630
 631 is transmitted at each $1/FPS$. That is, compared to the case 632
 where all frames have the same number of bits (i.e., $k = 1$), 633
 delivering P-frames is faster and delivering I-frames is slower. 634

635 However, the issue that may arise here is the transmit and 636
 637 receive buffers' overflow and underflow in a live streaming 638
 application. It can be shown that, with display latency as large 639
 as $M(k-1)/(M-1+k)$ frames, there is no overflow or 640
 underflow in the buffers and continuous playing of the video is 641
 preserved (see Appendix B in [32] for the proof). This latency 642
 increases with M ; therefore, a smaller M chosen for higher 643
 PLRs leads to lower latencies. 644

645 The value of k is content dependent; Fig. 6 shows the number 646
 of bites of I and P frames, with $M = 8$ for four sequences and two 647
 QPs. One can see that k is about 1.5 for *Stockholm* at $QP = 24$; 648
 that is, k is small and the delay is not significant. For example, for 649
 PLRs of 5%, if M is around of 4 as shown in Fig. 5, this gives a 650
 latency of about 0.5 frames. However, the ratio k becomes larger 651
 at $QP = 32$. And also, M is typically larger for lower bitrates; i.e., 652
 for $QP = 32$. Therefore, the incurred delay is more challenging 653
 here; for example, for *FourPeople* at $QP = 32$, k is about 10 as 654
 shown in Fig. 6, which is relatively very high. Now for $M = 15$ 655
 (as inferred from Fig. 5), the delay becomes about 5.5 frames. 656
 For FPS of 60, it leads to a delay less than 100 ms which is 657
 acceptable for many applications. For smaller delays, we can 658
 combine the above two approaches; that is, applying coarser 659
 quantizer and forcing a delay. The coarser quantizer to I-frames 660
 leads to a smaller k which in turn leads to a smaller delay. 661

VI. PERFORMANCE COMPARISON

657 The analysis explained in the previous sections shows that 658
 using I-frames instead of applying IRR is more efficient as 659
 an error resiliency tool and gives higher quality in dealing 660
 with transmission of encoded videos over lossy channels. The 661

