Dynamic Movement Primitives-Based Human Action Prediction and Shared Control for Bilateral Robot Teleoperation

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Abstract—This article presents a novel shared-control teleoperation framework that integrates imitation learning and bilateral control to achieve system stability based on a new dynamic movement primitives (DMPs) observer. First, a DMPs-based observer is first created to capture human operational skills through offline human demonstrations. The learning results are then used to predict human action intention in teleoperation. Compared with other observers, the DMPs-based observer incorporates human operational features and can predict long-term actions with minor errors. A high-gain observer is established to monitor the robot's status in real time on the leader side. Subsequently, two controllers on both the follower and leader sides are constructed based on the outputs of the observers. The follower controller shares control authorities to address accidents in real-time and correct prediction errors of the observation using delayed leader commands. The leader controller minimizes position-tracking errors through force feedback. The convergence of the predictions of the DMPsbased observer under the time delays and teleoperation system stability are proved by building two Lyapunov functions. Finally, two groups of comparative experiments are conducted to verify the advantages over other methods and the effectiveness of the proposed framework in motion prediction with time delays and obstacle avoidance.

Index Terms—Dynamic movement primitives (DMPs), shared control, stability proof, teleoperation, time delay.

I. INTRODUCTION

T ELEOPERATION technology has been widely used for exploration in the deep sea and toxic environments, and

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nuclear decommissioning, which enhances human reachability and delivers human actions to guide the movements of robots. Shared control is a typical control mode in teleoperation [1], [2]. However, due to the time delays, the commands sent from the leader side may not be able to respond in real time to the accidents that happened on the remote robot side. Therefore, shared control, allowing robot controllers to share the control authority between the autonomous reactions and the time-delayed action commands from leader side, can balance control requirements of both humans and robots to enable the effective interventions in emergencies [3], [4].

Generally, the two agents of teleoperation share information, such as velocity, position, and force to realize semiautonomous control (SAC). Some researchers extended the sharing of information to impedance [5], [6] and haptic information [7], [8] to improve system dexterity and manipulability through robot's autonomy. As reviewed in [9], shared control can be classified into three categories: SAC, state-guidance shared control (SGSC), and state-fusion shared control (SFSC), according to the sharing ways between humans and robots. Among the three classes, the SFSC has an innate and essential advantage in the seamless autonomy-level adaptation owing to the arbitration mechanism. For example, Ezeh et al. have proposed a probabilistic fusion mechanism to combine human's intended motions and autonomous planner's actions to control a wheelchair [10]. Selvaggio et al. proposed a shared-control teleoperation framework for robot manipulators, which transport an object on a tray, which considered the case that an object breaks contact with the robot end-effectors. The shared-control method could regulate the remote robot's movement to prevent the object from sliding over the tray [11]. Gottardi et al. proposed a real-time shared-control teleoperation framework that integrated an artificial potential field which is improved by the dynamic generation of escaping points around obstacles to overcome obstacles [13]. The methods addressed the problems in certain tasks such as preventing object sliding [10]. However, the robot's autonomous control was based on certain principles instead of human motion intentions.

Some researchers have addressed this problem by integrating imitation learning and teleoperation [12], [13], [14], [15], [16], [17]. The objective is to enable robots to learn skills from human demonstrations first, and then these skills are generalized for the shared control with delayed human inputs. Typically, an arbitration mechanism is introduced to mediate between robots and humans. As outlined in [9], this arbitration mechanism takes the

forms of weighted combination, probabilistic fusion, and phase switching. For example, Xi et al. proposed a shared-control framework where manipulation skills are learned by a taskparameterized hidden semi-Markov model (TP-HMM) from human demonstrations. The estimation of robots based on learning results can correct the inputs of the operators and provide manipulation assistance [14]. El-Hussieny et al. extracted human hand positions and proposed a framework with two key components: intention prediction and command arbitration to reduce control time and labor burden [16]. Ly et al. proposed a sharedcontrol paradigm incorporating robot actions learned from human demonstrations and dynamically adjusting the level of robotic assistance based on how closely the detected intentions match these trajectories. Human motion intention was predicted by a deep Q-network (DQN) with consideration of current robot states and baseline trajectories learned using probabilistic movement primitives to generate adaptive force guidance [17].

These frameworks can improve robot manipulation dexterity through learning from human demonstration. However, there are several key problems have not been solved: 1) the learned skills are not updated timely by human online intervention. The suitability of the learning results is questioned; 2) the key influence factor, time delay, is not considered; and 3) dynamics uncertainties and various errors are few considered, and system stability is not strictly proved in theory [13]. For the questions, we developed a dynamic movement primitives (DMPs)-based observer to make a timely prediction and correction of human intentions. Then, a shared-control teleoperation framework is developed with the following contributions.

- We develop a DMPs-based observer capable of predicting human action intentions and correcting the predictions using delayed tracking errors. The observer can be applied independently and adjusted to be integrated into the teleoperation system to enhance robot autonomy.
- 2) We build a new shared-control framework for teleoperation systems based on observers. The DMPs-based observer is used to estimate human intentions on the leader side, while the high-gain observer predicts the state of robots in real time. Signal measuring errors and uncertain dynamics are taken into consideration in the controller design.
- 3) We prove the convergence of estimations from the DMPsbased observer and prove the stability of the shared-control teleoperation system under varying time delays by creating two Lyapunov functions. The effectiveness of the proposed framework is validated through two experiments.

II. PRELIMINARY WORK

A. Model of Teleoperation System

Using the symbols described in Table I, the teleoperation system in a Lagrange form is expressed as

$$\begin{cases} M_{l}(q_{l})\ddot{q}_{l} + C_{l}(q_{l},\dot{q}_{l})\dot{q}_{l} + G_{l} = J_{l}^{T}(q_{l})F_{h} - \tau_{l} \\ M_{f}(q_{f})\ddot{q}_{f} + C_{f}(q_{f},\dot{q}_{f})\dot{q}_{f} + G_{f} = \tau_{f} - J_{f}^{T}(q_{f})F_{e} \end{cases}$$
(1)

where $M_i(q_i)$ and $C_i(q_i, \dot{q}_i)$, i = l, f are the inertia matrix and the centripetal and Coriolis matrix, which are expressed as M_i and

TABLE I Symbols and Meanings

Symbols	Meanings
$q_i, i = l, f$	Joints of robots and manipulators, and <i>i</i> represent the agent
	in the leader and follower sides
d_t	Time delays
$q^{dt}, q(t-d_t)$	Delayed signals with the time delay d_t
q_i, \hat{q}_i	Real value and estimation of robot joints
$ au_i$	τ_i is control torque
η_i	Estimation errors $\eta_i := q_{\overline{i}} - \hat{q}_i, \overline{i}$ is the opposite role to <i>i</i> in
	the set (l,f)
e_i	Control errors $e_i := q_i - \hat{q}_i$
F_h	Human force exerting on the manipulator
F_{e}	Environmental force against the robots

 C_i in simple, G_i is the gravitational torque, and $J_i(q_i)$ is the Jacobian matrix. F_h is the human operational force and $F_e = K_x(x_f - x_f^0) + D_x \dot{x}_f$ is the environment force, where K_x and D_x are stiffness and damping factors, x_f represents the position of the robot end. τ_l and τ_f represent the control torques.

Several assumptions and a lemma are presented as follows.

