

1 How to build a fast and accurate 2 Code-Modulated Brain-Computer 3 Interface

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13 Abstract

14 *Objective.* In the last decade, the advent of code-modulated brain-computer interfaces (BCIs) has allowed the implementation
15 of systems with high information transfer rates (ITRs) and increased the possible practicality of such interfaces. In this paper,
16 we evaluate the effect of different numbers of targets in the stimulus display, modulation sequences generators, and signal
17 processing algorithms on the accuracy and ITR of code-modulated BCIs. *Approach.* We use both real and simulated EEG
18 data, to evaluate these parameters and methods. Then, we compared numerous different setups to assess their performance
19 and identify the best configurations. We also evaluated the dependability of our simulated evaluation approach. *Main results.*
20 Our results show that Golay, Almost Perfect, and deBruijn sequence-based visual stimulus modulations provide the best
21 results, significantly outperforming the commonly used m-Sequences in all cases. We conclude that artificial neural network
22 processing algorithms offer the best processing pipeline for this type of BCI, achieving a maximum classification accuracy of
23 94.7% on real EEG data while obtaining a maximum ITR of 127.2 bits/min in a simulated 64-target system. *Significance.* We
24 used a simulated framework that demonstrated previously unattainable flexibility and convenience while staying reasonably
25 realistic. Furthermore, our findings suggest several new considerations which can be used to guide further code-based BCI
26 development.

27 **Keywords:** Brain-Computer Interface, Code Modulated Visual-Evoked Potentials, Canonical Correlation, Artificial Neural
28 Networks, m-Sequence, Almost Perfect Autocorrelation, DeBruijn, Golay Sequence.

29

30 1. Introduction

31 Electroencephalographic (EEG) data is acquired by
32 measuring the net synaptic excitations from the surface of the
33 scalp [1]. Components of the EEG elicited by exogenous
34 stimuli, known as event-related potentials (ERPs), are
35 commonly used in brain-computer interfaces (BCI) to identify
36 control commands, allowing BCI users to communicate
37 without motor or peripheral interaction [2]. These benefits
38 have led to the accelerated pursuit of high-performance BCI
39 systems in the last two decades [3][4][5][6].

40 Modern BCIs are frequently based on the neural potentials
41 evoked by out-of-sequence or unexpected time-dependent
42 external events, such as P300 event-related potential-based

43 systems, or by the response to frequency-dependent visual or
44 auditory stimuli, like steady-state visual-evoked potentials
45 (SSVEPs) [7]. Both types of BCI operate by presenting stimuli
46 to the user which alternates in appearance at regular intervals.
47 ERP-based BCIs are more comfortable to use, while SSVEP
48 BCIs offer better performance in terms of accuracy and speed
49 of the BCI [8][9].

50 In addition to the ERP and SSVEP types of BCI, systems
51 based on code-modulated visual evoked potentials (c-VEPs)
52 have gained relevance more recently as a proposed solution to
53 the issues of visual fatigue and sub-optimal information
54 transfer rates in users of several ERP and SSVEP-based BCIs
55 [3][8][10][11].

56 By modulating the display of an array of visual stimuli with
 57 a predetermined pseudorandom binary sequence (PRBS) at
 58 relatively high and uniform frequencies such as 60 and 120 Hz
 59 [3][12], BCIs based on c-VEP offer the potential for much
 60 more pleasant operation [10]. Although there are several
 61 methods for generating a PRBS, there is no definite optimal
 62 choice for BCI applications. Numerous types of PRBS have
 63 been implemented in this context, for example, m-Sequences
 64 [3] [8] [12] [13], Almost Perfect Autocorrelation [14]
 65 sequences, and Gold sequences have all been attempted [15].

66 The structure of the interface display used with c-VEP BCIs
 67 is similar to the interface typically used with other VEP-based
 68 BCIs and commonly consists of a rectangular arrangement of
 69 multiple square target cells surrounded by complementary
 70 non-target cells. By adopting the principle of equivalent
 71 neighbors [16] and the comments by Bin *et al.* [17] regarding
 72 the VEP field of view, it is reasonable to display all these
 73 stimulus sources in a compactly arranged grid on a display
 74 screen.

75 Besides reducing visual fatigue, several different c-VEP
 76 BCIs have been proposed which typically outperform the
 77 information transfer rates (ITRs) obtained with SSVEP-based
 78 systems. For example, in 2009 Bin *et al.* [17] obtained an
 79 information transfer rate of 58 ± 9.6 bit/min with an SSVEP-
 80 based BCI, but later in 2010 proposed a c-VEP system that
 81 achieved a much higher average ITR of 108 ± 12 bits/min [3].
 82 Two years later, this high ITR score was further improved by
 83 Spüler *et al.* [7], reaching 144 bit/min with a BCI that also
 84 incorporated error-related potentials, allowing online
 85 adaptation. In 2018, Wei *et al.* [14] proposed a novel c-VEP
 86 BCI structure based on grouped stimulus targets, yielding an
 87 even higher ITR of 181.05 bits/min.

88 Several parameters influence the efficacy of a c-VEP BCI.
 89 They include but are not limited to, the type of PRBS used to
 90 present the stimuli, the feature extraction process used within
 91 the signal processing pipeline, and the number of targets
 92 presented to the user. Many different variants of these
 93 parameters have been investigated by c-VEP BCI researchers.
 94 However, to date, there is no clear consensus on which
 95 parameters are most effective in allowing the construction of
 96 a fast and accurate c-VEP BCI.

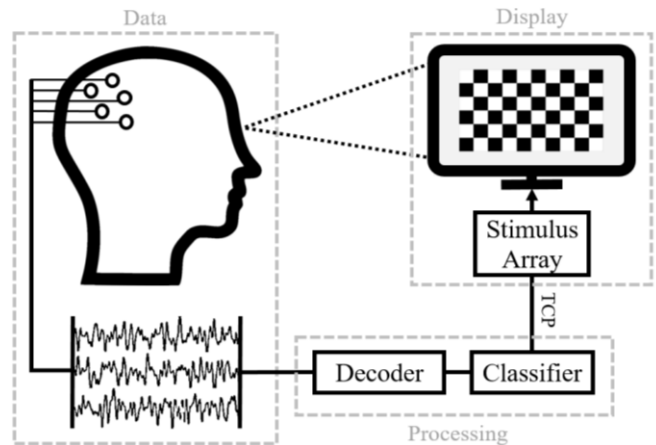


Figure 1. The workflow overview diagram of the c-VEP BCI system, composed of three stages executed cyclically: data acquisition, signal processing, and visual stimulation.