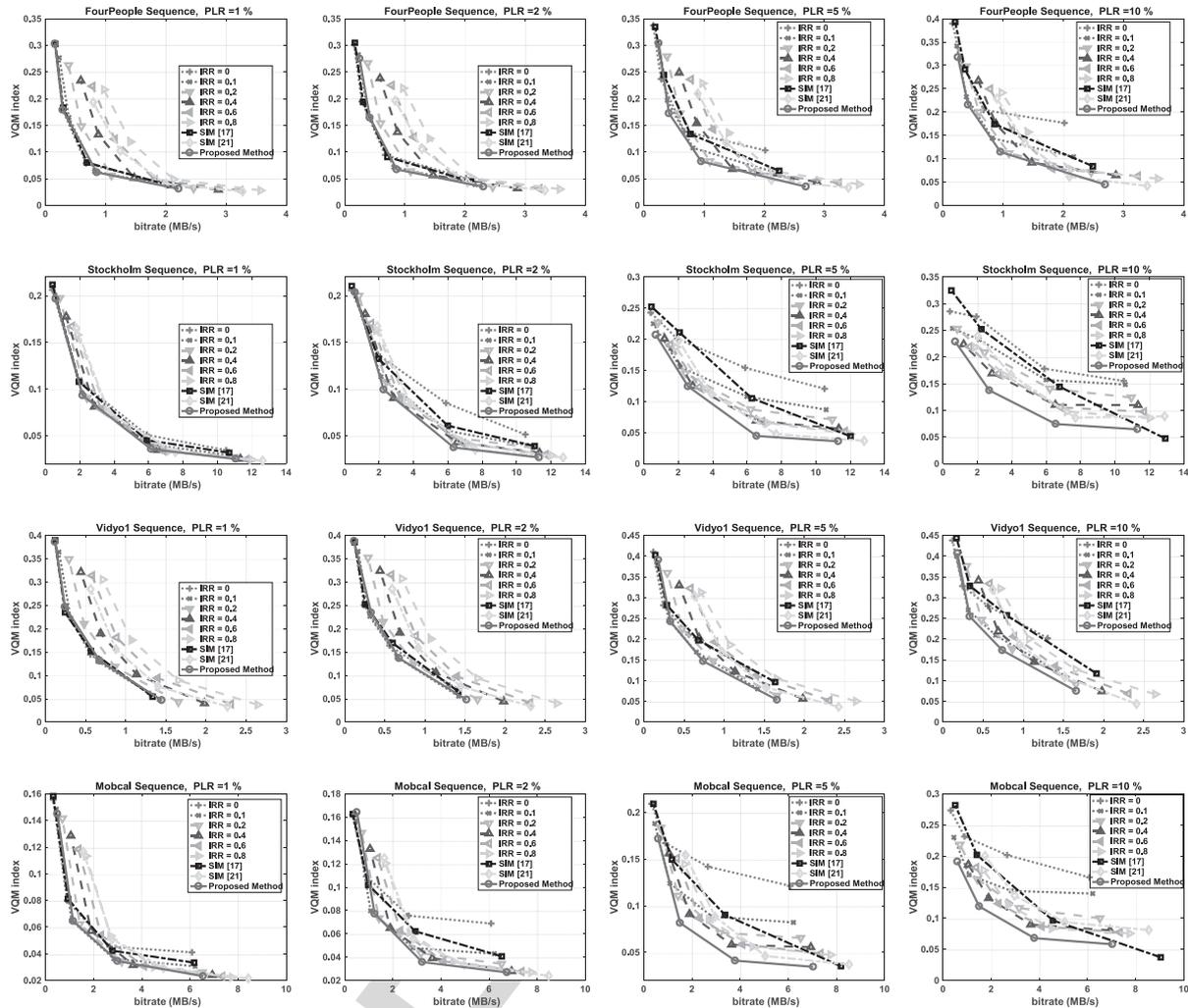


Fig. 7. Performance comparison of the proposed method for various PLRs and *FourPeople*, *Stockholm*, *Vidyo1* and *Mobcal* sequences for burst length of three packets.

662 suitable I-frame period is given by (22). As already mentioned
 663 in Section II, there are two other options for intra coding,
 664 SIM and Intra Refresh. For performance comparison, our
 665 proposed method is compared against two SIM methods, [17]
 666 and [21], where the PUs are selected based on an objective
 667 function for intra or inter coding. Note that as explained in
 668 Section II, there are also two options for selecting the
 669 blocks to be forced for intra coding in the Intra Re-
 670 fresh scheme. They can be selected randomly or in a
 671 regular manner, such as a column of intra blocks moving
 672 by frame from left to right. Our experiments showed that the
 673 latter option, called Periodic Intra Refresh (PIR) or cyclic
 674 intra-refresh generally gives superior performance in terms of
 675 rate-distortion. Therefore, we have included the results of PIR
 676 in Figs 7–9. Since there are no appropriate recent related works
 677 on the best value of IRR, we examine PIR with several possible
 678 values of IRR for all examined PLRs; these are {0, 0.1, 0.2,
 679 0.4, 0.6, 0.8}. Note that $IRR = 0$ is equivalent to not paying
 680 any attention to channel loss at the encoder. With the experimental
 681 settings given in Section V, these results are shown in Figs 7–9,
 682 Fig. 9 is for the average burst length of six packets.

683 Despite of the simplifications and approximations made in our
 684 method through analysis and curve fitting, it can be seen from
 685 Figs 7–8 that our proposed method outperforms the others in
 686 many cases. For lower PLRs and smaller bitrates, the proposed
 687 method provides actually no gain. In these regions, since the
 688 video is less sensitive to packet loss, the curves are actually
 689 close to each other. The algorithm of [21] picks many PUs for
 690 intra coding; therefore, it applies intra rate much more than
 691 required but with a slight gain in quality in lower PLRs. For
 692 this reason, this algorithm does not work well for low PLRs.
 693 In the cases of higher PLRs and higher bitrates, one can see
 694 the VQM quality index of our proposed method is better than
 695 the others which is sometimes significant. A reminder that the
 696 smaller VQM index means higher quality. Light content video
 697 sequences, such as *FourPeople* and *KrisenAndSara*, as already
 698 mentioned are less sensitive to data loss; hence the VQM
 699 curves are again similar while ours are still marginally better.

700 For the PLRs of 5% and 10%, the results of applying average
 701 burst length of six packets are shown in Fig. 9. It can be seen
 702 that the performance of our proposed method is still better than
 703 the others. Actually, the loss pattern does not significantly affect our