Assumption 1 [19]: The communication delays are bounded: $d_t \leq d_t \leq \overline{d}_t$ and the time derivative of d_t satisfies $0 < |\dot{d}_t| \leq \mu_t < 1$, where μ_t is a constant factor.

Assumption 2 [20], [23]: Due to the measuring noise and time delays in measurement, there exists the following relationship: $|\overline{F}_e - F_e| \leq \beta_e$, $|K_e \overline{F}_h^e - F_h| \leq \beta_h$, where \overline{F}_e is the environmental force measurements and \overline{F}_h^e represents the rendering force in the leader side, and β_e , β_h , and K_e are positive constants.

Assumption 3 [21]: The symmetric positive definite matrices M_l and M_f , and inverse matrices M_l^{-1} and M_f^{-1} are bounded

$$\lambda_{\min}(M_i)I \le M_i \le \lambda_{\max}(M_i)I$$

$$\lambda_{\min}(M_i^{-1})I \le M_i^{-1} \le \lambda_{\max}(M_i^{-1})I$$
(2)

with the minimum and maximum eigenvalues of $\lambda_{\min}(M_i)$, $\lambda_{\max}(M_i)$, $\lambda_{\min}(M_i^{-1})$, and $\lambda_{\min}(M_i^{-1})$, i = l, f.

Assumption 4 [22]: Matrix $\dot{M}_i - 2C_i$, i = l, f is symmetric and C_i is bounded by a quadratic term of the joint velocities \dot{q}_i

$$\|C_{i}(q_{i},\dot{q}_{i})\dot{q}_{i}\| \leq \|C_{i}^{b}(q_{i})\| \|\dot{q}_{i}\|^{2}$$
(3)

where $C_i^b(q_i)$ is a scalar function. For a robot with all revolute joints, $C_i^b(q_i)$ is constant.

Lemma 1 (Jensen's Integral Inequality) [21]: For any constant matrix $M \in \mathbb{R}^{n \times n}$, $M = M^T < 0$, a scalar $\vartheta < 0$, a vector function $w(s) : [0, \vartheta] \rightarrow n$ such that the integrations concerned are well defined, then

$$\left[\int_{0}^{\vartheta} w(s)ds\right]^{T} \mathbf{M}\left[\int_{0}^{\vartheta} w(s)ds\right] \leq \vartheta \int_{0}^{\vartheta} w^{T}(s)\mathbf{M}w(s)ds.$$
(4)

B. DMPs

The DMPs model is usually expressed as [24]

$$\begin{cases} \tau \dot{z} = K(g - y) - Dz + (g - y_0)f(s) \\ \tau \dot{y} = z \end{cases}$$
(5)

where K, D > 0 are stiffness and damping factors and $\tau > 0$ is a timing parameter for adjusting the duration of the trajectory *y*. y_0 and *g* are the start and the end position of the trajectory *y* and *y* represent the velocity. Generally, in order to enable *y* converge to *g*, *K*, and *D* satisfy $K = 4D^2[24]$. $f(s) = \theta^T \Psi(s)$ is a combination of normalized Gaussian functions ψ_j , where $\theta = [w_1, w_2, ..., w_n]^T, \Psi(s) = [\psi_1, \psi_2, ..., \psi_n]^T$, and w_j is a weight term and the expression of state variable ψ_j is as follows:

$$\psi_{j} = \frac{\varphi_{j}(s)s}{\sum_{i=1}^{n} \varphi_{i}(s)}, \varphi_{j}(s) = \exp(-h_{j}(s-c_{j})^{2})$$
(6)

where c_j and $h_j > 0$ are the centers and widths of the radial basis function $\varphi_j(s)$. The number of n, and the center c_j and bandwidth h_j can be set automatically by using nonparametric regression technique from locally weighted learning (RFWR) [25], [26]. The transformation function (or named as forcing function) f(s) has a phase variable s, which is calculated by a canonical system

$$\tau \dot{s} = -\gamma s, \qquad \gamma > 0. \tag{7}$$

The converging time is modified by factor γ to make sure $s \to 0$ at the end of trajectory for erasing the influence of f(s). The θ is estimated by minimizing $||f^{\text{Tar}}(s) - f(s)||$, where $f^{\text{Tar}}(s)$ is calculated by y and z in the demonstration

$$f^{\mathrm{Tar}}(s) = (\tau \dot{z} - K(g - y) - Dz)/(g - y_0).$$
(8)

III. CONTROL DIAGRAM

As illustrated in Fig. 1, the diagram is based on the bilateral control framework of teleoperation, similar to [15]. This control system comprises one observer and one controller on both the leader and follower sides, respectively. The observations serve for robotic autonomy on the follower side and feedback force rendering on the leader side and are then shared and controlled with delayed feedback from the remote side. The following sections will introduce these modules in sequence.

A. DMPs-Based Observer

Set $Y = \begin{bmatrix} y & z \end{bmatrix}^T$, then (5) can be rewritten as

$$\dot{Y} = K_1 Y + K_2 + \frac{g - y_0}{\tau} F(s)$$
 (9)

where $K_1 = \frac{1}{\tau} \begin{bmatrix} 0 & 1 \\ -K & -D \end{bmatrix}$, $K_2 = \frac{1}{\tau} \begin{bmatrix} 0 \\ Kg \end{bmatrix}$ and $F(s) = \begin{bmatrix} 0 \\ f(s) \end{bmatrix}$.

Set \hat{Y} as the estimation of *Y*, then an observer based on (9) is created as

$$\dot{\hat{Y}} = K_1 \hat{Y} + K_2 + K_n (Y(t - d_t) - \hat{Y}(t - d_t)) + \frac{g - y_0}{\tau} F^U(s)$$
(10)

where the estimation error $\Delta Y = Y - \hat{Y}$ will be compensated by the known errors $Y(t - d_t) - \hat{Y}(t - d_t)$ after receiving $Y(t - d_t)$ after the time delay d_t . K_n is a positive factor and $F^U(s)$ is initialized by (5) and updated in the following calculation.



Fig. 1. Illustration of sketch map of system control diagram.

Since new operational actions may be different from those in demonstration, we express the real-time and the delayed human actions as *Y* and *Y*(*t* - *d_t*), which can be also expressed by the DMPs with a different $F^{N}(s)$ as

$$\dot{Y} = K_1 Y + K_2 + \frac{g - y_0}{\tau} F^N(s).$$
 (11)

Then, according to (10) and (11), we can get the following:

$$\dot{Y} - \dot{\hat{Y}} = K_1(Y - \hat{Y}) - K_n(Y(t - d_t) - \hat{Y}(t - d_t)) + \frac{g - y_0}{\tau} (F^N(s) - F^U(s))$$
(12)

where $F^{N}(s) - F^{U}(s)$ represents the difference of two forcing functions. Equation (12) can be simplified as

$$\Delta \dot{Y} = K_1 \Delta Y - K_n \Delta Y(t - d_t) + \frac{g - y_0}{\tau} (F^N(s) - F^U(s)) \quad (13)$$

where $\Delta Y = \hat{Y} - Y$. We set $f^U(s)$ and $f^N(s)$ are calculated based on the same kernels $\Psi(s)$, that is,

$$\begin{cases} f^N(s) = (\theta^N)^T \Psi(s) \\ f^U(s) = (\theta^U)^T \Psi(s). \end{cases}$$
(14)