97 In this paper, we work with a high-speed c-VEP BCI
 98 framework using both a real EEG dataset and a simulated EEG
 99 dataset. We evaluate the effect of multiple PRBS types, signal
 100 processing algorithms, and numbers of stimuli in the
 101 presentation setup on the overall performance of the c-VEP
 102 BCI system, measured through accuracy and ITR. We also
 103 compare various attributes between the experimental and the
 104 simulated EEG datasets to assess the dependability of the
 105 simulation approach.

106 2. Methods

107 2.1 Theory of Operation

108 Figure 1 shows the workflow overview diagram of a typical
 109 c-VEP BCI system. It is composed of three stages executed
 110 cyclically: data acquisition, signal processing, and visual
 111 stimulation. The interface first presents multiple command
 112 options to the user. Each of these commands displayed is
 113 modulated, over time, by the PRBS. For example, commands
 114 may be toggled between two different states (e.g. visible vs.
 115 hidden, or greyed out vs. highlighted) according to the digit of
 116 each bit in the PRBS. For the signal processing stage, as is
 117 generally the case [5], the system acquires the c-VEP data

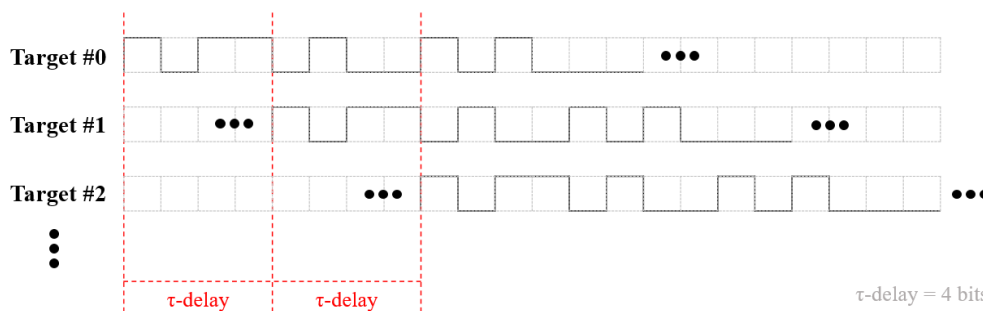


Figure 2. Visualization of an example of the modulation behavior of the first three stimulus targets, showing a consecutive circular shift of 4 bits of the same pseudorandom binary sequence

118 from the user, processes the
 119 multi-channel signals in the
 120 time and spatial domains,
 121 extracting the relevant
 122 features, to finally perform the
 123 identification as to which
 124 stimulus source the user is
 125 fixating on, and ultimately
 126 execute the command of the
 127 user's interest without

128 physical interaction with the
 129 machine.

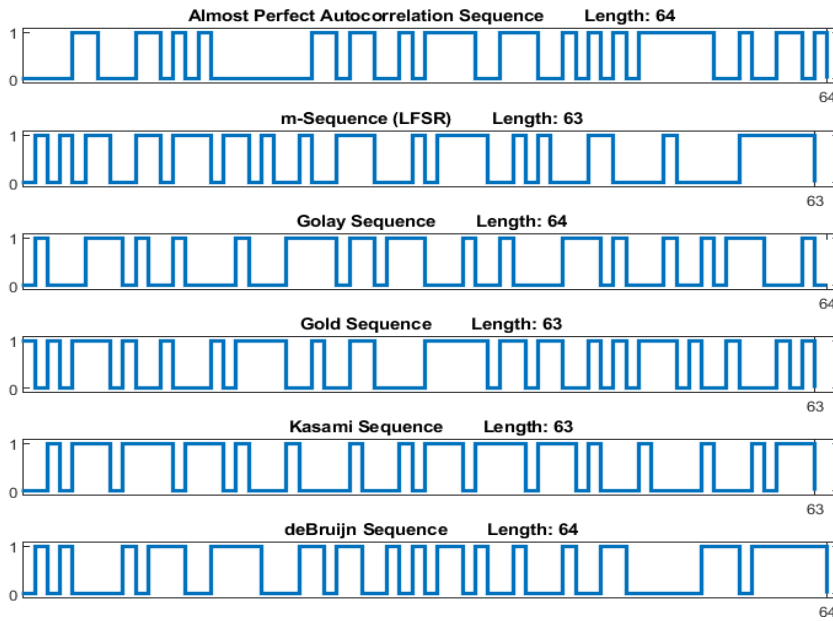


Figure 3. Instances of modulation sequences visualized. Examples of the six distinct PRBS evaluated in a 64-bit setup, from top to bottom: APA, m-Sequence, Golay, Gold, Kasami, and DeBruijn sequences.

In this study we supersede the data acquisition and display stages by employing an offline BCI, that is, by using recorded real and pre-generated synthetic EEG, allowing us to focus on the processing pipeline. Specifically, we utilized a signal simulation program (developed in MATLAB R2019b) for EEG signal simulation, inspired by the open-source framework developed by Lindgren *et al.* in 2018 [18]. While for the real EEG, we used a dataset provided by Wei *et al.* [14].

As shown in Figure 2, the behavior of each target stimulus presented to the user is modulated frame by frame with a consecutively shifted PRBS, in which the 0/1 value of the momentary bit toggles a particular stimulus on and off, as suggested by Wei *et al.* [19]:

$$M(t)_{Tar_i} = PRBS\left(t + (i * \tau_{delay})\right) \quad (eq. 1)$$

where M is the binary value of target i (Tar_i) at time t , considering a τ lag of 4 bits between consecutive targets, and $PRBS(x)$ defines digit x of the stimuli modulation sequence in the BCI setup.

To evaluate the effect of different configurations on the system performance we explored multiple options for three key parameters from the typical c-VEP BCI setup and processing pipeline. First, we used three distinct numbers of targets (16, 32, and 64 targets). This choice of numbers of available targets was based on the comments made by Baseler *et al.* [20] describing the negative impact on performance from an increase of targets presented to users in a BCI. Second, we evaluated 6 of the most widely used types of PRBS for modulation of the stimuli (detailed in section 2.3). Finally, we implemented 6 decoding algorithms that are commonly used in the context of BCI feature extraction (section 2.4).