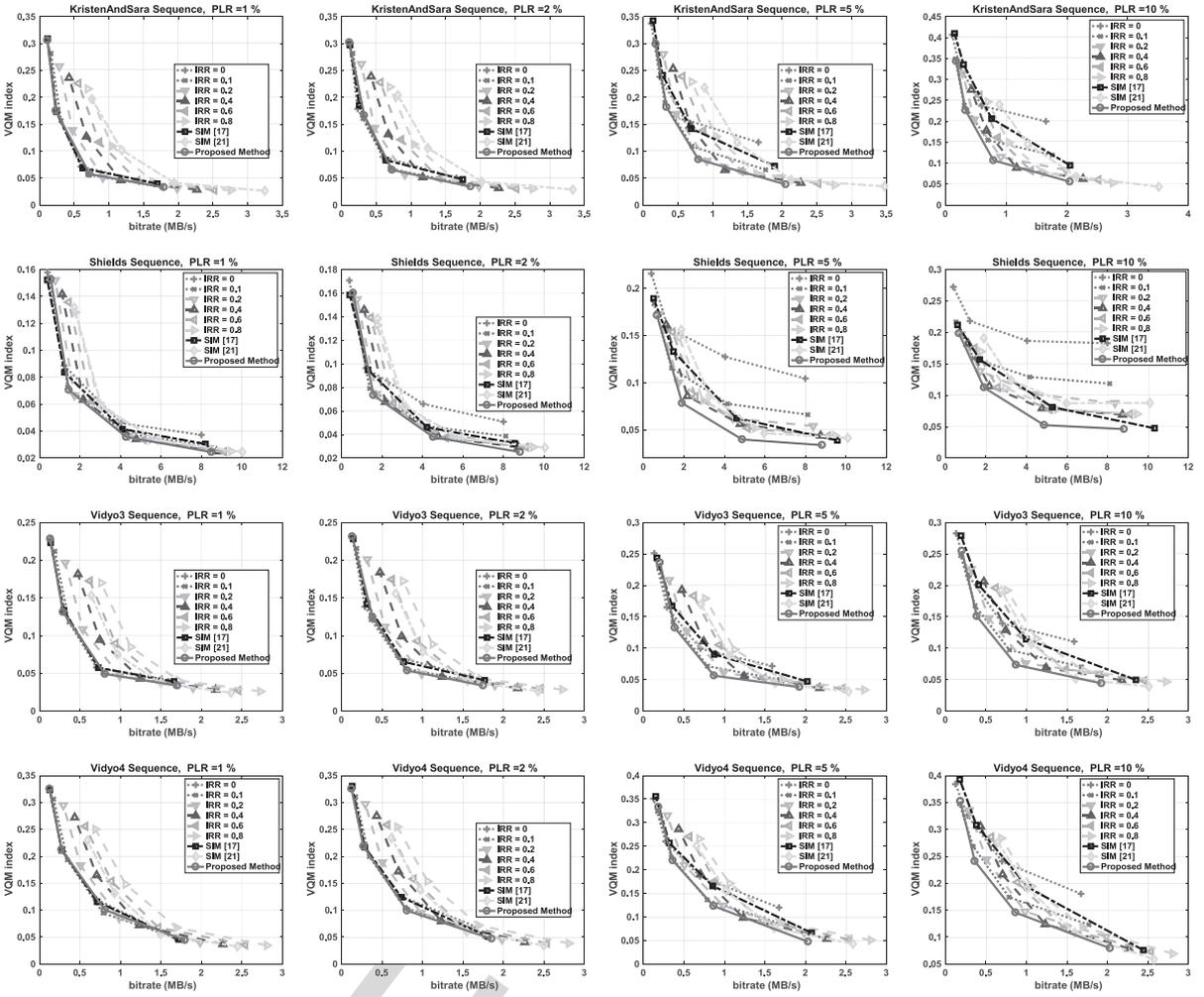


Fig. 8 Performance comparison of the proposed method for various PLRs and *Kristen and Sara*, *Shields*, *Vidyo3* and *Vidyo4* sequences for burst length of three packets.