Then, the errors of two forcing functions are expressed as

$$F^{N}(s) - F^{U}(s) = \begin{bmatrix} 0\\ f^{N}(s) - f^{N}(s) \end{bmatrix}$$
$$= \begin{bmatrix} 0\\ (\theta^{N} - \theta^{U})^{T} \Psi(s) \end{bmatrix} = \begin{bmatrix} \theta\\ \tilde{\theta}^{T} \Psi(s) \end{bmatrix}$$
(15)

and (13) will be updated by

$$\Delta \dot{Y} = K_1 \Delta Y - K_n \Delta Y(t - d_t) + \frac{g - y_0}{\tau} \begin{bmatrix} 0\\ \tilde{\theta}^T \Psi(s) \end{bmatrix}$$
(16)
$$= K_1 \Delta Y - K_n \Delta Y(t - d_t) + G \tilde{\Theta}^T \Psi(s)$$

where $\tilde{\Theta} = \begin{bmatrix} 0 & \tilde{\theta} \end{bmatrix}^T$ and $G = (g - y_0)/\tau$. Since in (11), the θ^N is recognized as a desired value for θ^U , then set $\Theta = \begin{bmatrix} 0 & \theta^U \end{bmatrix}^T$ and use (17) to update θ^U to enable \hat{Y} to approach Y

$$\dot{\Theta} = (g - y_0)\Psi(s)\Gamma\Delta Y$$
 (17)

where Γ is a constant matrix as transformation of vector ΔY .

Since Θ desires to converge to $\Theta^N = \begin{bmatrix} 0 & \theta^N \end{bmatrix}^T$, then the parameter estimation error exists $\dot{\tilde{\Theta}} = \dot{\Theta}^N - \dot{\Theta}$ and has the following:

$$\tilde{\Theta} = -(g - y_0)\Psi(s)\Gamma\Delta Y.$$
(18)

Using Schur Complement, the sufficient stable condition for the stability of the estimation \hat{Y} is shown in Theorem 1:

Theorem 1: For the observer (10) with a weight updating rate (17), if there exist positive matrices Ξ_1 , Ξ_2 , Ξ_3 , and Q such that the following LMIs holds:

$$\Xi = \begin{bmatrix} \Gamma_{11} & \Gamma_{12} & \Gamma_{13} \\ * & \Gamma_{22} & \Gamma_{23} \\ * & * & \Gamma_{33} \end{bmatrix} < 0$$
(19)

where $\Gamma_{11} = \Xi_1 + 2K_1\Xi_3 + (\overline{d}_t^2 K_1^2 - I)\Xi_2, \ \Gamma_{12} = \Xi_2 - \overline{d}_t^2 K_1 K_n$ $\Xi_2 - K_n\Xi_3, \ \Gamma_{13} = G(\overline{d}_t^2 K_1\Xi_2 + \Xi_3) + \Gamma Q(g - y_0), \ \Gamma_{22} = \overline{d}_t^2$ $GK_n\Xi_2, \ \Gamma_{23} = -G(K_n\Xi_2 + (g - y_0)\Gamma Q\tau), \ \Gamma_{33} = \overline{d}_t^2 G^2 \Xi_2.$

Then, the estimation error ΔY and Θ will converge to 0.

Remark 1 : The proof of system convergence is presented in Section IV-A. However, it should be noted that the observer (10) is constructed based on the same K_1 and K_2 as those in (11), demonstrated by humans. This implies that the start and end points of the trajectory are known before teleoperation. The update of Θ in (17) is to facilitate the predicted movements \hat{Y} in (10) to track human teleoperation actions Y in (9).

B. High-Gain Observer in the Leader Side

As the movement of robots cannot be regularized as humans' movement in DMPs, we build a high-gain nonlinear observer to estimate the actions of robots. According to (1), we have the following:

$$\ddot{q}_f = M_f(q_f)^{-1}(\tau_f - J_f^T(q_f)F_e - C_f(q_f, \dot{q}_f)\dot{q}_f - G_f).$$
(20)

Set $Q = [q_f, \dot{q}_f]^T$, $\hat{Q} = [x_l, v_l]^T$, and the left formula of \ddot{q}_f in (20) as $\Phi(q_f, \dot{q}_f, \tau_f, F_e)$, where x_l and v_l are observations of q_f and \dot{q}_f from the leader view, then the desired values of the observations \hat{Q}^d can be expressed as

$$\dot{\hat{Q}}^{d} = \begin{bmatrix} \dot{x}_{l} \\ \dot{v}_{l} \end{bmatrix}^{d} = \begin{bmatrix} \dot{q}_{f} \\ \Phi(x_{l}, v_{l}, \tau_{f}, F_{e}) \end{bmatrix}$$

$$= \begin{bmatrix} v_{l} M_{f}(x_{l})^{-1} (\tau_{f} - J_{f}^{T}(x_{l}) F_{e} - C_{f} v_{l} - G_{f}) \end{bmatrix}.$$
(21)

The desired value is $\hat{Q}^d = Q$. Defining $\eta_l = q_f - x_l$ as the estimation errors, the following high-gain observer is:

$$\dot{\hat{Q}} = \begin{bmatrix} \dot{x}_l \\ \dot{v}_l \end{bmatrix} = \begin{bmatrix} v_l + \ell k_1 \eta_l^{dt} \\ \hat{\Phi} (x_l, v_l, \tau_f, F_e) + \ell^2 k_2 \eta_l^{dt} \end{bmatrix}$$
(22)

where ℓ is a high gain of the observer, and k_1 and k_2 are the two positive factors. According to [15], the essential Lipschitz-like condition holds for a constant factor $L_{\delta} > 0$ with Q and its estimation \hat{Q} to ensure the asymptotic stability of the feedback system using the observer in (22) as

$$\left| \begin{bmatrix} 0, \quad \Phi \left(q_f, \dot{q}_f, \tau_f, F_e \right) - \quad \hat{\Phi} \left(x_l, v_l, \tau_f, F_e \right) \end{bmatrix}^T \right| \le L_{\delta} |Q - \hat{Q}|. \tag{23}$$

According to Assumptions 3 and 4 and the properties of the Lagrangian system (1), $M_f(q_f)^{-1}$, $C_f(q_f, \dot{q}_f)\dot{q}_f$, $J_f^T(q_f)$, and G_f are bounded. Meanwhile, F_e and control torque τ_l are also bounded. Then, $\Phi(q_f, \dot{q}_f, \tau_f, F_h)$ and $\hat{\Phi}(x_l, v_l, \tau_f, F_e)$ are bounded and there exists a L_{δ} satisfying condition in (23).