61 2.2 Data Acquisition

62 2.2.1 Experimental Approach

The experimental dataset, provided by Wei *et al.* [14], consisted of two independent c-VEP data subsets recorded from 12 different c-VEP BCI users (8 females) with normal or corrected to normal vision, between the ages of 21 and 26 years old. In the training subset, users fixated on one particular target from the array, defined as the reference target, for 20 trials, effectively providing 240 training trials in total. In the testing subset, each of the 12 participants fixated on each target from an array of 16 square targets, for 5 useful cycles of the stimuli modulation sequence each, totaling 960 distinct trials.

The setup for the acquisition of the real experimental EEG data utilized an almost perfect autocorrelation (APA) sequence of length 64 bits with frequency modulation of

60Hz and a sampling rate of 1000Hz. The electrode impedances were $<10k\Omega$ and EEG electrodes were placed at positions P3, Pz, P4, PO7, POz, PO8, O1, Oz, and O2 in the international 10/20 system for EEG electrode placement.

63 2.2.2 Simulated Approach

Using the EEG simulator program, we generated an extensive synthetic EEG dataset for use in our analysis, consisting of two independent subsets for training and testing data, with a total of 240 and 1920 trials respectively, mirroring the structure from the experimental EEG dataset, while doubling the extent of the testing data.

The generation of the artificial EEG signals consisted of a composite of three elements: the purely code-modulated responses to the PRBS stimulation, white and pink noise originating uniformly from the scalp surface and the head volume, respectively, with internal signal-to-noise-ratios of 1 and 0.8, as suggested in [18]. We also added heuristically-sourced eye movement and eye blink noise artifacts, which in the simulation were set to occur at random times within the trial with probabilities of 30% and 10% respectively, and have random lengths of between 0 (i.e. non-existent) and 2 seconds, as proposed by Tangermann *et al.* [21]. This signal was passed through a 2-45Hz bandpass filter to limit the data to the frequency bands of interest, resulting in the final simulated EEG.

To calibrate the proportions between the noise components and the purely evoked responses, we incorporated a global signal-to-noise ratio (SNR) coefficient into the simulator. We tuned the SNR to maximize the resemblance of the performance results between both approaches and those

212 obtained by Wei *et al* [14] using an identical
 213 setup in simulation. Once tuned, the global
 214 SNR coefficient was set to a unitary value
 215 to later analyze the performance of our BCI
 216 with a range of SNR values (from 0.2 to 2
 217 dB) and observe how influential this
 218 simulation parameter is. These results are
 219 shown in *Figure 9* and detailed in *section 3*.
 220 Finally, the modulation frequency and
 221 the sampling rate were set to 60Hz and
 222 1000Hz, respectively, and the simulated
 223 EEG electrodes were placed in the same
 224 positions as those from the experiments,
 225 following the international 10/20 system for
 226 EEG electrode placement: P3, Pz, P4, PO7,
 227 POz, PO8, O1, Oz, and O2. To achieve this
 228 in simulation, the signal generation is based
 229 on a linear superposition model that uses a
 230 leadfield matrix encoding the electrical
 231 propagation of the head model [18]. We
 232 work with a physiologically realistic non-
 233 specific brain model, which projects
 234 uniform brain volume data to the surface
 235 electrodes, constrained by the cortical
 236 surface normal. The conductivity
 237 parameters of the model consist of scalp,
 238 skull, and brain mesh layers, with
 239 normalized conductivities of 1, 1/15, and 1,
 240 respectively, per Oostendorp *et al.* [22].
 241 Finally, this head model also contains the
 242 dipole sources located at the front of the head representing the
 243 users' eyes, from which the previously mentioned eye noise
 244 artifacts are set to originate.

245 2.3 Modulation Sequences

246 Six different PRBS were selected. These modulation
 247 sequences (MS) were chosen because they all are
 248 deterministically generated and have desirable statistical
 249 properties, such as low autocorrelation, despite the non-linear
 250 influence that these characteristics have on VEPs [3]. The
 251 sequences used in this study were: Linear-feedback shift
 252 register (LFSR, also known as m-Sequences), deBruijn,
 253 Almost Perfect Autocorrelation, Golay, Gold, and Kasami
 254 sequences. Examples of each of these MS are shown in *Figure*
 255 3. The sequences are generated through brute computational
 256 methods and/or distinct recursive algorithms. This is the case
 257 for LFSR and DeBruijn sequences where, for instance, the
 258 following primitive polynomials (mod 2 and 3 respectively)
 259 can be used recursively to generate both of these PRBS:

$$260 \quad f(x)_{LFSR} = x^4 + x^3 + x^2 + 1 \quad (eq. 2)$$

$$261 \quad f(x)_{deBruijn} = x^4 + 2x + 2 \quad (eq. 3)$$

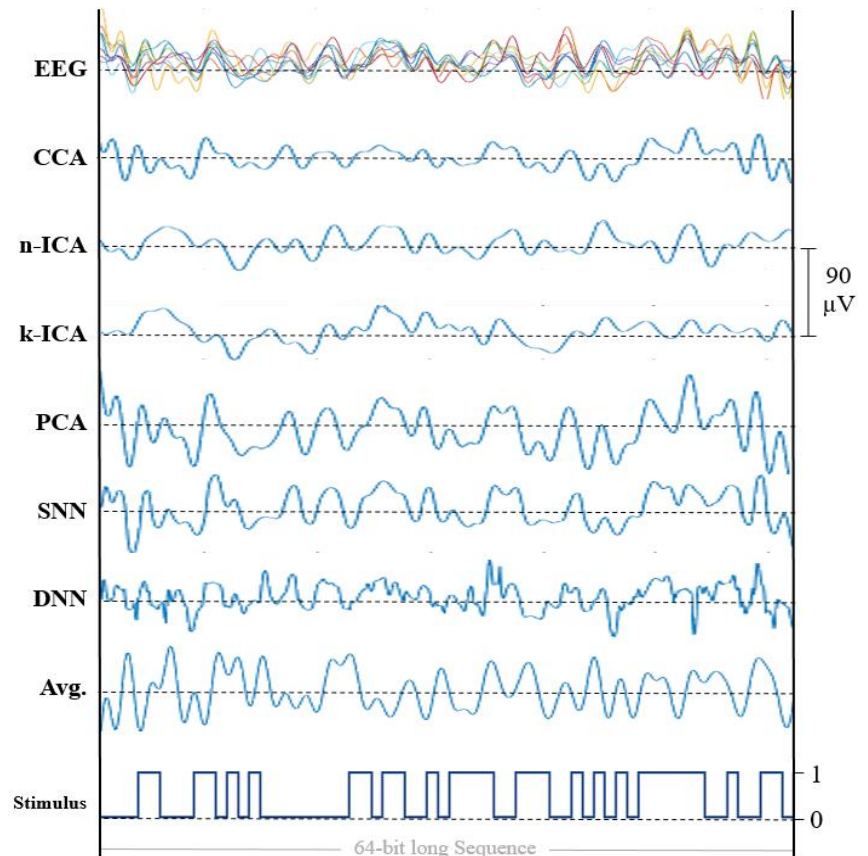


Figure 4. Comparison of single-cycle signals. From top to bottom: Raw EEG signal, pre-processed signal outputs of the six decoding algorithms, the signal average from 20 cycles, and an APA modulation sequence with a length of 64 bits.