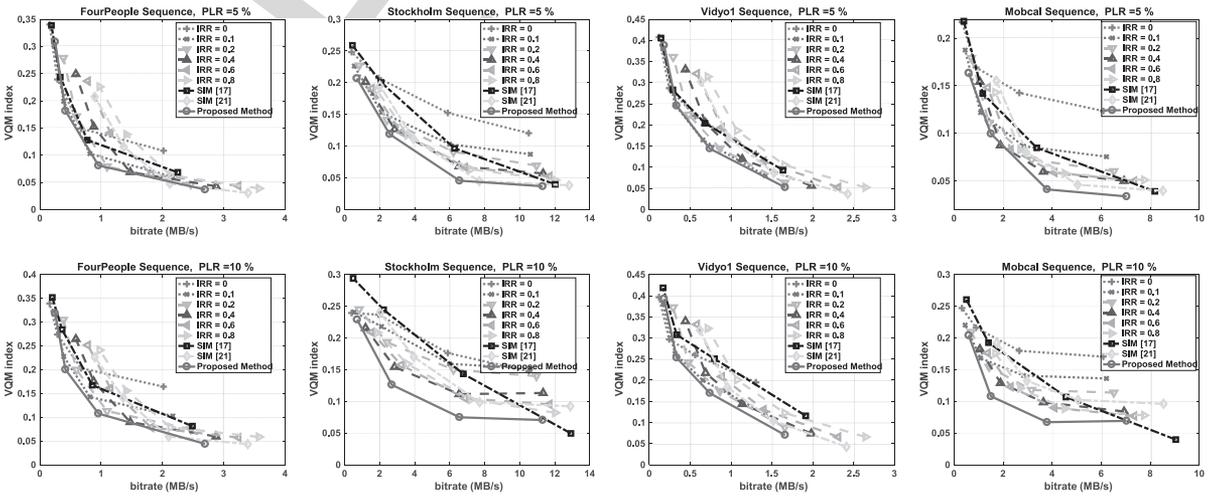


Fig. 9 Performance comparison of the proposed method for various PLRs and *FourPeople*, *Stockholm*, *Vidyo1* and *Mobcal* sequences for burst length of six packets.

704 results due to our loss concealment procedure applied to lossy
705 bitstreams generated by any of competing methods.

706 The burst loss leads to larger lossy areas in the pictures,
707 which is usually handled by the Motion Copy algorithm. Note
708 that burst loss will lead to the loss of consecutive frames in low
709 bitrate and low resolution videos, while it is not so destructive
710 for HD and beyond.

711 VII. CONCLUSION

712 In this paper, the best strategy for intra coding as an error
713 resiliency tool is presented. It was proposed to encode some
714 frames entirely in intra mode, rather than the conventional ap-
715 proach where some blocks or PUs are selected in PIR manner
716 (with a specific intra rate) or by a cost function to be coded in
717 intra mode. Considering the error propagation, the receiver side
718 distortion is formulated and it is simplified with some obser-
719 vations. The simplified objective function has a straightforward
720 solution: $\beta^{(i^*)} = 1$, where i^* is the index of the frames sym-
721 metrically positioned in the GoP, and the number of I-frames
722 depends on β_{red} or equivalently the available bitrate budget for
723 intra coding. The output of the objective function is to reduce
724 the *IP* as much as possible and as long as the bitrate overhead
725 of intra coding is justified at the given channel loss rate.

726 The optimal *IP* varies with the coding bitrate as well as the
727 PLR as shown in Fig. 5. We have fitted a curve to the experi-
728 mental points obtained from examining various test sequences,
729 as given in (22). With the IP^* selected by (22), experimental re-
730 sults show that the proposed method achieves lower VQM index
731 compared to the conventional SIM and PIR methods.

732 APPENDIX

733 Assume that frame 1 is transmitted through n packets. If m
734 packets are lost, the average distortion after error concealment
735 is:

$$D_m^{(1)} = \frac{(n-m)}{n} D_q^{(1)} + \frac{m}{n} D_{conceal}^{(1)} \quad (26)$$

736 If each packet is lost with a probability of *PLR*, the proba-
737 bility of losing m packets is

$$\begin{aligned} PLR_m &= C(n, m) PLR^m (1 - PLR)^{n-m} \\ &= \binom{n}{m} PLR^m (1 - PLR)^{n-m} \end{aligned} \quad (27)$$

738 where $C(n, m)$ is the number of m -combinations from n packets.
739 Therefore, the expected distortion of frame 1 is as given by (28):

$$\begin{aligned} D^{(1)} &= \sum_{m=0}^n \left(PLR_m D_m^{(1)} \right) \\ &= \frac{D_q^{(1)}}{n} \sum_{m=0}^n \left[(n-m) \binom{n}{m} PLR^m (1 - PLR)^{n-m} \right] \\ &\quad + \frac{D_{conceal}^{(1)}}{n} \sum_{m=0}^n \left[m \binom{n}{m} PLR^m (1 - PLR)^{n-m} \right] \end{aligned} \quad (28)$$

740 Both summations in (28) are the expected values of a *Bino-*
741 *mial* distribution with probabilities of $(1 - PLR)$ and *PLR*,
742 respectively. That is $D^{(1)}$ becomes

$$\begin{aligned} D^{(1)} &= \frac{D_q^{(1)}}{n} [n(1 - PLR)] + \frac{D_{conceal}^{(1)}}{n} [n PLR] \\ &= (1 - PLR) D_q^{(1)} + PLR D_{conceal}^{(1)} \end{aligned} \quad (29)$$

743 which is the same as equation (2).

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