Setting
$$\tilde{Q} = [q_f - x_l, \ell^{-1}(\dot{q}_f - v_l)]^T$$
 and $\overline{K}_e = \begin{bmatrix} -k_1 e^{-dt} & 1\\ -k_2 e^{-dt} & 0 \end{bmatrix}$
< 0, and using (21) and (22), we can get the following:

$$\begin{split} \dot{\tilde{Q}} &= [\dot{q}_{f} - \dot{x}_{l} \cdot \ell^{-1} (\ddot{q}_{f} - \dot{v}_{l})]^{T} \\ &= \begin{bmatrix} \dot{q}_{f} - v_{l} - \ell k_{1} e^{-dt} \eta_{l} \\ \ell^{-1} (\Phi(q_{f}, \dot{q}_{f}, \tau_{f}, F_{e}) - \hat{\Phi}(x_{l}, v_{l}, \tau_{f}, F_{e}) - \ell^{2} k_{2} \dot{\overline{d}}_{t} e^{-dt} \eta_{l}) \end{bmatrix} \\ &= \ell \begin{bmatrix} -k_{1} e^{-dt} & 1 \\ -k_{2} e^{-dt} & 0 \end{bmatrix} \tilde{Q} + \begin{bmatrix} 0 \\ \ell^{-1} (\Phi(q_{f}, \dot{q}_{f}, \tau_{f}, F_{e}) - \hat{\Phi}(x_{l}, v_{l}, \tau_{f}, F_{e})) \end{bmatrix} \\ &= \ell \overline{K}_{e} \tilde{Q} + \Delta(q_{f}, \dot{q}_{f}, x_{l}, v_{l}, \tau_{f}, F_{e}). \end{split}$$
(24)

So, for a high gain $\ell \gg 1$, (24) will be dominated by term $\ell \overline{K}_e \tilde{Q}$, and the term $\Delta(q_f, \dot{q}_f, x_l, v_l, \tau_f, F_e)$ satisfies the following:

$$\left|\Delta(q_f, \dot{q}_f, x_l, \nu_l, \tau_f, F_e)\right| \le \frac{L_{\delta}}{\ell} \left|\tilde{\mathcal{Q}}\right| \le L_{\delta} \left|\tilde{\mathcal{Q}}\right| \tag{25}$$

to ensure that the estimation error \hat{Q} converge to 0 finally. The stability conditions and measurements for eliminating negative effects of high gain can refer to [18].

C. Controller Design in the Follower and Leader Side

In Sections III-A and III-B, two observers are built to estimate the timely motions of the agents on both sides in teleoperation. These estimations will be used as current control references in local site. Define two errors in the follower side $e_f := q_f - \hat{q}_f$ and $\eta_f := q_l - \hat{q}_f$ to represent tracking errors to estimations and estimating errors to the desired positions, then we can set two error terms $r_f := \dot{\eta}_f + k_\eta^f \eta_f$, $\varepsilon_f := \dot{e}_f + k_e e_f$, where k_η^f and k_e are constants, then the control torque τ_f in the follower side is designed as

$$\tau_f = M_f(q_f)(\hat{q}_f - k_e \dot{e}_f) + C_f(q_f, \dot{q}_f)(\hat{q}_f - k_e e_f) + G_f - \xi_1 \varepsilon_f - (1 - \xi_1) r_f^{dt} + J_f^T(q_f) \overline{F}_e + \sigma_f$$
(26)

where \overline{F}_e represents the measurement of F_e and \hat{q}_f is estimated based on (10) and detailed as

$$\tau^2 \ddot{\hat{q}}_f = K(g - \hat{q}_f) - D\tau \dot{\hat{q}}_f - K_n r_f^{dt} + (g - q_0) f^u(s)$$
(27)

where $f^{u}(s) = (\theta^{u})^{T} \Psi(s)$ and θ^{u} is updated as

$$\dot{\theta}^{u} = \frac{g - q_0}{\tau^2} \Psi(s) r_f \tag{28}$$

where $\xi_1 \in (0, 1)$ is a constant factor for shared control. The ξ_1 is for robot autonomy and $1 - \xi_1$ is for human delayed inputs, and their values are determined by Theorem 2. Set the finalized weight learned in (11) as constant θ^n , similar to (18), the factor

 $\tilde{\theta} := \theta^n - \theta^u$ is updated as

$$\dot{\tilde{\theta}} = -\frac{g-q_0}{\tau^2} \Psi(s) r_f \tag{29}$$

and σ_f is a saturated term for the force measuring errors

$$\sigma_f = \phi_f(\alpha_f, \varepsilon_f, \mathbf{o}_f) = \begin{cases} -\varepsilon_f / \|\varepsilon_f\| \cdot \alpha_f, & \text{if } \alpha_f \ge \mathbf{o}_f \\ -\varepsilon_f / \|\varepsilon_f\| \cdot \mathbf{o}_f, & \text{if } \alpha_f < \mathbf{o}_f \end{cases}$$
(30)

where α_f satisfies $|J_f^T(q_f)(\overline{F}_e - F_e)| \leq |J_f^T(q_f)||\overline{F}_e - F_e| < \alpha_f$ and the $|J_f^T(q_f)|$ and the force error term $|\overline{F}_e - F_e|$ are bounded, and o_f denotes a positive term. Taking τ_f into (1), we can get the following:

$$M_{f}(\ddot{q}_{f} - \ddot{\hat{q}}_{f} + k_{e}\dot{e}_{f}) + C_{f}(\dot{q}_{f} - \dot{\hat{q}}_{f} + k_{e}e_{f}) = M_{f}\dot{\varepsilon}_{f} + C_{f}\varepsilon_{f} = -\xi_{1}\varepsilon_{f} - (1 - \xi_{1})r_{f}^{dt} + J_{f}^{T}(q_{f})(\overline{F}_{e} - F_{e}) + \sigma_{f}$$
(31)

The leader controller τ_l is designed with new-defined terms $\eta_l^x := q_f - x_l, \eta_l^v := \dot{q}_f - v_l, e_l := x_l - q_l, \dot{e}$ $l := v_l - \dot{q}_l, \varepsilon_l := \dot{e}_l + k_e e_l$, and $r_l^{dt} := \eta_l^v (t - dt) + k_\eta^l \eta_l^x (t - dt)$, k_η^l is constant. Then, τ_l is as follows:

$$\tau_{l} = M_{l}(q_{l})(\dot{v}_{l} - k_{e}\dot{e}_{l}) + C_{l}(q_{l}, \dot{q}_{l})(v_{l} - k_{e}e_{l}) + J_{l}^{T}(q_{l})\beta\overline{F}_{h}^{e} + G_{l} + \xi_{2}\varepsilon_{l} + (1 - \xi_{2})r_{l}^{dt} + \sigma_{l}$$
(32)

where \overline{F}_{h}^{e} represents the haptic force feedback in the leader side, simulated F_{e} by estimation of $\overline{F}_{h}^{e} = \hat{K}_{x}J_{f}^{T}(q_{f})e_{i} + \hat{D}_{x}\dot{e}_{i}$, to generate a virtual force generated by position errors e_{i} , and the stiffness and damping factors \hat{K}_{x} and \hat{D}_{x} . ξ_{3} is a shared-control parameter in the leader side, similar to ξ_{3} in (26). σ_{l} is a robust term with $\sigma_{l} = \phi_{l}(\alpha_{l}, \varepsilon_{l}, o_{l})$ and $|J_{l}^{T}(q_{l})(\overline{F}_{h} - F_{h})| < \alpha_{l}$.

The system stability condition is presented in Theorem 2 and the proof of system stability is presented in Section IV-B.