262 where the exponents of each x term (also referred to as *taps*),
 263 represent the non-zero bit positions influencing the feedback
 264 for the next state in the recursive arrangement. In this case, the
 265 polynomial degree of $n=4$ results in a PRBS of 15 (2^n-1) and
 266 16 (2^n) bits in length, respectively.

267 Each of these MS is commonly used in cryptography and
 268 spectrometry [23], neurological research [8] [24], and
 269 communication systems [25] due to their semi-random
 270 statistical properties [26] [27]. Furthermore, DeBruijn
 271 sequences have been beneficial for neural decoding processes
 272 in the wider neuroscientific context ([4]). While m-Sequences
 273 are perhaps the most frequently implemented type of MS in
 274 the context of c-VEP BCI research ([3] [8] [12] [13]), Golay
 275 and APA sequences have also been successfully implemented
 276 in novel c-VEP paradigms ([14]). Although to a lesser extent,
 277 Gold sequences have also previously been explored by
 278 Thielen *et al.* [15] in another VEP-based paradigm consisting
 279 of asynchronously evoked Broad-band VEPs, due to the
 280 optimal cross-correlation properties of such sequences.
 281 Similarly, while Kasami sequences have had a highly limited
 282 presence in BCI research, these demonstrated inconclusive
 283 results in the context of c-VEP modulation when studied in
 284 2017 by Isaksen *et al.* [28].

285

286 **2.4 Decoding Algorithms**

287 Multiple decoding algorithms were implemented to assess
288 their effectiveness at decluttering an EEG signal through
289 feature extraction.

290 In our evaluation of the c-VEP processing pipeline, we use
291 six of the most commonly used decoders for EEG feature
292 extraction [8] [13] [29] [30]. The feature algorithms
293 implemented are Canonical correlation analysis (CCA),
294 principal component analysis (PCA), independent component
295 analysis with maximum kurtosis (k-ICA) and maximum
296 negative entropy criterion (n-ICA), shallow (SNN), and deep
297 neural networks (DNN).

298 We used these algorithms to perform a translation from the
299 multidimensional raw EEG signal to a one-dimensional
300 processed feature signal. Each of the algorithms is described
301 in the following sections. The resulting processed one-
302 dimensional feature set was then passed to the classification
303 phase, thus identifying which c-VEP target stimuli the user
304 was attending to in a given trial (described in *section 2.5*).

305 **2.4.1 Canonical Correlation Analysis**

306 The CCA algorithm was utilized to create the spatial filter:

$$307 \quad y[n] = \sum_{i=1}^c x_i[n] w_{xi} \quad (eq. 4)$$

308 where $x_i[n]$ represents the n -th element of the i -th channel ($i=$
309 1, 2, ..., C) from the multichannel input signal, which, once
310 multiplied by the i -th weight from the set of weights W_x ,
311 results in the one-dimensional spatially-filtered signal y . And
312 the set of weights W_x is calculated from the CCA:

$$313 \quad \max_{W_x, W_y} \frac{W_x^T X \hat{X}^T W_y}{\sqrt{W_x^T X X^T W_x \cdot W_y^T \hat{X} \hat{X}^T W_y}} \quad (eq. 5)$$

314 where the terms W_x and W_y denote the linear canonical
315 coefficients that maximize the correlation between the
316 unprocessed EEG input X and an averaged multichannel signal
317 replicated for congruency, denoted here as \hat{X} , and computed
318 as follows:

$$319 \quad X = [X_1 \ X_2 \ X_3 \ \dots \ X_N] \quad (eq. 6)$$

$$320 \quad \bar{X} = \frac{1}{N} \sum_{i=1}^N X_i \quad (eq. 7)$$

$$321 \quad \hat{X} = [\bar{X} \ \bar{X} \ \bar{X} \ \dots \ \bar{X}] \quad (eq. 8)$$

322 where the X input signal is collected from N stimulus cycles
323 and \bar{X} represents the averaged signal before being replicated
324 lengthwise N number of times.

325 **2.4.2 Principal component analysis**

Principal component analysis increases the interpretability
of the signal X , by identifying a projection of the data such that
the new dimensions of the data projected are organized by
decreasing variance. The dimensionality of the signal can then
be reduced by sub-selecting components from the new
projected dimensions [31]. We select and further process only
the one principal component with the largest corresponding
Eigenvalue, here denoted as W_1 :

$$\max_{W_1} \frac{W_1^T X^T X W_1}{W_1^T W_1} \quad (eq. 9)$$

which in our testing corresponds to the single projected
component of the data that represented 75-90% of the total
variance in the case of simulation, and 35-50% for
experimental data, indistinguishable of the particular stimulus
source or modulation sequence.

340 **2.4.3 Independent component analysis**

341 By assuming that the input X is an initial linear combination
342 of real independent sources, denoted as S , we can use
343 Independent Component Analysis (ICA) to extract a single
344 feature set. These algorithms seek the linear transformation
345 matrix A that transforms the EEG signals X into a new
346 component space Y that approximates S . This is achieved by
347 maximizing the statistical independence between each of the
348 output components. Specifically, each recorded signal trial X
349 is assumed to be a linear mixture of sources:

$$350 \quad X = A \times S \quad (eq. 10)$$

351 Where S denotes the original sources and A denotes the
352 linear mixing matrix. An estimate of the sources Y can then be
353 found by inverting the mixing matrix:

$$354 \quad Y = A^{-1} \times X \quad (eq. 11)$$

355 ICA has been demonstrated to produce a useful
356 decomposition of EEG signals in numerous BCI applications
357 [29] [32].

358 However, when using an ICA method the dimensionality of
359 the EEG signal set is not reduced, but maintained. Therefore,
360 it is necessary to define some method to select one of the C
361 independent components of a test trial available for eventual
362 use in classifying the c-VEPs. To accomplish this, we measure
363 the Pearson correlation coefficient between all independent
364 components and all T reference templates produced for the
365 current BCI setup, hence performing $T \times C$ computations.
366 Whichever component maximizes the Pearson correlation
367 coefficient with any of the reference templates is selected as
368 the feature of interest for the subsequent classification stage.
369 The generation of said templates is elaborated upon in *section*
370 *2.5*, while a discussion on the benefits and caveats of this
371 procedure is included in *section 4.2*.

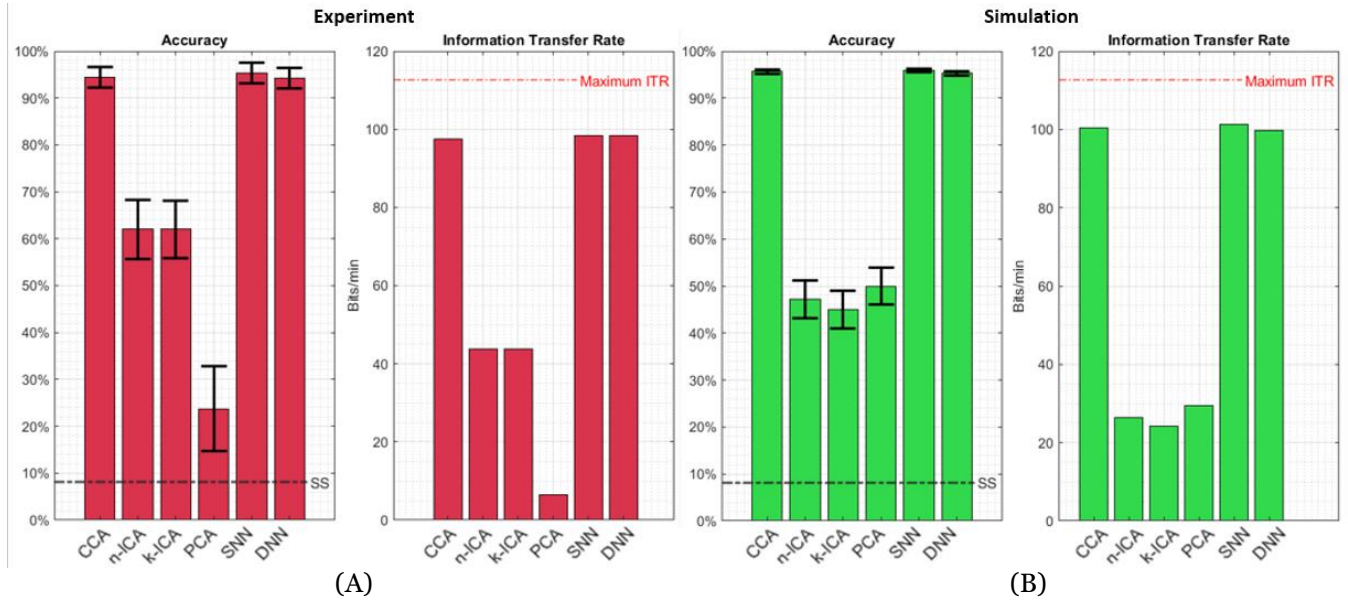


Figure 5. Comparison of experimental and simulated analysis. Results obtained from both experimental (A) and simulated (B) approaches with the same configuration: APA sequence modulation with a 16-target BCI. The left plots of (A) and (B) show the accuracies [%] with error bars and statistical significance line with a p-value < 0.01 of a random 16-target classifier. The right plots of (A) and (B) show the ITR for each decoder [bits/min]. The maximum ITR (red horizontal line) is achieved when the accuracy reaches 100%, resulting in an ITR of 112.5 bits/min.

2.4.4 Artificial neural networks

Although the incorporation of artificial neural networks (ANNs) into c-VEP BCIs is not the most common practice, these methods have previously achieved highly accurate results in a few BCI systems [30] [33] [34]. We evaluated two different multi-layer perceptrons for their computational light signal processing capacity and their high accuracies [35]. While one consists of 4 hidden layers, with 9, 18, 18, and 9 hidden neurons in each layer respectively; the other network is shallow, consisting of a single 10-neuron hidden layer. We trained both ANN structures using sigmoid activation and with the same inputs and the summed channels of the outputs with which the CCA-based filter was also generated, but staying independent from the CCA method. That is to say, the training inputs consist of the unprocessed EEG signal X of C -channels (from eq. 6), while the training outputs consisted of the signal \hat{X} (see eq. 8), averaged along the C channels, resulting in a one-dimensional signal, here denoted as H :

$$H = \frac{1}{C} \sum_{i=1}^C \hat{x}_i \quad (\text{eq. 12})$$

2.5 Classification and Evaluation

The classification procedure consisted of matching the processed one-dimensional feature set extracted from the EEG signals using each of the previously described decoding algorithms to one template from a set of T reference templates, where T is the number of classes (or targets) in the particular setup. All the necessary templates are obtained from the

consecutive circular shift of one reference template, T number of times. This initial reference template is obtained by averaging the EEG data from all the trials collected for the training subset, in the case of the experimental approach; and from the average of all signals generated as the training subset using the simulator, for the simulated approach. Since all stimulus targets are modulated by the same circularly-shifted PRBS, each resulting reference template can be associated with each individual target.

Once all templates are available after the training, the testing phase can be performed. In this phase, whichever reference template has the highest correlation coefficient with the feature set indicates which of the T target positions the BCI user is attempting to select, classifying it as such. Lastly, each of the 18 simulated configurations possible, as well as the decoding algorithms on the real data, were assessed by calculating the accuracy [%], with its variance, and the information transfer rate (ITR) expressed in bits/min.

Beyond evaluating all configuration parameters in the simulated framework, we are interested in assessing the reliability of the framework itself. To carry out this evaluation, we statistically compare the power spectra and the grand average ERPs obtained from both approaches, as well as the SNR-accuracy relationship in simulation. The following section describes the results of all analyses, while a discussion on their significance is contained in Section 4.

425 **3. Results**

426 The accuracy and ITR of the offline classification tests
 427 carried out on the experimental set are presented in *Figure*
 428 5(A), while those results achieved by the simulator in an
 429 identical setup (16 targets with APA modulation) are
 430 contained in *Figure 5(B)*. Also included in both accuracy
 431 graphs within *Figure 5* is the variance and statistical
 432 significance level ($p < 0.01$), the latter of which is indicated
 433 by a dashed horizontal line at 8.13% and represents the
 434 accuracy level that we expect less than 1% of a set of random
 435 16-target classifiers to obtain, as assessed against a binomial

478 80%. However, it is worth pointing out that all three Golay,
 479 APA, and DeBruijn modulation sequences achieve the most
 480 promising results in all cases, frequently without being
 481 significantly distant from each other.