Theorem 2: For system (1) with controller (26) and (32), if there exist positive matrices E_1 and E_2 such that the following LMIs holds:

$$E_{1} = \begin{bmatrix} H_{11} & 0 & H_{13} \\ * & H_{22} & H_{23} \\ * & * & H_{33} \end{bmatrix} < 0, \ E_{2} = \begin{bmatrix} \Gamma_{11} & 0 & \Gamma_{13} \\ * & \Gamma_{22} & 0 \\ * & * & \Gamma_{33} \end{bmatrix} < 0$$
(33)

where $H_{11} = -\xi_1$, $H_{22} = k_2 - 2k_1 K/\tau^2$, $H_{33} = -k_2(1 - \mu_t)$, $H_{13} = (\xi_1 - 1)/2$, $H_{23} = k_1 K_n/\tau^2$, $\Gamma_{11} = -\xi_2$, $\Gamma_{13} = (\xi_2 - 1)/2$, $\Gamma_{22} = 2k_3 k_\eta^l + k_4 + 2k_3 L_\delta$, $\Gamma_{33} = -k_4(1 - \mu_t)$, and then the system (1) is robust asymptotic stable with the following parameters $k_\eta^f = D\tau/(\tau^2 + K)$, $k_\eta^l = \ell/2$ $(\pm \sqrt{k_1^2 - 4k_2} - k_1)$, and $k_1, k_2, k_3, k_4 > 0$.

IV. CONVERGENCE AND STABILITY PROOFS

A. Proof of Convergence of DMPs-Based Observations

Set a Lyapunov function $V_o = V_1 + V_2$ for the observer (10)

$$\begin{cases} V_1 = \int_{t-dt}^{t} \Delta Y^T \Xi_1 \Delta Y + \int_{-dtt+\theta}^{0} \int_{-dtt+\theta}^{t} \Delta \dot{Y}^T \Xi_2 \Delta \dot{Y} \\ V_2 = \Delta Y^T \Xi_3 \Delta Y + \tilde{\Theta}^T Q \tilde{\Theta} . \end{cases}$$
(34)

Using $0 \le |\dot{d}_t| \le \mu_t < 1$, then the time derivative of V_1 is as follows:

$$\dot{V}_{1} \leq \Delta Y^{T} \Xi_{1} \Delta Y - (1 - \dot{d}_{t}) \Delta Y(t - d_{t})^{T} \Xi_{1} \Delta Y(t - d_{t})$$

$$+ d_{t}^{2} \Delta \dot{Y}^{T} \Xi_{2} \Delta \dot{Y} - d_{t} \int_{t+d_{t}}^{t} \Delta \dot{Y}(\tau)^{T} \Xi_{2} \Delta \dot{Y}(\tau) d\tau$$

$$\leq \Delta Y^{T} \Xi_{1} \Delta Y - (1 - \mu_{t}) \Delta Y(t - d_{t})^{T} \Xi_{1} \Delta Y(t - d_{t})$$

$$+ d_{t}^{2} \Delta \dot{Y}^{T} \Xi_{2} \Delta \dot{Y} - d_{t} \int_{t+d_{t}}^{t} \Delta \dot{Y}(\tau)^{T} \Xi_{2} \Delta \dot{Y}(\tau) d\tau.$$
(35)

Following Lemma 2, we have the following:

$$-d_{t}\int_{t+d_{t}}^{t}\Delta\dot{Y}(\tau)^{T}\Xi_{2}\Delta\dot{Y}(\tau)d\tau$$

$$\leq -\left(\int_{t+d_{t}}^{t}\Delta\dot{Y}(\tau)d\tau\right)^{T}\Xi_{2}\left(\int_{t+d_{t}}^{t}\Delta\dot{Y}(\tau)d\tau\right)$$

$$\leq -(\Delta Y(t) - \Delta Y(t-d_{t}))^{T}\Xi_{2}(\Delta Y(t) - \Delta Y(t-d_{t})).$$
(36)

Using (16), (35) can be further rewritten as

$$\dot{V}_{1} \leq \Delta Y^{T} \Xi_{1} \Delta Y - (1 - \mu_{t}) \Delta Y(t - d_{t})^{T} \Xi_{1} \Delta Y(t - d_{t}) + d_{t}^{2} (K_{1} \Delta Y - K_{n} \Delta Y(t - d_{t}) + G \tilde{\Theta}^{T} \Psi(s))^{T} \cdot \Xi_{2} (K_{1} \Delta Y - K_{n} \Delta Y(t - d_{t}) + G \tilde{\Theta}^{T} \Psi(s)) - (\Delta Y - \Delta Y(t - d_{t}))^{T} \Xi_{2} (\Delta Y - \Delta Y(t - d_{t})).$$
(37)

Using (18), the time derivative of V_2 is as follows:

$$\dot{V}_{2} = 2\Delta \dot{Y}^{T} \Xi_{3} \Delta Y + 2 \stackrel{\circ}{\Theta}^{T} Q \stackrel{\circ}{\Theta}$$

= 2(K₁ \Delta Y - K_n \Delta Y(t - d_t) + G $\stackrel{\circ}{\Theta}^{T} \Psi(s)$)\Delta_3 \Delta Y (38)
- 2(g - y_0) \Delta Y^{T} Q $\stackrel{\circ}{\Theta} \Gamma \Psi(s)$.

Using (37) and (38), we can get the following:

$$\dot{V}_{1} + \dot{V}_{2} \leq \Delta Y^{T} (\Xi_{1} + 2K_{1}\Xi_{3} + (\overline{d}_{t}^{2}K_{1}^{2} - I)\Xi_{2})\Delta Y + Y(t - d_{t})^{T} (\overline{d}_{t}^{2}K_{n}^{2}\Xi_{2} - (1 - \mu_{t})\Xi_{1} - \Xi_{2})\Delta Y(t - d_{t}) + 2\Delta Y^{T} (\Xi_{2} - \overline{d}_{t}^{2}K_{1}K_{n}\Xi_{2} - K_{n}\Xi_{3})\Delta Y(t - d_{t}) + 2\Psi(s)\tilde{\Theta} [(G\overline{d}_{t}^{2}K_{1}\Xi_{2} + G\Xi_{3} + \Gamma Q(g - y_{0}))\Delta Y - \overline{d}_{t}^{2}GK_{n}\Xi_{2}\Delta Y(t - d_{t})] + \overline{d}_{t}^{2}G^{2}\Xi_{2}(\Psi(s)\tilde{\Theta})^{T}\Psi(s)\tilde{\Theta}.$$
(39)

Set a vector $Z = [\Delta Y, \Delta Y(t - d_t), \Psi(s) \tilde{\Theta}]^T$, then (39) can be expressed as

$$\dot{V}_1 + \dot{V}_2 \le \mathbf{Z}^T \Xi \mathbf{Z} \tag{40}$$

where Ξ is represented in (19), then Theorem 1 is proved.