482 Additionally, Linear-feedback shift register (m-
 483 Sequences), Gold, and Kasami sequences demonstrated
 484 substantially poorer performances in almost all scenarios. In
 485 particular, Kasami sequences resulted in an average
 486 decrement from the highest accuracy of -50.9%, -44.3%, and
 487 -48.5% throughout each of the 64, 32, and 16-target simulated
 488 configurations, respectively.

436 distribution (see [36]). This figure
 437 shows nearly equal scores obtained
 438 through both approaches using
 439 CCA, SNN, and DNN, reaching
 440 accuracies of 94.38%, 95.34%, and
 441 94.22%, in the respective
 442 experiments; and 95.63%, 95.94%,
 443 and 95.31%, in the respective
 444 simulations. Note, while both ICA
 445 and the PCA algorithm return
 446 much lower scores relative to the
 447 rest of the decoders in experiments
 448 and simulation, it must be noted
 449 that both approaches achieve
 450 significantly different scores,
 451 which is discussed in *Section 4.2*.

452 Proceeding with the evaluation
 453 through purely simulated means,
 454 *Figure 6* condenses the scores
 455 obtained by each of the possible
 456 BCI setups. From the upper
 457 portion of this figure, which
 458 contains the accuracies, variance,
 459 and significance level of each
 460 instance, there is a noticeable
 461 decline in the scores as the number
 462 of targets is increased. On the other
 463 hand, as can be observed from the
 464 information transfer rates shown in
 465 the lower section of *Figure 6*, this
 466 negative tendency is partially
 467 counteracted by this same increase
 468 in targets, resulting in the net
 469 relative increase of ITR with a
 470 higher target number.

471 Concerning the modulation
 472 sequence used, Golay sequences
 473 produced all of the highest
 474 accuracies in the 16-target setups,
 475 while Almost Perfect sequences
 476 provide the best results of 32 and
 477 64-target configurations above

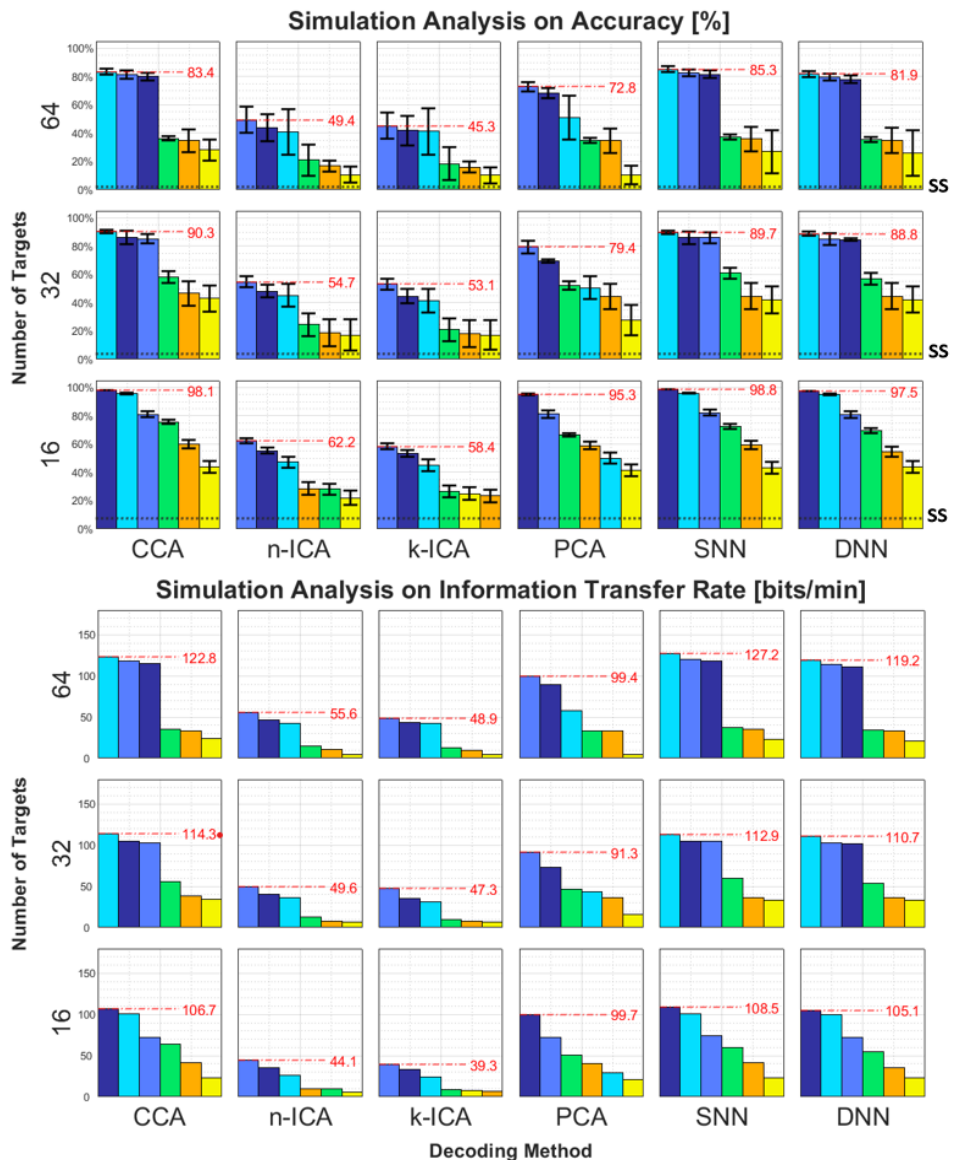


Figure 6. Simulated analysis results summary. (Upper) The accuracies obtained from all possible combinations of decoder, target number, and sequence type, with corresponding variances, and statistical significance levels (with p -value < 0.01) marked with a black dotted lines and the subscript "SS". (Lower) The corresponding ITRs calculated as a function of the number of targets and the accuracy of each setup. Additionally, the red dashed lines mark the maximum scores achieved within each one of the setups.