B. Proof of Stability of the Shard-Control Framework

We build the following Lyaponov function:

$$V = V_{f}^{e} + V_{f}^{p} + V_{l}^{e} + V_{l}^{p}$$
(41)

where V_i^e is for position tracking to \hat{q}_i and V_i^p is for position tracking to the real value $q_i, i = l, f$. Taking the functions in the following controller as an example first, and V_f^e is as follows:

$$V_f^e = \frac{1}{2} \varepsilon_f^{\ T} M_f \varepsilon_f \tag{42}$$

where M_f is a positive diagonal matrix. The time derivative of V_f^e is as follows:

$$\dot{V}_{f}^{e} = \dot{\varepsilon}_{f}^{\ T} M_{f} \varepsilon_{f} + \frac{1}{2} \varepsilon_{f}^{\ T} \dot{M}_{f} \varepsilon_{f}.$$

$$\tag{43}$$

Following (31) and using Assumption 4, we have the following:

$$\begin{split} \dot{V}_{f}^{e} &= \varepsilon_{f}^{T} (-\xi_{1}\varepsilon_{f} - (1-\xi_{1})r_{f}^{dt} + J_{f}^{T}(q_{f})(\overline{F}_{e} - F_{e}) - C_{f}\varepsilon_{f} + \sigma) \\ &+ \varepsilon_{f}^{T}\dot{M}_{f}\varepsilon_{f}/2 \\ &= -\xi_{1}\varepsilon_{f}^{T}\varepsilon_{f} - (1-\xi_{1})\varepsilon_{f}^{T}r_{f}^{dt} - \varepsilon_{f}^{T}J_{f}^{T}(q_{f})(\overline{F}_{e} - F_{e}) - \varepsilon_{f}^{T}\sigma \\ &\leq -\xi_{1}\varepsilon_{f}^{T}\varepsilon_{f} - (1-\xi_{1})\varepsilon_{f}^{T}r_{f}^{dt}. \end{split}$$

$$(44)$$

For the tracking errors between the leader and the follower, we refer the Lyaponov function in (34) and set

$$V_f^p = k_1 r_f^T r_f + k_2 \int_{t-d_t}^t r_f^T r_f d\tau + \tilde{\theta}^T k_1 \tilde{\theta}$$
(45)

where $k_1 > 0$. Set $r_f^{dt} := r_f(t - d_t)$, the time derivative of V_f^p is as follows:

$$\dot{V}_{f}^{p} = 2k_{1}\dot{r}_{f}^{T}r_{f} + k_{2}r_{f}^{T}r_{f} - k_{2}(1-\dot{d}_{t})(r_{f}^{dt})^{T}r_{f}^{dt} + 2\dot{\tilde{\theta}}^{T}k_{1}\tilde{\theta}.$$
(46)

As the trajectories \hat{q}_l and q_l are generated by DMPs function in (5), according to (10), we can achieve the following equations:

$$\begin{cases} \tau^2 \ddot{q}_f = K(g - \hat{q}_f) - D\tau \dot{q}_f + (g - \hat{q}_0)f^u(s) - K_n r_f^{dt} \\ \tau^2 \ddot{q}_l = K(g - q_l) - D\tau \dot{q}_l + (g - q_0)f^n(s) \end{cases}$$
(47)

where $\hat{q}_0 = q_0$, representing the initial position for estimations and real values are the same. According to the definition of η_f and defining $\Delta f(s) = f^n(s) - f^u(s)$, we have the following:

...

$$\eta_{f} = \dot{q}_{l} - \dot{q}_{f}$$

$$= \frac{1}{\tau^{2}} (-K(q_{l} - \hat{q}_{f}) - D\tau(\dot{q}_{l} - \dot{q}_{f}) + (g - q_{0})\Delta f(s) + K_{n}r_{f}^{dt})$$

$$= -\frac{K}{\tau^{2}}\eta_{f} - \frac{D}{\tau}\dot{\eta}_{f} + \frac{K_{n}r_{f}^{dt}}{\tau^{2}} + \frac{g - q_{0}}{\tau^{2}}\Delta f(s).$$
(48)

Considering $f^n(s) = (\theta^n)^T \Psi(s)$ and $f^u(s) = (\theta^u)^T \Psi(s)$, $\Delta f(s) = f^n(s) - f^u(s) = (\theta^n - \theta^u)^T \Psi(s) = \tilde{\theta}^T \Psi(s)$, then

$$\ddot{\eta}_f = -\frac{K}{\tau^2}\eta_f - \frac{D}{\tau}\dot{\eta}_f + \frac{K_n r_f^{at}}{\tau^2} + \frac{g - q_0}{\tau^2}\tilde{\theta}^T \Psi(s).$$
(49)

So, for the term $\dot{r}_f = \ddot{\eta}_f + k_\eta^f \dot{\eta}_f$, we have the following:

$$\dot{r}_f = -\frac{K}{\tau^2}\eta_f + \left(k_\eta^f - \frac{D}{\tau}\right)\dot{\eta}_f + \frac{K_n r_f^{dt}}{\tau^2} + \frac{g - q_0}{\tau^2}\tilde{\theta}^T \Psi(s).$$
(50)

If we define factor k_{η}^{f} in (50) satisfying $\left(k_{\eta}^{f} - D/\tau\right) = -k_{\eta}^{f}K/\tau^{2}$, then we can get $k_{\eta}^{f} = D\tau/\tau^{2} + K$, and (50) can be simplified as

$$\dot{r}_{f} = -\frac{K}{\tau^{2}}\eta_{f} - k_{\eta}^{f}\frac{K}{\tau^{2}}\dot{\eta}_{f} + \frac{K_{n}r_{f}^{dt}}{\tau^{2}} + \frac{g - q_{0}}{\tau^{2}}\tilde{\theta}^{T}\Psi(s)$$

$$= -\frac{K}{\tau^{2}}r_{f} + \frac{K_{n}}{\tau^{2}}r_{f}^{dt} + \frac{g - q_{0}}{\tau^{2}}\tilde{\theta}^{T}\Psi(s).$$
(51)

Then (46) can be expressed as

$$\begin{split} \dot{V}_{f}^{p} &\leq 2k_{1}\dot{r}_{f}^{T}r_{f} + k_{2}r_{f}^{T}r_{f} - k_{2}(1-\mu_{t})(r_{f}^{dt})^{T}r_{f}^{dt} + 2\dot{\tilde{\theta}}^{T}k_{1}\tilde{\theta} \\ &= 2k_{1}\left(-\frac{\kappa}{\tau^{2}}r_{f} + \frac{\kappa_{n}}{\tau^{2}}r_{f}^{dt} + \frac{g-q_{0}}{\tau^{2}}\tilde{\theta}^{T}\Psi(s)\right)^{T}r_{f} + k_{2}r_{f}^{T}r_{f} - k_{2}(1-\mu_{t})(r_{f}^{dt})^{T}r_{f}^{dt} - 2\frac{g-q_{0}}{\tau^{2}}k_{1}\tilde{\theta}^{T}\Psi(s)r_{f} \\ &= \left(k_{2}-2k_{1}\frac{\kappa}{\tau^{2}}\right)r_{f}^{T}r_{f} + 2k_{1}\frac{\kappa_{n}}{\tau^{2}}r_{f}^{T}r_{f}^{dt} - k_{2}(1-\mu_{t})(r_{f}^{dt})^{T}r_{f}^{dt}. \end{split}$$
(52)

So, the time derivative of $V_f = V_f^e + V_f^p$ satisfies the following:

$$\dot{V}_{f} \leq -\xi_{1}\varepsilon_{f}^{T}\varepsilon_{f} - (1-\xi_{1})\varepsilon_{f}^{T}r_{f}^{dt} + \left(k_{2}-2k_{1}\frac{K}{\tau^{2}}\right)r_{f}^{T}r_{f} + 2k_{1}\frac{K_{n}}{\tau^{2}}(r_{f}^{dt})^{T}r_{f} - k_{2}(1-\mu_{t})(r_{f}^{dt})^{T}r_{f}^{dt}.$$
(53)

Similarly, we build Lyapunov functions for the leader side

$$V_{l} = V_{l}^{e} + V_{l}^{p}, \quad V_{l}^{e} = \frac{1}{2} \varepsilon_{l}^{T} M_{l} \varepsilon_{l}$$

$$V_{l}^{p} = k_{3} r_{l}^{T} r_{l} + k_{4} \int_{t-d_{t}}^{t} r_{l}^{T} r_{l} d\tau$$
(54)

and the time derivative of V_l^e and V_l^p are calculated as

$$\dot{V}_{l}^{e} = \dot{\varepsilon}_{l}^{T} M_{l} \varepsilon_{l} + \frac{1}{2} \varepsilon_{l}^{T} \dot{M}_{l} \varepsilon_{l} \le -\xi_{2} \varepsilon_{l}^{T} \varepsilon_{l} - (1 - \xi_{2}) \varepsilon_{l}^{T} r_{l}^{dt}$$
(55)

$$\dot{V}_{l}^{p} = 2k_{3}\dot{r}_{l}^{T}r_{l} + k_{4}r_{l}^{T}r_{l} - k_{4}(1-\dot{d}_{t})(r_{l}^{dt})^{T}r_{l}^{dt}.$$
(56)

According to the definition of r_l and (24), we have the following:

$$\begin{aligned} \dot{r}_{l} &= \dot{\eta}_{l}^{v} + k_{\eta}^{l} \dot{\eta}_{l}^{x} \\ \dot{\eta}_{l}^{x} &= \dot{q}_{f} - \dot{x}_{l} = \dot{q}_{f} - v_{l} - \ell k_{1} \eta_{l}^{x} = \eta_{l}^{v} - \ell k_{1} \eta_{l}^{x} \\ \dot{\eta}_{l}^{v} &= \ddot{q}_{f} - \dot{v}_{f} = \ell \Delta (q_{f}, \dot{q}_{f}, x_{l}, v_{l}, \tau_{f}, F_{e}) - \ell^{2} k_{2} \eta_{l}^{x} \\ \dot{r}_{l} &= \ell \Delta (q_{f}, \dot{q}_{f}, x_{l}, v_{l}, \tau_{f}, F_{e}) - \ell^{2} k_{2} \eta_{l}^{x} + k_{\eta}^{l} (\eta_{l}^{v} - \ell k_{1} \eta_{l}^{x}) \\ &= k_{\eta}^{l} \eta_{l}^{v} - (\ell k_{1} k_{\eta}^{l} + \ell^{2} k_{2}) \eta_{l}^{x} + \ell \Delta (q_{f}, \dot{q}_{f}, x_{l}, v_{l}, \tau_{f}, F_{e}). \end{aligned}$$

$$(57)$$

Set, $k_{\eta}^{l} = \ell/2(\pm\sqrt{k_{1}^{2}-4k_{2}}-k_{1})$, then we can get the following:

$$\dot{r}_{l} = k_{\eta}^{l} \eta_{l}^{\nu} + (k_{\eta}^{l})^{2} \eta_{l}^{x} + \ell \Delta(q_{f}, \dot{q}_{f}, x_{l}, \nu_{l}, \tau_{f}, F_{e})$$

$$= k_{\eta}^{l} r_{l} + \ell \Delta \Phi.$$
(58)



Fig. 2. Comparison of human demonstration and robot prediction trajectories. (a) Experimental setup. (b) Human demonstration trajectory and learned result using DMPs. (c)–(f) New task and trajectory predictions in a new environment using (10) (dashed red lines) and (60) (solid blue lines) with the time delays of 0.02, 0.08, $0.08 + 0.01\sin(t) + 0.02\cos(2t)$, and 0.1 s.

Using (56) can be expressed as

$$\dot{V}_{l}^{p} \leq 2k_{3}(k_{\eta}^{l}r_{l} + \ell\Delta\Phi)^{T}r_{l} + k_{4}r_{l}^{T}r_{l} - k_{4}(1 - \dot{d}_{t})(r_{l}^{dt})^{T}r_{l}^{dt} \\ \leq (2k_{3}k_{\eta}^{l} + k_{4} + 2k_{3}L_{\delta})r_{l}^{T}r_{l} - k_{4}(1 - \mu_{t})(r_{l}^{dt})^{T}r_{l}^{dt}.$$
(59)

Set vectors as $\Lambda_f = [\varepsilon_f, r_f, r_f^{dt}]$ and $\Lambda_l = [\varepsilon_l, r_l, r_l^{dt}]$, the sufficient condition for $\dot{V} \leq 0$ is $(\Lambda_f)^T E_1 \Lambda_f + (\Lambda_l)^T E_2 \Lambda_l \leq 0$, where E_1 and E_1 are shown in Theorem 2.

V. EXPERIMENTS

A. Comparative Simulations Using Omni Joystick

We use an Omni haptic phantom to interact with a simulation system built using MATLAB/Simulink for trajectory prediction and teleoperation control. The first simulation is to compare the DMPs-based prediction method with a comparative method for estimating human motion that is deduced from [4]

$$\dot{\hat{X}}_{f} = \Upsilon_{1}(\hat{X}_{f} + X_{f}) + \Upsilon_{n}(X_{l}(t - d_{t}) - \hat{X}_{f}(t - d_{t}))$$
(60)

where
$$\Upsilon_1 = \begin{bmatrix} -0.3 & 0 \\ 0 & -0.3 \end{bmatrix}$$
 and $\Upsilon_n = \begin{bmatrix} -20 & 0 \\ 0 & -20 \end{bmatrix}$.

Using a joystick illustrated in Fig. 2(a), we draw a trajectory from [2] and [3] to [10] and [12] crossing two obstacles, and the learned results are presented in Fig. 2(b). Fig. 2(c)–2(f) illustrates a new demonstration trajectory (red solid lines) from [3] and [4] to [9] and [11]. The trajectories are predicted by (10) and (60) with different time delays, shown as dashed red and solid blue lines. Regarding DMPs learned in the form of (5), the parameters are set $K = 200, D = 28, \tau = 0.01$ to learn f(s) and transfer that to (10) to generate a new trajectory to approach a new target by overcoming two obstacles. For the observers in (10) and (60), we compare the predictive trajectories by choosing time delays as 0.02, 0.08, (0.08 + 0.01sin(t)+ 0.02cos(2t)), and 0.1 s.



Fig. 3. Comparison of human demonstration and robot trajectories prediction of letters A, C, and E with different time delays of 0.02, 0.1, and 0.4 s. (a)–(c) Results using the predictor (60). (d)–(f) Results using the predictor (10).

We can see from Fig. 2(c)-2(f) that under the short constant time delay of 0.02 s both trajectories estimated by two observers align well with human demonstrations. Upon increasing time delays to 0.08 s or even 0.1 s, the results of (60) suffer a heavier influence, resulting in larger tracking errors compared to those of (10). The fluctuation in time delays exacerbates the influence of time delays on the prediction accuracy of (60) but has a limited effect on the observer of (10). In addition, the observer of (60) is unable to guide the trajectory to the target and only reaches the surrounding region as indicated by the gray square. In contrast, the DMPs-based observer keeps stable observations, exhibits smaller prediction errors, approaches the target, and is less influenced by time delays.