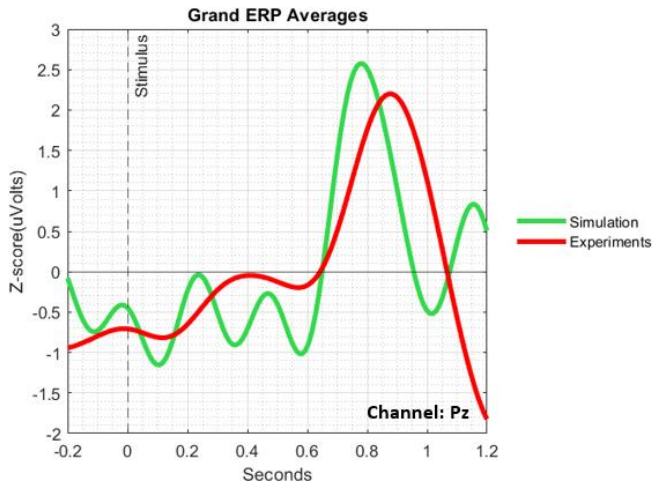


Figure 7. Grand ERP averages, z-scored. Grand ERP average of channel Pz from simulated data (green) and experimental data (red). Both are obtained by averaging over 20 cycles. The visual stimulus is presented at time zero.

509 Further analysis between signals obtained through both
 510 approaches can be done with the power spectra from all 9
 511 electrodes, shown in *Figure 8*. From this figure we can draw
 512 two conclusions: the frequency bands are greatly comparable
 513 since the relevant portions of both (the 0-50 Hz range
 514 approximately) are not statistically different based on a two-
 515 sample t-test with a significance level of $\alpha=0.05$; and that the
 516 simulation provides more orderly activation among the
 517 electrodes than the real EEG data provides, suggesting
 518 unrealistic response distribution among the electrodes, as well
 519 as slightly larger amplitudes in the higher frequencies before
 520 the cutoff at ~ 50 Hz (i.e. 30-40Hz).

521 Finally, *Figure 9* is intended to show the influence of the
 522 signal-to-noise ratio (SNR) coefficient of the simulator on the
 523 accuracy of each feature extractor. As detailed in *section 2.2.2*,
 524 a coefficient of 1 was set as a baseline for the SNR that
 525 provides the most realistic results, using the experimental data
 526 as a reference. The outcomes depicted were obtained by
 527 averaging the accuracies scored by the three setups using APA
 528 modulation (16, 32, and 64 targets), resulting in an inverted
 529 exponential relationship between SNR and the accuracy.

4. Discussion

4.1 On the BCI System

532 As previously stated, our results show that the SNN and
 533 CCA algorithms represent the most promising feature
 534 extractors for building c-VEP-based BCIs at a somewhat equal
 535 degree, since these achieve the highest scores throughout all
 536 numbers of targets without diverging significantly. However,
 537 by taking into account the considerably higher computational
 538 load and training time required to set up neural networks, we
 539 consider CCA a more favorable choice for an online system,
 540 especially if computing capacity is of the essence. The
 541 consistently inferior performances from the ICA and PCA
 542 algorithms suggest that these are not suitable for this type of
 543 BCI. Additionally, the correlation-based component selection
 544 procedure of ICA feature extraction (described in *Section*

489 Finally, concerning the impact of each feature extraction
 490 algorithm, the results demonstrate that both ICA algorithms
 491 get remarkably lower scores, while CCA and both NNs
 492 represent the most efficient decoding methods. Even though
 493 *Figure 6* suggests these three decoders are similarly
 494 competent, the SNN notably achieves the highest accuracy of
 495 98.8% with a 16-target Golay setup and the maximum ITR of
 496 127.2 bits/min with an APA 64-target system.
 497 Proceeding with the evaluation of the simulator properties,
 498 a comparison of the normalized grand ERP averages and
 499 power spectra of both data acquisition approaches is shown in
 500 *Figure 7* and *Figure 8*, respectively. We can observe that the
 501 morphologies of the positive peaks from the simulated and
 502 experimental responses in *Figure 7* are noticeably similar,
 503 with no statistically significant difference based on a two-
 504 sample t-test with a significance of $\alpha=0.05$. Still, there is an
 505 approximate deviation of 11.9% between both response
 506 latencies, and approximately a 14.6% increase in the
 507 amplitude of the simulator's ERP relative to the one generated
 508 with real EEG data.

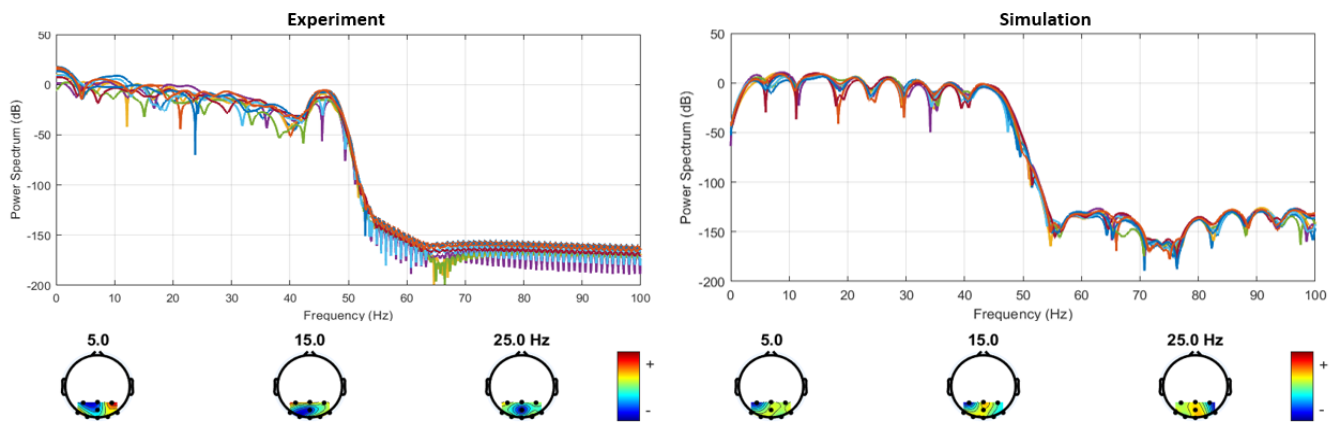


Figure 8. The frequency power spectrum was obtained from experimental (left) and simulated (right) c-VEP datasets. With a topological activation map of the regions with electrodes at 5, 15, and 25 Hz for each approach.

545 2.4.3) is a non-ideal process in terms of
 546 computation, since the number of calculations
 547 greatly increases along with an increase in the
 548 number of targets, which in an online system
 549 represents a reduction of processing speed.