Here, we further compare the predicting complex trajectories of two predictors of writing letters A, C, and E with different time delays in Fig. 3. We can observe that for the short time delays like 0.02 and 0.1 s, both the predicted trajectories have smaller errors to the demonstrations, which are presented in red solid lines. Only for the letter E, the tracking differences to the demonstrations using (60) are smaller than the results using (10). Comparatively, with the increment of time delays to 0.4 s, the tracking trajectories of the predictor (60) seriously leave away from the demonstration and do not approach the target finally, while the proposed DMPs-based prediction can reach the destination even though the position-tracking errors are much larger than those with small time delays.

The second simulation uses the Omni to get human inputs for a virtual teleoperation system consisting of a two-Degree of Freedom (DoF) robot and a two-DoF manipulator with parameters: $m_l^1 = 0.12 \text{ kg}, m_l^2 = 0.14 \text{ kg}, m_f^1 = 0.23 \text{ kg}, m_f^2 = 0.46 \text{ kg}, l_f^1 = l_l^1 = 0.3 \text{ m}, l_f^2 = l_l^2 = 0.3 \text{ m}, I_l^1 = 0.01 \text{ kg} \cdot \text{m}^2, I_l^1 = 0.02 \text{ kg} \cdot \text{m}^2, I_f^1 = 0.03 \text{ kg} \cdot \text{m}^2, I_f^1 = 0.03 \text{ kg} \cdot \text{m}^2, \text{ where } m_i^j, l_j^i, \text{ and } I_j^i, i = 1, 2, j = l, f$ represent the mass, link length, and inertia of link *i* of agent *j*, and the time delay is d(t) = 0.2 + 0.05 sin(t) + 0.02 cos(t/2). Fig. 4(b) shows a demonstration of crossing an obstacle and the learned results using DMPs. The results are then generalized to create a new trajectory (blue dotted line) in Fig. 4(c), connecting the start and the end of the new



Fig. 4. Teleoperation based on the proposed framework. (a) Experimental setup. (b) Human demonstrations. (c) Trajectories in the leader and follower sides with time delays of 0.2 + 0.05sin(t)+0.02cos(t/2). (d) Parameters changes for the weight vector. (e) Comparisons of trajectories with different time delays 0.2. 0.6, and 1.0 s. (f) Comparison with the shared controller in [14].

humans trajectory (black solid line). Using controllers (26) and (32), the robot trajectory is depicted as the red dashed line in Fig. 4(c). Throughout the control process, we set $\xi_1 = \xi_2 = 0.5$ to enable robots and humans to share control authority equally. The elements in the weight vector θ^{u} in (28) are updated timely and the weight parameters' changes are presented in Fig. 4(d). Fig. 4(e) illustrates the influence of different time delays on the positiontracking performance. It can be observed that with the increase in time delays, the position-tracking deviations become larger than those with smaller time delays. Fig. 4(f) illustrates a comparison of the proposed method with the shared controller in [14], which is a position-level shared controller integrating TP-HSMM and human inputs with the same sharing coefficient $\xi_1 = 0.5$ ($\alpha = 0.5$ in [14]). We used the same human inputs as those in the controllers (26) and (32). The generated trajectory (blue lines) deviates away from the human inputs due to the inaccurate predictions of human actions. In contrast, the method in (10) can correct predictions based on delayed human inputs and achieve smaller tracking errors (red dashed line).

B. Experiments on Franka robot

In this experiment, we apply the framework shown in Fig. 1 to the Franka robot. First, we demonstrate the Franka robot in a low-stiffness dragging state and hold the handle of the Franka to cross an obstacle as depicted in Fig. 5(a). The trajectory is then learned using (5) to acquire the basic skill of overcoming an obstacle. Subsequently, we configure controllers for both the robot and the Omni joystick on the same laptop and simulate the communication channels and time delays through software programming. The control signals and haptic feedback are then published separately to the robot and joystick sides to generate robot actions and haptic force on human hands. Simultaneously, real-time actions of robots and human inputs are collected and delivered to the laptop to generate future control commands. Fig. 5(b) presents the process in which an operator teleoperates the Franka to reach a



Fig. 5. Human demonstrations and DMPs-based shared-control teleoperation. (a) Human demonstrations. (b) Human shared-control teleoperation. (c) Robot execution under the proposed shared-control teleoperation. (d) Robot execution using autonomous robot control to follow the DMPsgeneralized trajectory.

new target position and Fig. 5(c) illustrates a close view of the process of crossing a higher obstacle. For comparison, we implement robot autonomous control using the DMPs-based generalized results [27], in a nonsharing control case. As shown in Fig. 5(d), there are conflicts during the robot crossing process and leading to the pushing down the obstacle. Bilateral control can also enable robots to reach the target without conflicts, but due to the time delays, it requires a longer time to wait for robots to complete actions and feedback.

In Fig. 6, we generalized the learned skill and applied that to a more complex scenario, where the robot is required to cross two obstacles and contact positions 1–4 in sequence, which are presented in Fig. 6(a), and the two obstacles have different heights. We compare the results of using a trajectory generalized by DMPs and a trajectory based on shared-control teleoperation with a DMP-based observer and the experimental process is illustrated in Fig. 6(b) and 6(c). There are three crosses during the process in both two cases, the robot can overcome the higher obstacle and contact the designed positions. During the third cross, the robot end controlled by the shared control is closer to the top height of the lower obstacle, which is presented as the smaller Δh in Fig. 6(c).

We conduct another experiment of writing letters. The robot was controlled in real-time teleoperation to write two letters: 'L' and 'C,' and the motions of the robot's ends were recorded for training purposes. The motions learned from one letter using ordinary DMPs were transferred to write the other letter. New writings of one letter were generated through shared control between the delayed teleoperation motions of the other letter



Fig. 6. Human demonstrations and DMPs-based shared-control teleoperation. (a) Experimental setup. (b) Robot execution using autonomous robot control to follow the DMPs-generalized trajectory. (c) Robot execution using shared-control teleoperation based on DMPs-based observer.



Fig. 7. Human demonstrations and DMPs-based shared-control teleoperation (a) trajectory transfer from L to (b) human shared-control teleoperation.

and the generalized DMPs trajectory using (26) and (32). The results are presented in Fig. 7(a2) and 7(b2). These results are further detailed in Fig. 7(a3) and 7(b3) to illustrate the influence of time delays more clearly. It is evident that due to the time delays, in the initial stage, the trajectories exhibit varying levels of deviation. The deviations in trajectories with larger time delays (2 s) are more significant than those with smaller time delays (0.1 s), as depicted in the zoomed figures.

VI. CONCLUSION

In this article, we developed a DMPs-based observer to predict human motion intentions and applied this observer for the shared control of teleoperation. The experimental results present that, compared with other observers and shared-control frameworks, the proposed observer can accurately predict long-term human action intentions and correct prediction errors using the delayed signals to establish consistency between the predicted actions of robots and the actual human operational actions. The DMPs-based observer contains human operational features, ensuring stable operational outputs despite the changes in time delays, this is particularly beneficial for long-distance operations with time delays. We prove the convergence of the estimation and system stability of the control framework with two observers by building two Lyapunov functions as well. Future work has two directions. First, we aim to consider varying sharing factors in (26) based on the objective conditions or requirements of robot manipulation. Second, we aim to extend the DMPs-based shared-control teleoperation framework for a wider range, such as multirobot coordination.

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