550 We also conclude that among the PRBS
 551 investigated with simulation, Golay,
 552 DeBruijn, and Almost Perfect sequences are
 553 the most effective for stimuli modulation.
 554 While APA sequences are fairly common in c-
 555 VEP studies, Golay and DeBruijn sequences
 556 have only been implemented to a very limited
 557 extent, which prompts a highly interesting
 558 hypothesis for further testing through non-
 559 simulated means. Furthermore, the
 560 consistently suboptimal results obtained with
 561 the Kasami, Gold, and m-Sequence PRBS
 562 suggest that these have unfavorable characteristics for code-
 563 modulated BCIs.

564 Finally, as indicated earlier, the increase in the number of
 565 targets in the BCI results in a noticeable decline in the
 566 accuracy of all of the configurations. This highlights the
 567 limited scalability of numbers of targets in c-VEP BCI
 568 systems, as noted by [14] and [20]. This tendency is likely due
 569 to the nature of the correlation classifier, since as the number
 570 of classes increases, the discrimination between consecutive
 571 targets has lower classification tolerance, becoming less
 572 reliable. Taking this into account, we consider that a direct
 573 increment in the number of stimuli without additional
 574 modifications to the BCI structure is not practical nor
 575 dependable.

576 4.2 On the EEG Simulator

577 Regarding the reliability of realistic c-VEP simulation, we
 578 first observe some non-significant inconsistencies in the grand
 579 ERP averages and power spectra of *Figures 7 and 8*. However,
 580 perhaps the most notable discrepancy concerns the results
 581 obtained from both ICAs and PCA in *Figure 5*. This figure
 582 shows significant differences in accuracy between the same
 583 feature extractors in identical setups. Since we can rule out the
 584 SNR as the origin of these inconsistencies based on the result
 585 in *Figure 9* (showing relatively little variation throughout the
 586 whole range), and the discrepancy is exclusive to component
 587 analysis algorithms, we estimate that it derives from
 588 insufficiently realistic component rankings and orthogonality
 589 among data sources. Therefore, we conclude that the biggest
 590 shortcoming identified in the simulator originate from the
 591 limitations of the simulated electrodes and head model,
 592 resulting in significantly more favourable performance in the
 593 PCA algorithm's orthogonal transformations.

594 While we do acknowledge numerous areas of improvement
 595 for the EEG simulator, within the scope of this study, we
 596 consider that the operation and results achieved through a

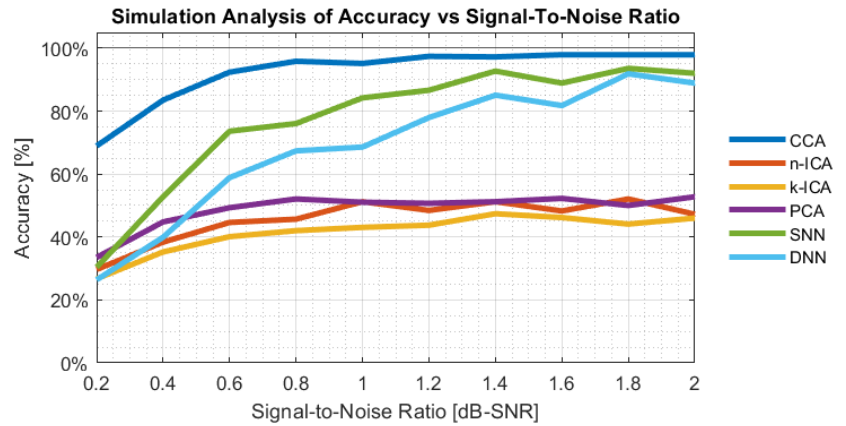


Figure 9. Analysis of the averaged influence of the simulated SNR coefficient on the accuracy of the BCI for each of the feature extractor methods in all target setups with an APA sequence. The x-axis represents the dB ratio between the signal and noise components in the EEG simulation.

597 simulated approach are satisfactory. It effectively provided a
 598 genuinely practical, flexible, and robust platform for in-depth
 599 BCI analysis, with a certain degree of dependability. We
 600 believe, it is a powerful framework and a highly promising
 601 tool for streamlining the development of modern high-
 602 performance brain-computer interfaces. Undoubtedly, more
 603 sophisticated and realistic simulations will further benefit the
 604 development of BCIs in the future.

605 4.3 Future work

606 The majority of the observations and results obtained in this
 607 study suggest promising methodologies and parameters, but
 608 also demand future experimentation. Particular effects of
 609 interest include the effects of the Golay and DeBruijn
 610 sequences, new paradigms to increase the number of targets
 611 per system, and the optimization of the ANN architecture in
 612 the feature extraction stage with a comparable speed to that
 613 achieved through CCA-based processing.

614 More sophisticated signal processing algorithms are
 615 perhaps the development with the most potential to influence
 616 the performance of c-VEP BCI systems. Although
 617 computational requirements should be taken into
 618 consideration, we consider the integration of multiple
 619 advanced methodologies for signal decoding (i.e.
 620 convolutional neural networks, fuzzy logic), classification
 621 (i.e. Support Vector Machines, k-Nearest Neighbour), and
 622 methodologies that optimize user adaptability [7], such as
 623 higher modulation frequencies and stimulation sequences that
 624 move beyond binary presentation modalities, comprise the
 625 contemporary priorities of c-VEP BCI implementations.

626 Finally, we consider that the insights and advancements
 627 made on realistic c-VEP simulation represent a tool that will
 628 likely provide highly significant benefits to all types of code-
 629 modulated BCIs. A simulated framework provides
 630 unparalleled practicality and control and is an approach for
 631 which we strongly encourage further development.

5. Conclusion

In this paper, we evaluated the effects of various feature extractors, modulation sequences, and the number of targets in the stimulus interface on the accuracy and information transfer rates of c-VEP BCI systems. We utilized both real and generated EEG datasets through simulation, evaluating the characteristics of the latter, and ultimately assessing its reliability. We were able to achieve a maximum information transfer rate of 127.2 bits/min with a 64-targets setup using an Almost Perfect Autocorrelation sequence for modulation, and 98.8% accuracy in a Golay-modulated 16-target system, both with a shallow neural network as a feature extractor.

Our results suggest several branching paths for the research and development of contemporary c-VEP BCI systems. Most notably our results suggest that the Golay and DeBruijn sequences, studies of which are not extensive, are highly effective for c-VEP BCI performance. We observed that the CCA and SNN methods represent the most effective feature extractors compared to multiple typical algorithms. Finally, we explored a realistic simulation framework, which not only achieved satisfactory fidelity but also provided highly valuable flexibility and exceptional accessibility to the processing pipeline analysis of a c-VEP-based BCI.

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